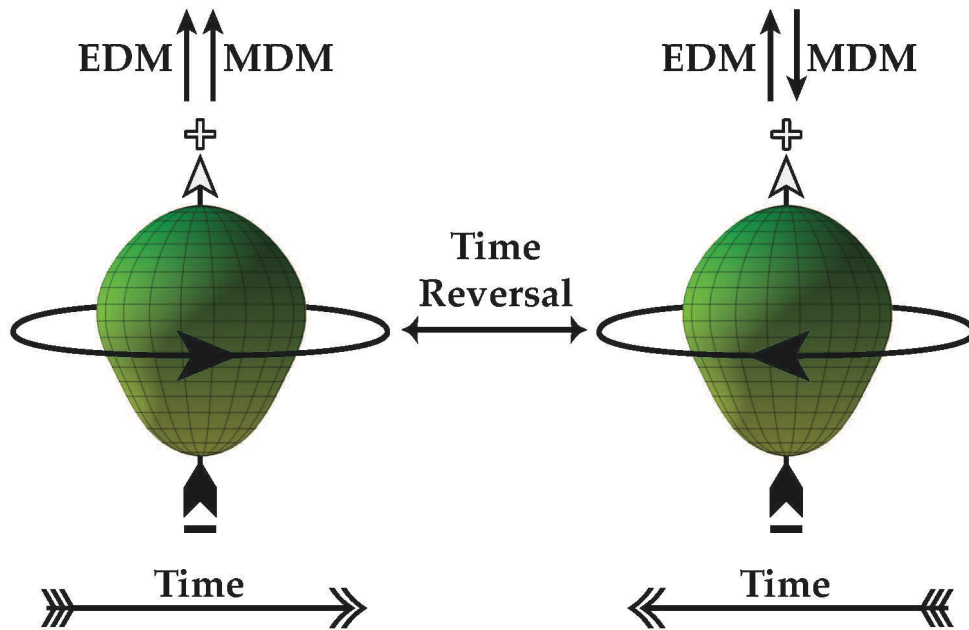


Electric Dipole Moment (1/2)

Today: Motivation & Background, The Atomic Ra EDM Experiment

*Tomorrow: "Atomic" Parity Violation, Neutrons & Nuclei,
& Radioactive Molecules*



Carolyn
Beatrice
Parker

M.S. Physics MIT
1917-66

Jaideep Taggart Singh (he/him/his)

Michigan State University / FRIB

National Nuclear Physics Summer School 2024

Monday July 22, 2024 @ 14:00

Indiana University Bloomington

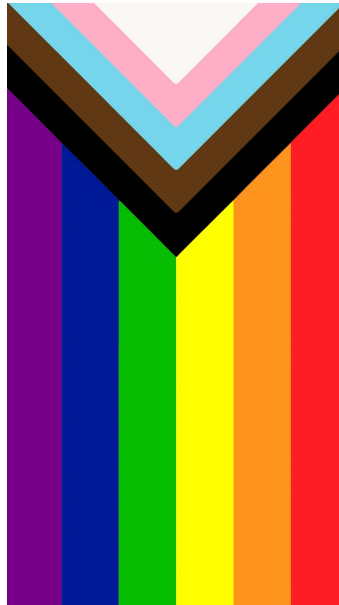
Swain Hall West 007 (Basement)



SCAN ME

Introductions

- Theory
- Experiment
- Accelerator Physics
- Computational Physics
- Hadronic Physics
- Nuclear Structure
- Nuclear Astrophysics
- Fundamental Symmetries
- Neutrons
- Neutrinos
- Radiochemistry
- Other



