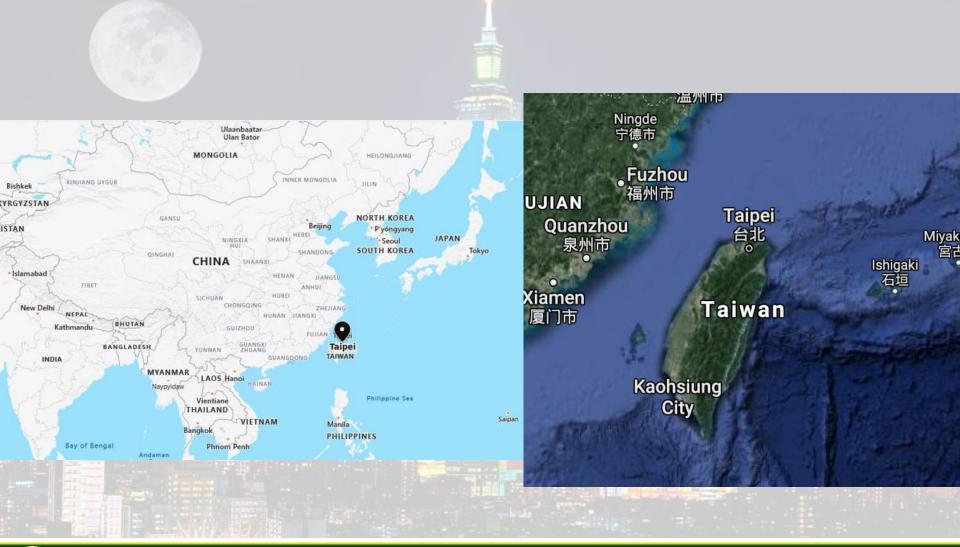


QCD on the Lattice



Few Personal Facts

§ I am from a small town in Taiwan; PhD at Columbia U





Few Personal Facts

§ I am from a small town in Taiwan; PhD at Columbia U
§ Preferred pronoun: she/her
§ Since NYC, I've lived in Virginia, Seattle, and the Bay Area
> My biggest worry when I moved to the Midwest: snowstorms
§ Like many women in physics, I married a physics PhD, and often find myself the only female in the room
> I started a number of diversity-related activities (social events, surveys, codes of conduct, etc.)









Few Personal Facts

- § I am from a small town in Taiwan; PhD at Columbia U § Preferred pronoun: she/her
- § Like many women in often find myself the
 My Journey
- I started a number of (social events, survey)
- A Podcast
- § My research is in quantum chromodynamics (QCD)
 I use high-performance supercomputers to study the properties of the quarks and gluons in the hadrons (nucleon, pion, ...)



My Journey as a Physicist

Season 3: <u>Nuclear-Science Advisory Committee</u> Long Range Plan (LRP)

This season's interviews were conducted by Bill Good and Kinza Hasan, and edited by Kiran Sakorikar and Esther Cohen-Lin.

Episode 1 (flyer) (transcript) Prof. Gail Dodge (she/her) **Old Dominion University**



Probing the Heart of Matter

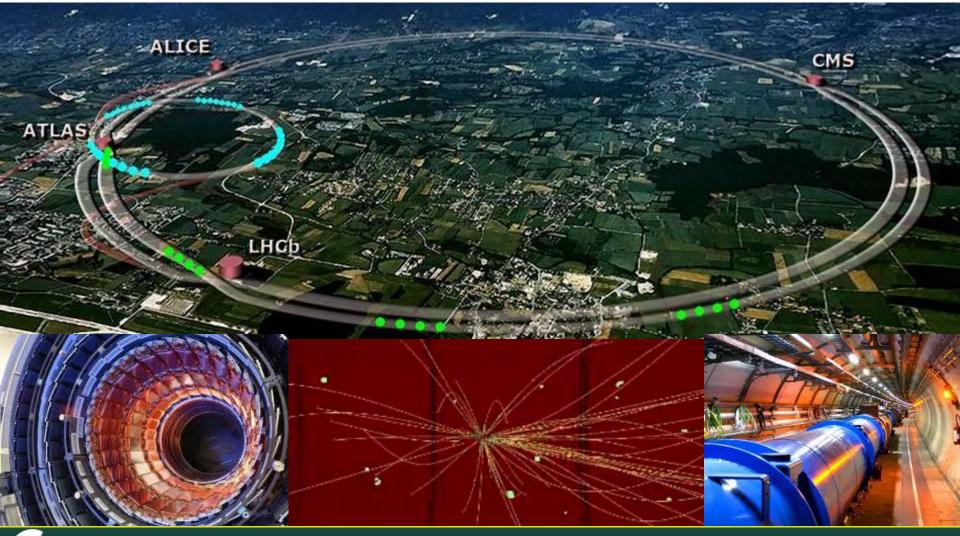
§ Our natural instinct: Smash!





Probing the Heart of Matter

§ LHC strikes out onto the high-energy frontier (13 TeV)



MICHIGAN STATE

Probing the Heart of Matter

§ The Electron-Ion Collider (EIC): The Ultimate QCD Microscope

The Electron-Ion Collider

A machine that will unlock the secrets of the strongest force in Nature

https://www.bnl.gov/eic/

EIC White Paper, 1212.1701; EIC Yellow Report (2103.05419); The Present and Future of QCD (2303.02579)



Probing the Heart of Matter

§ Calculations done using world's largest supercomputers
 Many millions of CPU/GPU hours







Lecture Plan

§ Lecture Plan (Mon)

✤ Why lattice QCD? > Anatomy of a lattice calculation > Spectroscopy example § Lecture Plan (Tue) >>> Lattice calculation of hadron structure Source Charges, moments and form factors Proton spin/mass decomposition *∞ x*-dependent parton distributions Source Recent lattice PDFs progress Applications to GPDs Future prospects and challenges



From Thy Standard Model to Lattice QCD



The Standard Model and QCD

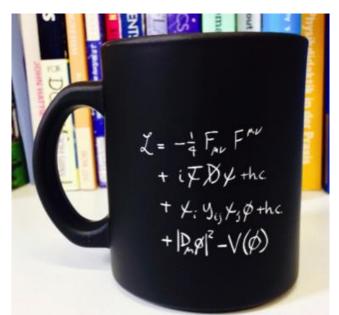


Image credit: CERN

§ Quantum chromodynamics (QCD)

The strong interactions of quarks and gluons (SU(3) gauge)



Image source: https://www.particlezoo.net



Learn QCD on Your Phone!



Chris Oakley @DrPhysOaks · Mar 21 Replying to @NSF_MPS and @michiganstateu

...and my seven year old is explaining to me how to create Xi - ...



MICHIGAN STAT

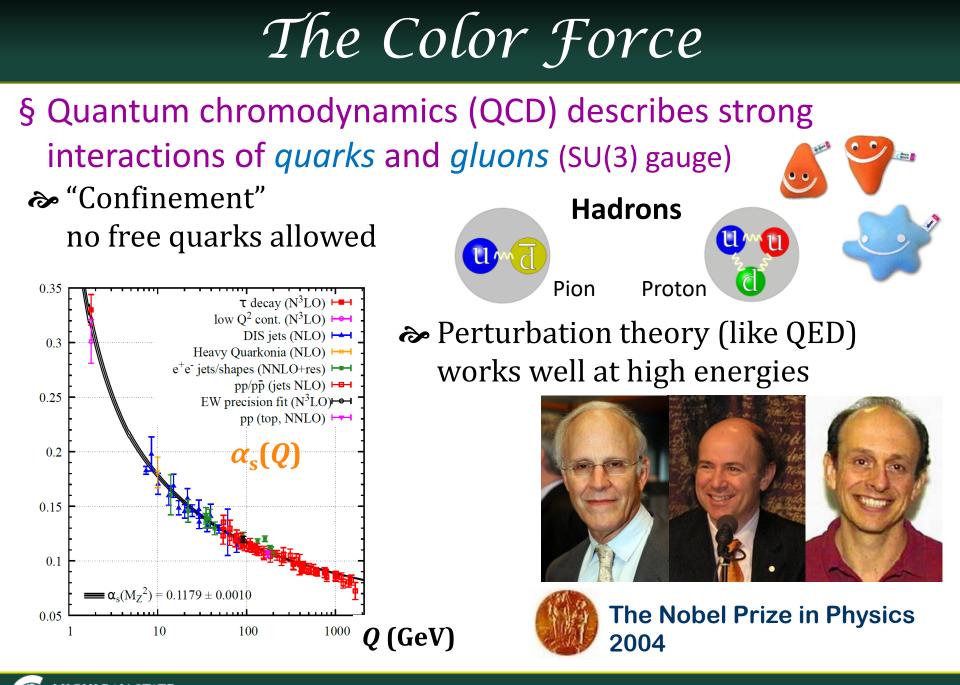
Learn QCD on Your Phone!



Supported by the NSF under grant PHY 1653405

MICHIGAN STAT

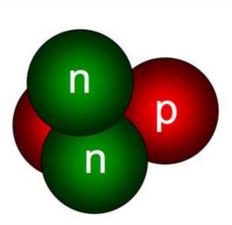


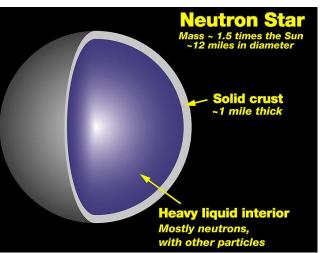


Wide-Scale Applications

§ What can we learn from it?







10⁻¹⁵ m

10⁴ m

Origin of proton mass and spin, imaging of proton, Parton distribution functions For new-physics searches, ... Nuclei and why we exist

Neutron matter How they evolve



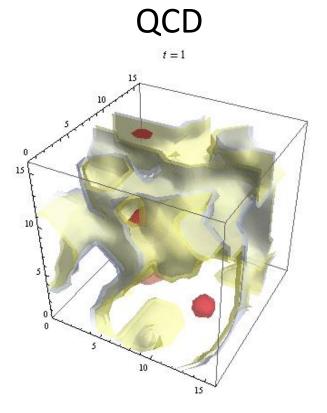


Difficulties at Low Energy

§ Even just the vacuum of QCD is complicated

Classical

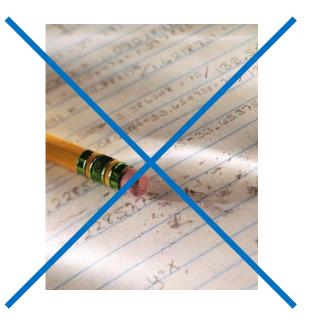


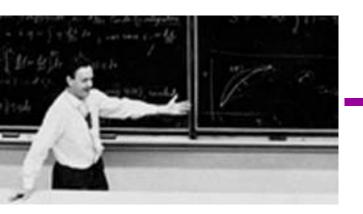


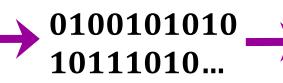


Difficulties at Low Energy

- § Strong interactions make analytic calculation impossible
- § Direct QCD calculation is desired → Lattice QCD