<https://www.them.us/story/pride-flag-redesign>

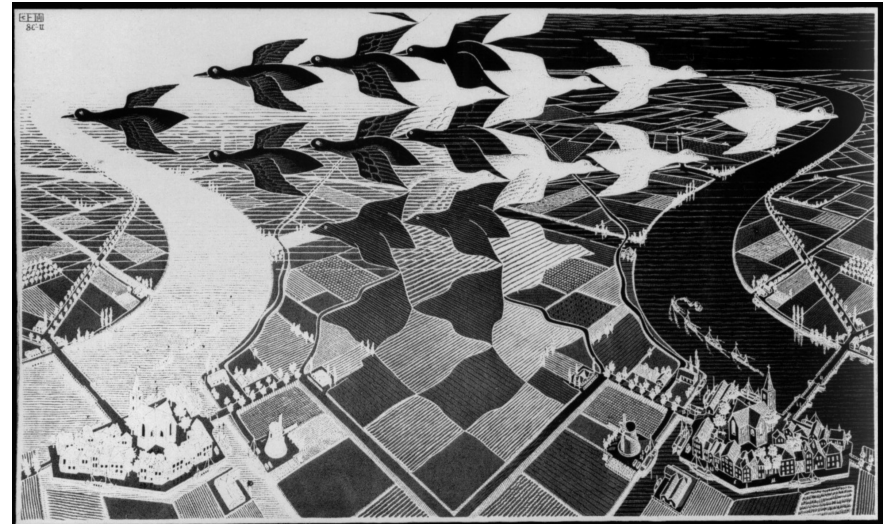
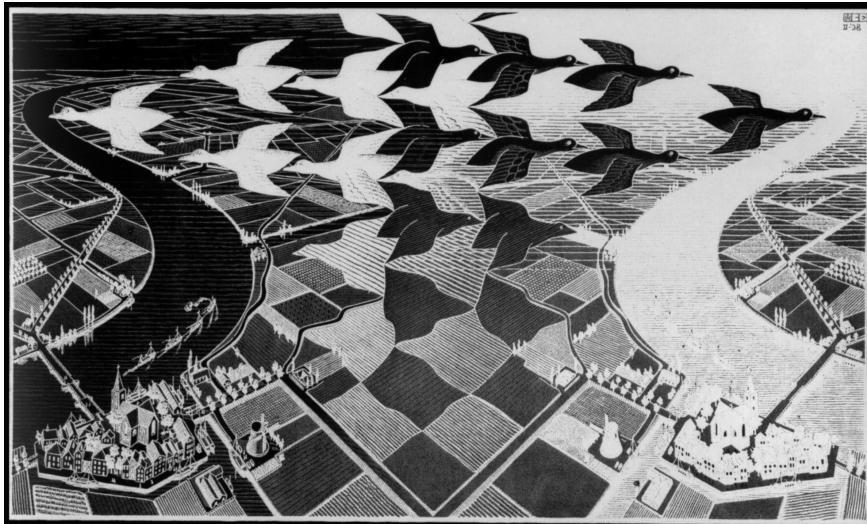
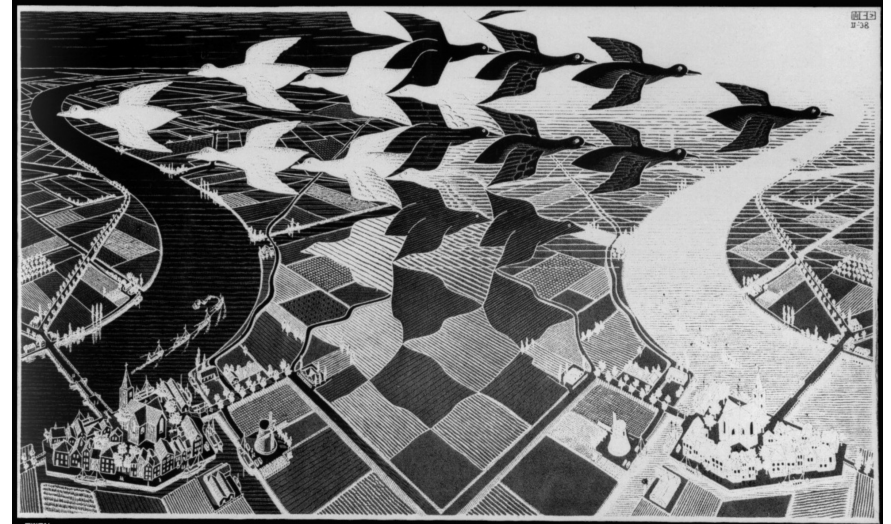
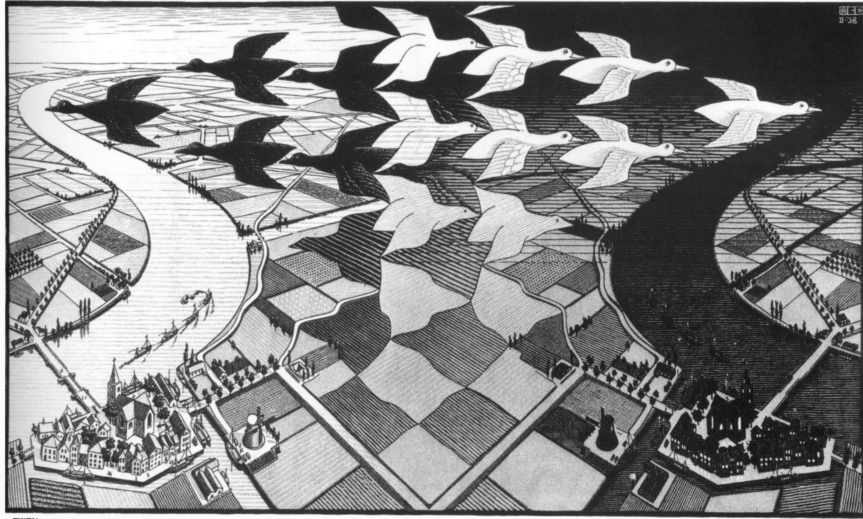
**Benny (7 years old, they/them)
@ DNP Hawaii 2023**