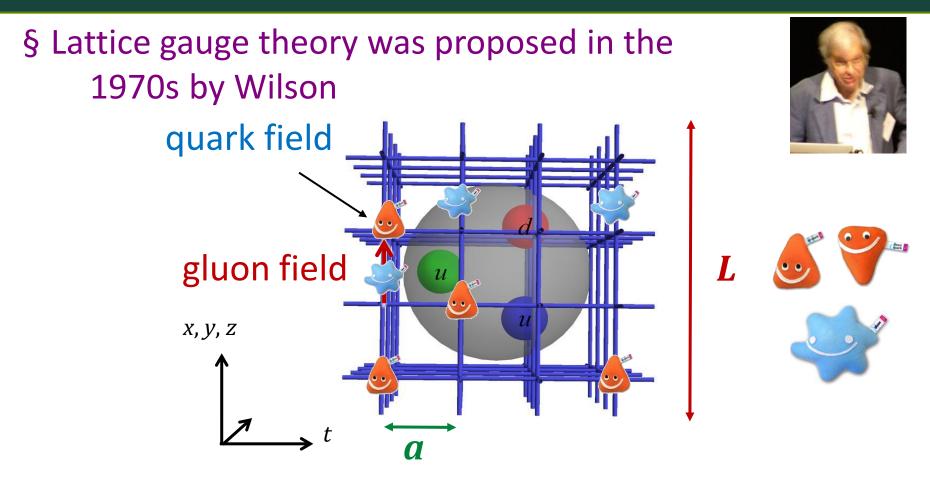








Wilson Comes to Rescue!



§ Recover physical limit $m_q \rightarrow m_q^{\text{phys}}, a \rightarrow 0, L \rightarrow \infty$

Introducing the Lattice

 § Lattice QCD is an ideal theoretical tool for investigating strong-coupling regime of quantum field theories
 § Physical observables are calculated from the path integral

$$\langle 0 | O(\bar{\psi}, \psi, A) | 0 \rangle = \frac{1}{Z} \int \mathcal{D}A \mathcal{D}\bar{\psi} \mathcal{D}\psi \ e^{iS(\bar{\psi}, \psi, A)} O(\bar{\psi}, \psi, A)$$

n **Euclidian** space

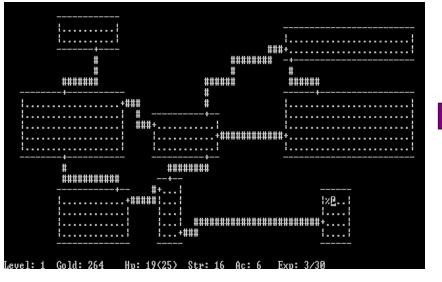
Quark mass parameter (described by m_{π})
Impose a UV cutoff discretize spacetime
Impose an infrared cutoff finite volume
S Recover physical limit $m_{\pi} \rightarrow m_{\pi}^{\text{phys}}, a \rightarrow 0, L \rightarrow \infty$ x, y, z y,



İr

Are We There Yet?

- § Lattice gauge theory was proposed in the 1970s by Wilson
- > Why haven't we solved QCD yet?
- § Progress is limited by computational resources 1980s Today





§ Greatly assisted by advances in algorithms Physical pion-mass ensembles are not uncommon!



1. Hardware (computational resources) and Software (Code)

If you are young and energetic...

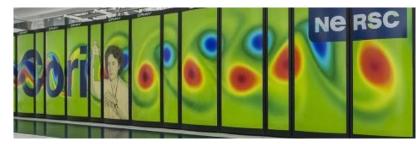




FNAL pi0 Cluster (USQCD SciDAC)



Stampede2@TACC (NSF ACCESS)



Cori@NERSC (DOE ERCAP, ALCC)

1. Hardware (computational resources) and Software (Code)

US Lattice Quantum Chromodynamics

USQCD has developed a suite of software enabling lattice QCD computations to be peformed with high performance across a variety of architectures, including both custom facilities and commodity clusters. This software is made up of software library modules that can be re-used by higher level applications. The approximate organisation of the packages into layers is depicted below (we omit here 3rd party packages or packages auxiliary to another package). Please click on the plaquettes below to find project web pages of the individual software modules, as well as to complete lattice QCD packages which use them.

Chroma	CPS		FUEL		MILC		C	QLUA
Inverter I		MD	WF	QOPQD		P		QUDA
QDP++			QDP			QIO		
QLA			QMP			QMT		
Figure 1: The SciDAC Layers and the software module architecture.								

§ The lattice community shares much software \gg for example, many in the US lattice community use code from http://usqcdsoftware.github.io



1. Hardware (computational resources) and Software (Code) Online tutorials available:

http://www.int.washington.edu/PROGRAMS/12-2c/

Week 3 (Aug. 20-24, 2012)

- "Hadron Structure", James Zanotti (University of Adelaide)
- "Lattice QCD+QED", Taku Izubuchi (BNL)
- Computational Lattice QCD", Balint Joo (Thomas Jefferson Lab)
 - Exercises: seattle tut.tar.gz (2012 Aug 24)
 - Code: <u>package-int.tar.gz</u> (110 MB)
 - Lecture 1: <u>Slides</u> <u>Video</u>
 - Lecture 2: <u>Slides</u> <u>Video</u>
 - Lecture 3: <u>Slides Video</u>
 - Lecture 4: <u>Slides</u> <u>Video</u>
 - Lecture 5: <u>Slides Video</u>
- "Extreme Computing Trilogy: Nuclear Physics", <u>Martin Savage</u> (University of Washington)
- "Cold Atoms and Unitary Fermi Gas", Michael M. Forbes (INT)
- "Introduction to GPU Computing", Mike Clark (NVIDIA)
- "Introduction to QUDA GPU Computing for LQCD", Mike Clark (NVIDIA)
- "Extreme Computing Trilogy: Infrastructure", Kenneth Roche (PNNL)

Problem Solv

slack

uria

OL

Lecture playlist: https://www.youtube.com/watch?v=FsN34Sm6Ldo&list=PLDi14w7i5C3Bm3U1IQ4n596U ZQhOpr1Cx



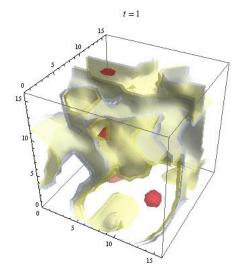
MAnchor.

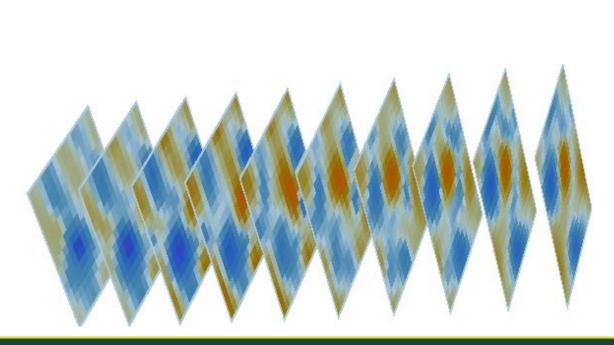
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Schoo

1. Hardware (computational resources) and Software (Code)

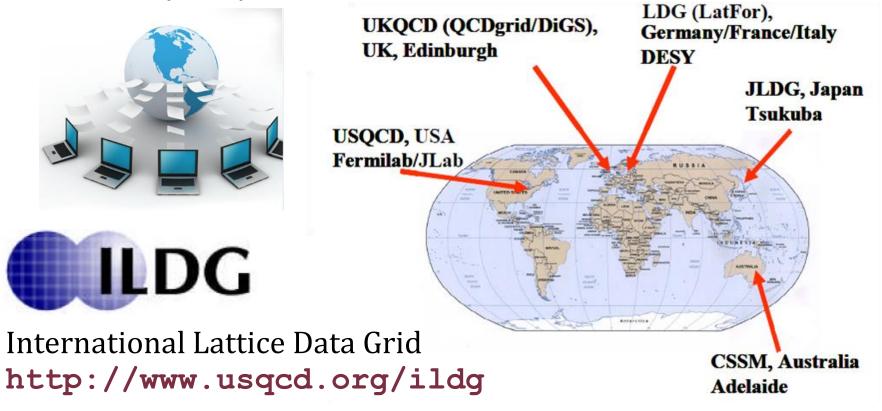
2. Some QCD Vacuum (gauge configurations)







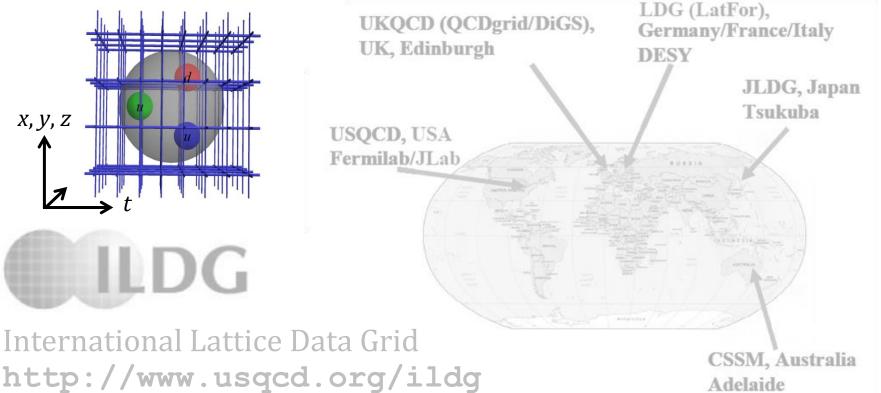
1. Hardware (computational resources) and Software (Code)





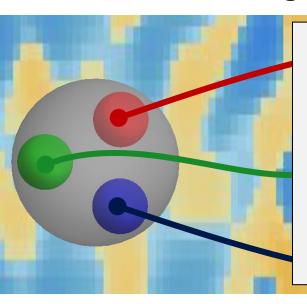
1. Hardware (computational resources) and Software (Code)

- 2. Some QCD Vacuum (gauge configurations)
- ➢ WWW (ILDG) or generate it yourself 0810.3588 350+





- 1. Hardware (computational resources) and Software (Code)
- 2. Some QCD Vacuum (gauge configurations)
- 3. Correlators (hadronic observables)
 Invert Dirac operator matrix (rank 10¹²)
 Combine using color, spin and momentum into hadrons



§ Simple hadron operators (not unique)

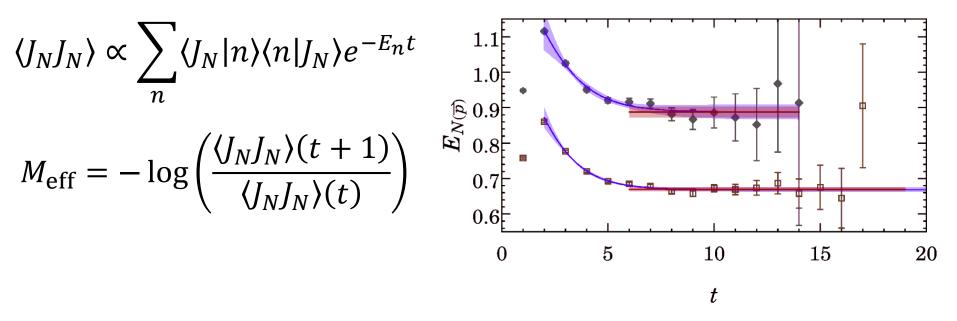
$$\approx \pi^+(x) = \bar{u}^a(x)\gamma_5 d^a(x)$$

 $\approx \rho^+(x) = \bar{u}^a(x)\gamma_\mu d^a(x)$
 $\approx p_\delta(x) = (\bar{u}^a(x)C\gamma_5 d^b(x))u_\delta^c \epsilon_{abc}$
 $\approx \Delta_{\mu,\delta}^{++}(x) = (\bar{u}^a(x)C\gamma_\mu u^b(x))u_\delta^c \epsilon_{abc}$

Time

Exercise: 1) Derive the time-dependent correlator formula. How does it differ between the pion and nucleon?
2) Are there other ways to define M_{eff}? Can you find an M_{eff} that gives the mass of the first radially excited state?

4. Analysis (extraction of masses or couplings)





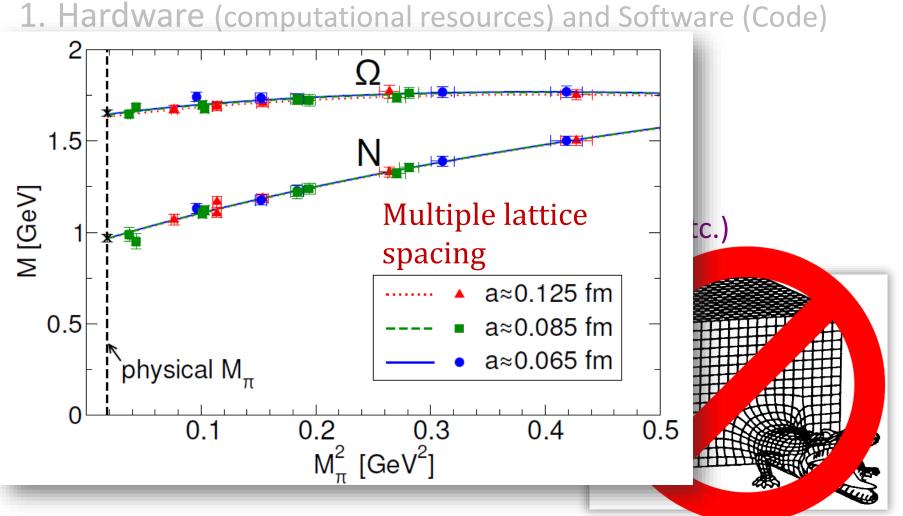
- 1. Hardware (computational resources) and Software (Code)
- 2. Some QCD Vacuum (gauge configurations)
- 3. Correlators (hadronic observables)
- 4. Analysis (extraction of masses or couplings)
- 5. Systematic Uncertainty (nonzero *a*, finite *L*, etc.)

Extrapolation to the continuum limit

 $(m_{\pi} \rightarrow m_{\pi}^{\text{phys}}, L \rightarrow \infty, a \rightarrow 0)$







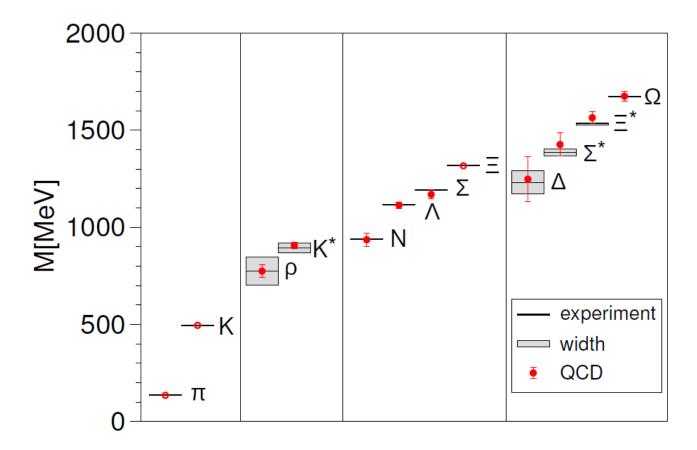
BMW Collaboration, Science (2008)



Lattice in the News

§ Post-dictions of well known quantities

➢ Example: BMW Collaboration, Science 2008

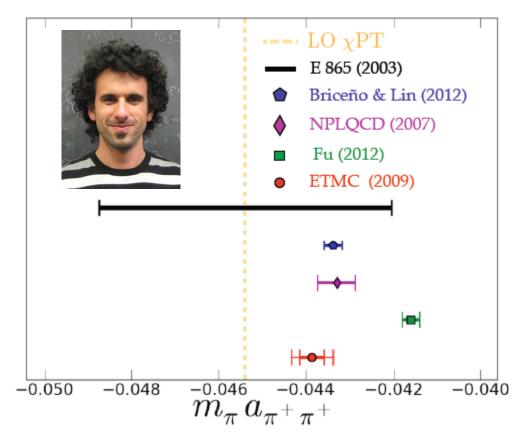




Successful Examples

§ Provide higher precision for known quantities

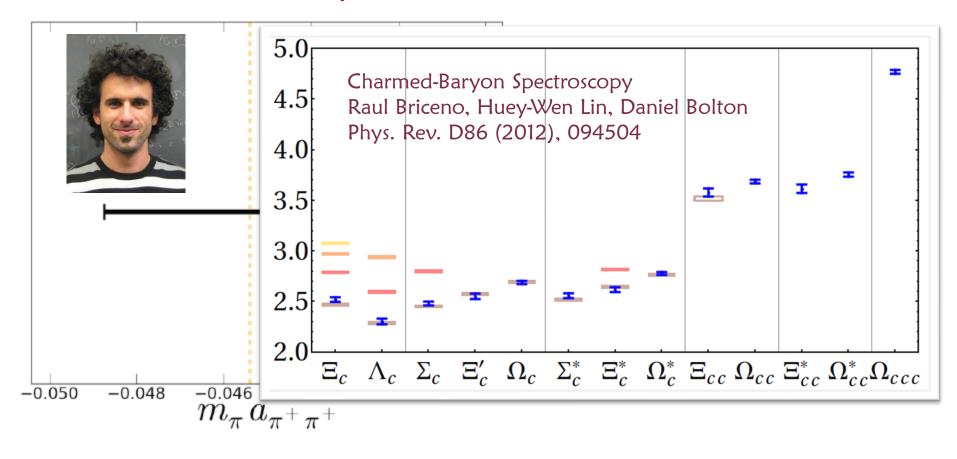
§ Make a lot of mass predictions





Successful Examples

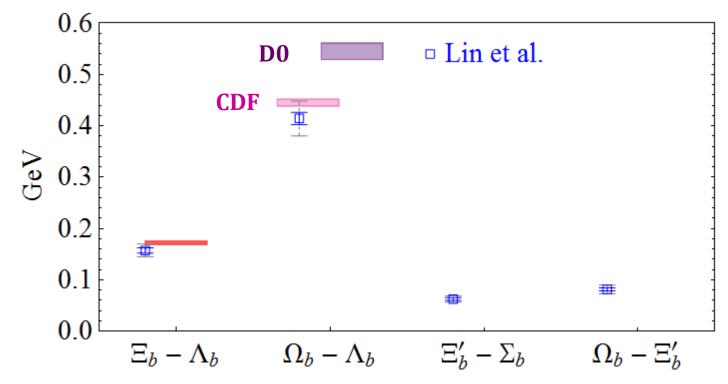
§ Provide higher precision for known quantities§ Make a lot of mass predictions





Bottom Baryons

§ Inconsistency in the CDF and DØ results for Ω_b mass \gg Our Ω_b agrees with the CDF result

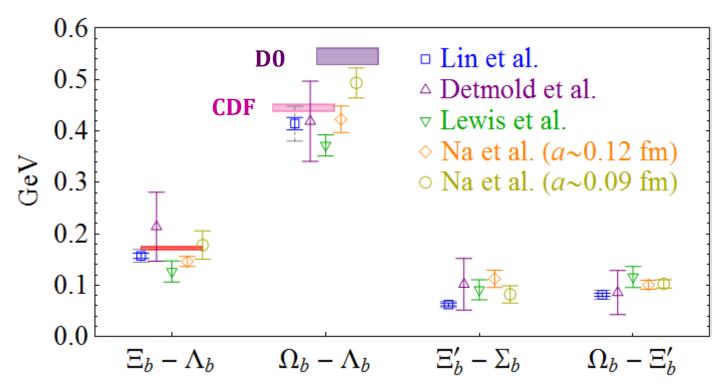


HWL, S. D. Cohen, N. Mathur, K. Orginos, Phys. Rev. D80, 054027 (2009)



Bottom Baryons

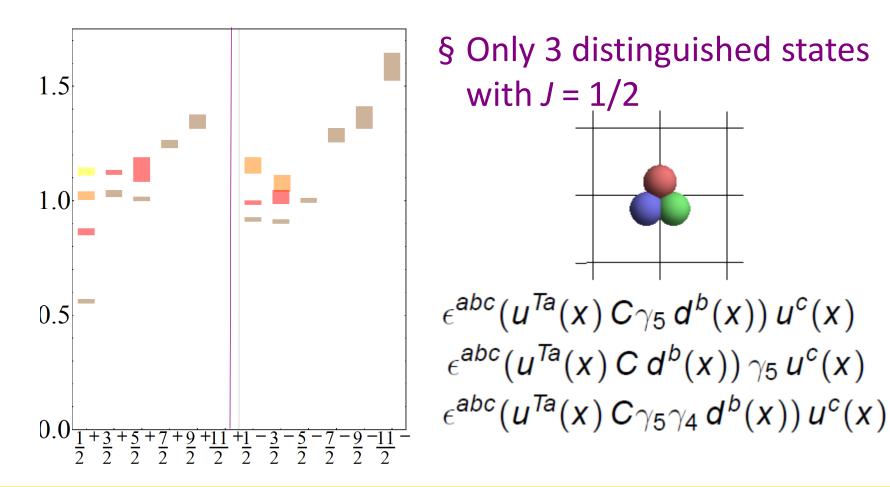
§ Inconsistency in the CDF and DØ results for Ω_b mass \gg Our Ω_b agrees with the CDF result



HWL, S. D. Cohen, N. Mathur, K. Orginos, Phys. Rev. D80, 054027 (2009);
W. Detmold et al., (2008), 0812.2583[hep-lat]; R. Lewis et al., PRD79, 014502 (2009);
H. Na et al., PoS LATTICE2008, 119 (2008).

Nucleon

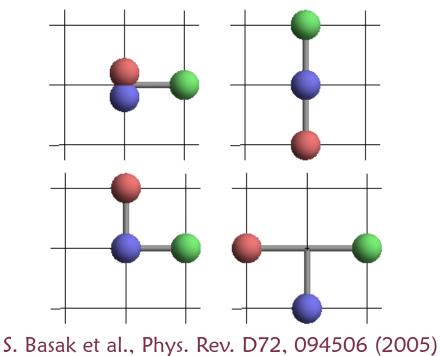
§ All baryon spin states wanted: |J| = 1/2, 3/2, 5/2, ... § List of 4-star states



Nucleon

§ Rotation symmetry is reduced rotation SO(3) \Rightarrow octahedral O_h group

> § Include more quark orientations

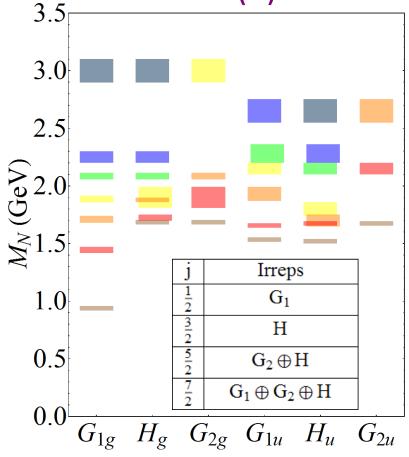


j	Irreps
$\frac{1}{2}$	G ₁
$\frac{3}{2}$	Н
$\frac{5}{2}$	$G_2\oplus H$
$\frac{7}{2}$	$G_1 \oplus G_2 \oplus H$

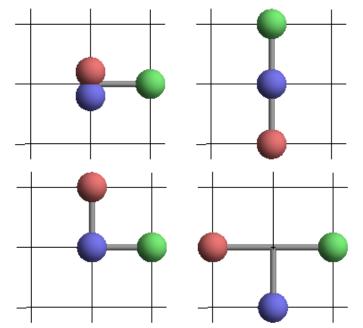


Nucleon

§ Rotation symmetry is reduced rotation SO(3) \Rightarrow octahedral O_h group



§ Include more quark orientations



§ More details on operators: check out this YouTube video

Variational Method

§ Recall: still a coupling problem

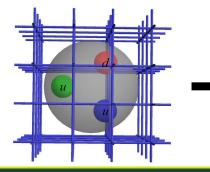
lowest-mass state dominates $C(t) = \sum_{n} \langle O | n \rangle \langle n | O \rangle e^{-E_n t}$

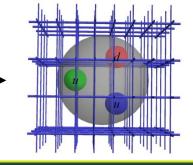
§ Decouple them:

- 1. Construct correlator matrix $C_{i j}(t) = \langle 0 | \mathcal{O}_i(t)^{\dagger} \mathcal{O}_j(0) | 0 \rangle$
- 2. Solve the gen. eigensystem $C(t_0)^{-1/2}C(t)C(t_0)^{-1/2}\psi = \lambda(t,t_0)\psi$
- 3. Simple analysis of eigenvalues (t-dependence) to get each excited state $\lambda_n(t, t_0) = e^{-(t-t_0)E_n}(1 + O(e^{-|\delta E|(t-t_0)}))$

C. Michael, Nucl. Phys. B 259, 58 (1985)

M. Lüscher and U. Wolff, Nucl. Phys. B 339, 222 (1990) § Higher resolution (at least in time direction)

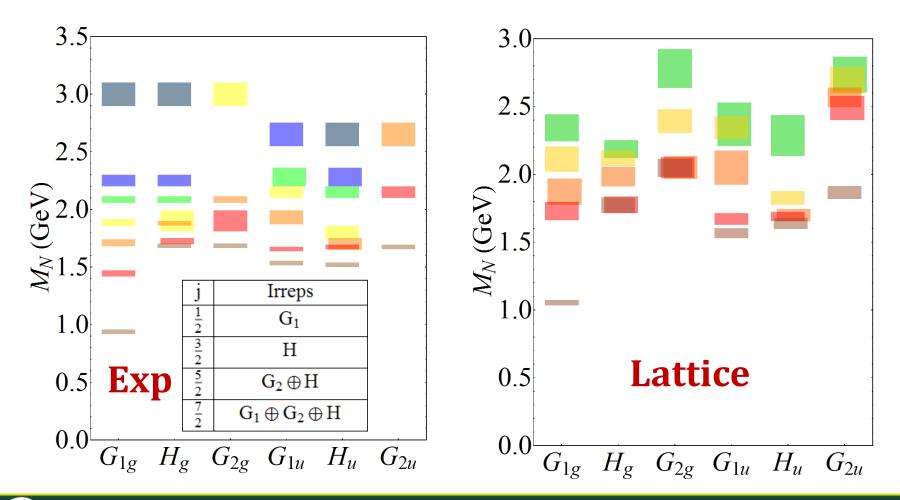




R. Edwards, B. Joo, HWL, Phys. Rev. D 78, 014505 (2008); HWL et al., Phys. Rev. D 79, 034502 (2009)

 $\mathcal{N}_{f} = 2+1$ Study: Nucleon

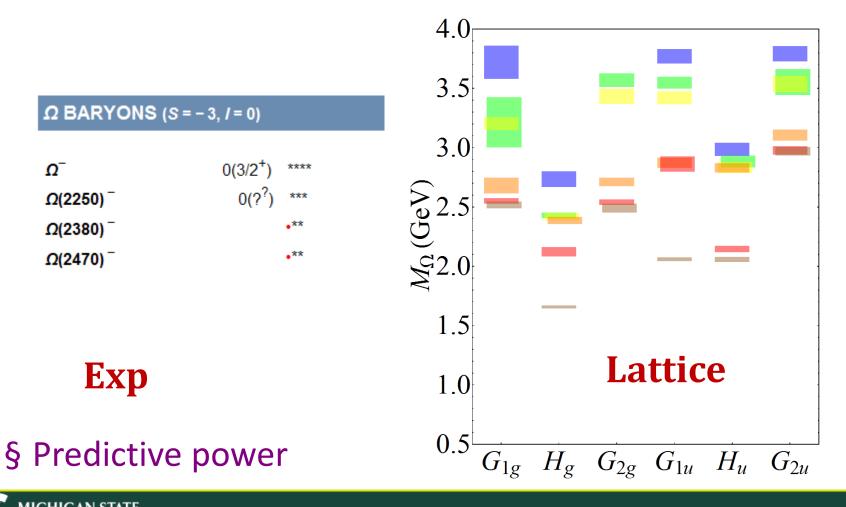
§ $N_f = 2+1$, anisotropic clover action $V = 16^3 \times 128$, $a_s \approx 0.12$ fm, $a_s/a_t \approx 3.5$, $M_\pi \approx 390$ MeV HSC, 1004.5072[hep-lat]





Less Known Case

§ $N_f = 2+1$, anisotropic clover action HSC, 1004.5072[hep-lat] $V = 16^3 \times 128$, $a_s \approx 0.12$ fm, $a_s/a_t \approx 3.5$, $M_\pi \approx 390$ MeV



If time allows...

Learning by Doing!

- § Prior Python with Jupyter notebook experience required
- How many of you have not used these before?
- § Form groups of about 4 students
- > Rearrange the tables so your group is sitting together
- § Introduce yourself to the other students in your group (5-10 mins)
 - > Name and preferred pronoun
- > Where are you from and tell us a few things about the place
- If you could hang out with any cartoon character, who would you choose and why?
- > Make sure you listen to each other!

Hands-on Exercíse

§ Hands-on exercise (scan the QR code to access the Jupyter notebooks)

- Always starts with "pre-class" notebook before moving on to "in-class" one
 - Set01: Jackknife analysis (Mon)
 - Set02: Calculating proton masses (Mon)
 - Set03: Extracting nucleon charges (Tue)









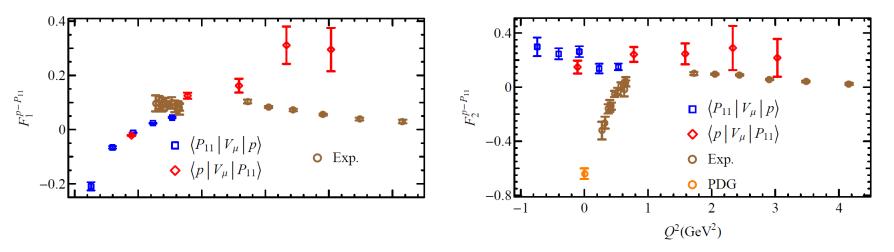


§ Challenge: Resonances and multiple-particle final states

- Neutrino scattering above the pion-production threshold, where the scattered nucleon is excited into resonances
- ➢ Inputs: need knowledge on N → ∆ and N → N^{*}

 $\gg N - P_{11}$ transition EM form factors

$$\gg \left\langle N_2 \left| V_{\mu} \right| N_1 \right\rangle_{\mu}(q) = \bar{u}_{N_2}(p') \left[F_1(q^2) \left(\gamma_{\mu} - \frac{q_{\mu}}{q^2} \not{q} \right) + \sigma_{\mu\nu} q_{\nu} \frac{F_2(q^2)}{M_{N_1} + M_{N_2}} \right] u_{N_1}(p) e^{-iq \cdot x}$$

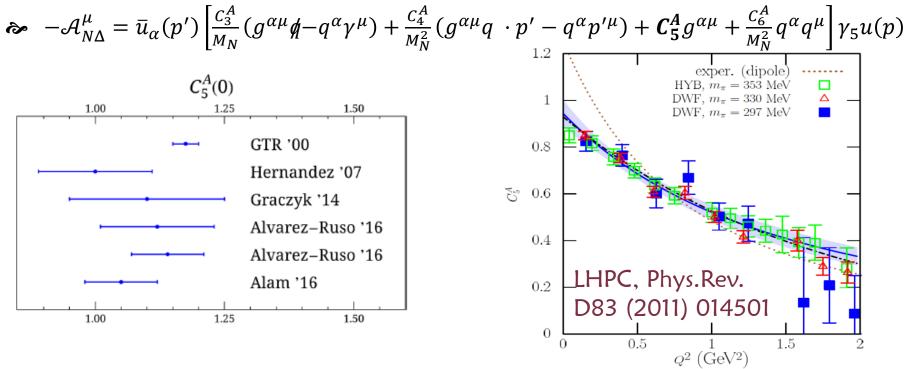


Lin et al, Phys.Rev.D78 (2008), 114508



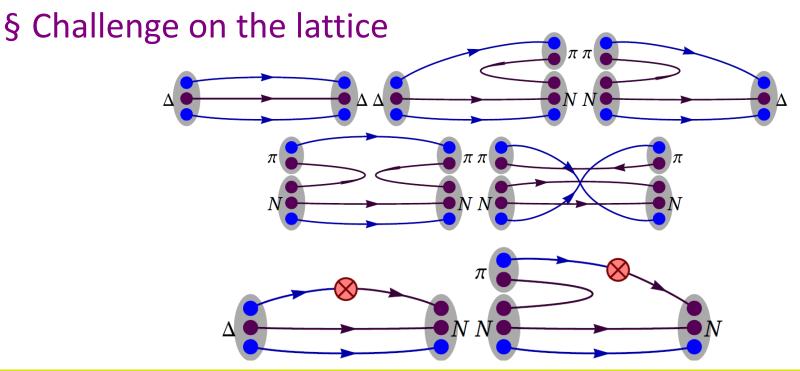
§ Challenge: Resonances and multiple-particle final states

- Neutrino scattering above the pion-production threshold, where the scattered nucleon is excited into resonances
- *∞* Inputs: need knowledge on $N \to \Delta$ and $N \to N^*$
- $\gg N\Delta$ axial form factors C_{3-6}^A in the transition axial current are



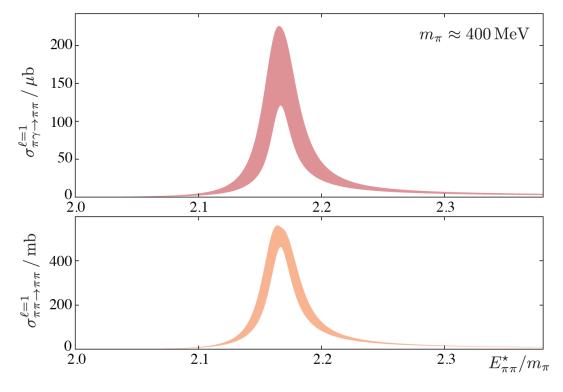
§ Challenge: Resonances and multiple-particle final states

- Neutrino scattering above the pion-production threshold, where the scattered nucleon is excited into resonances
- *∞* Inputs: need knowledge on $N \to \Delta$ and $N \to N^*$





§ Challenge: Resonances and multiple-particle final states
 Simpler cases show promising results from lattice



R. Briceno et al, Phys. Rev. D92, 074509 (2015)