My Dad: Condensed Matter Theory (Pittsburgh) – [Hindi Movies & Songs](#)

My Wife: Artist from West Des Moines, Iowa

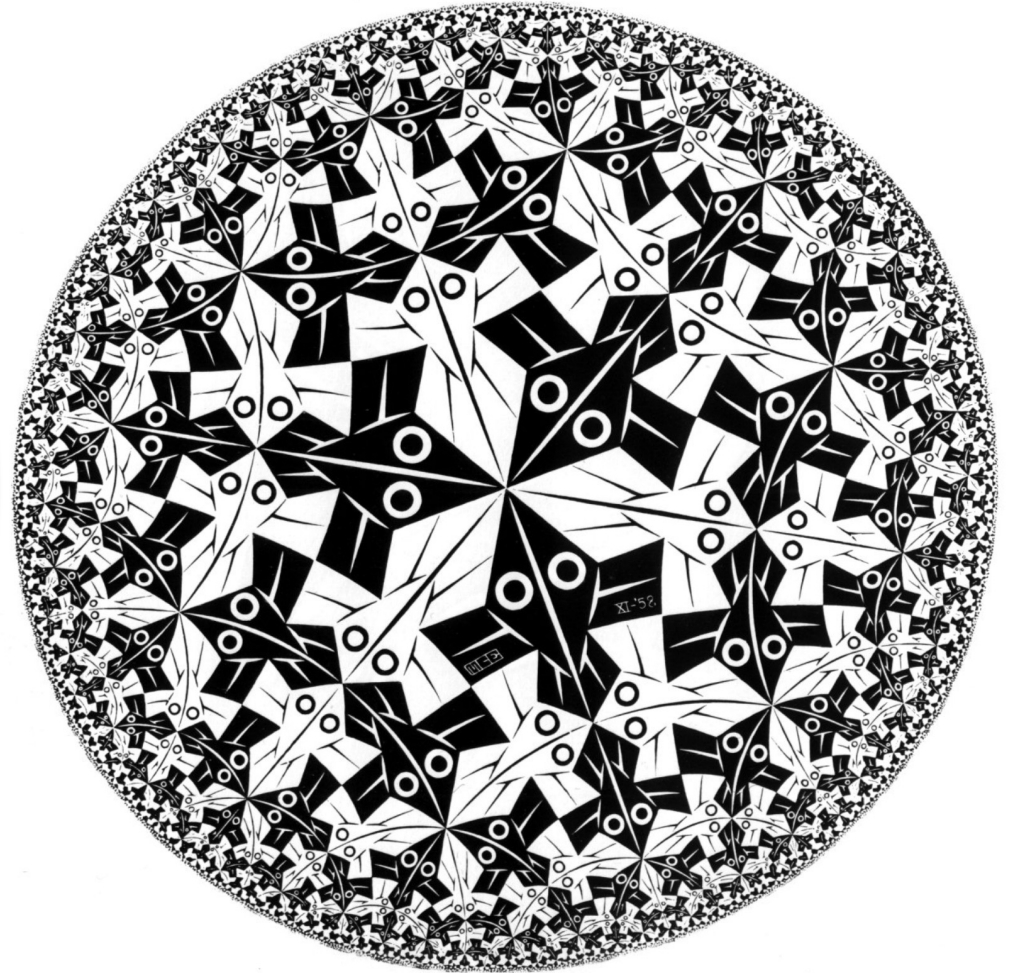
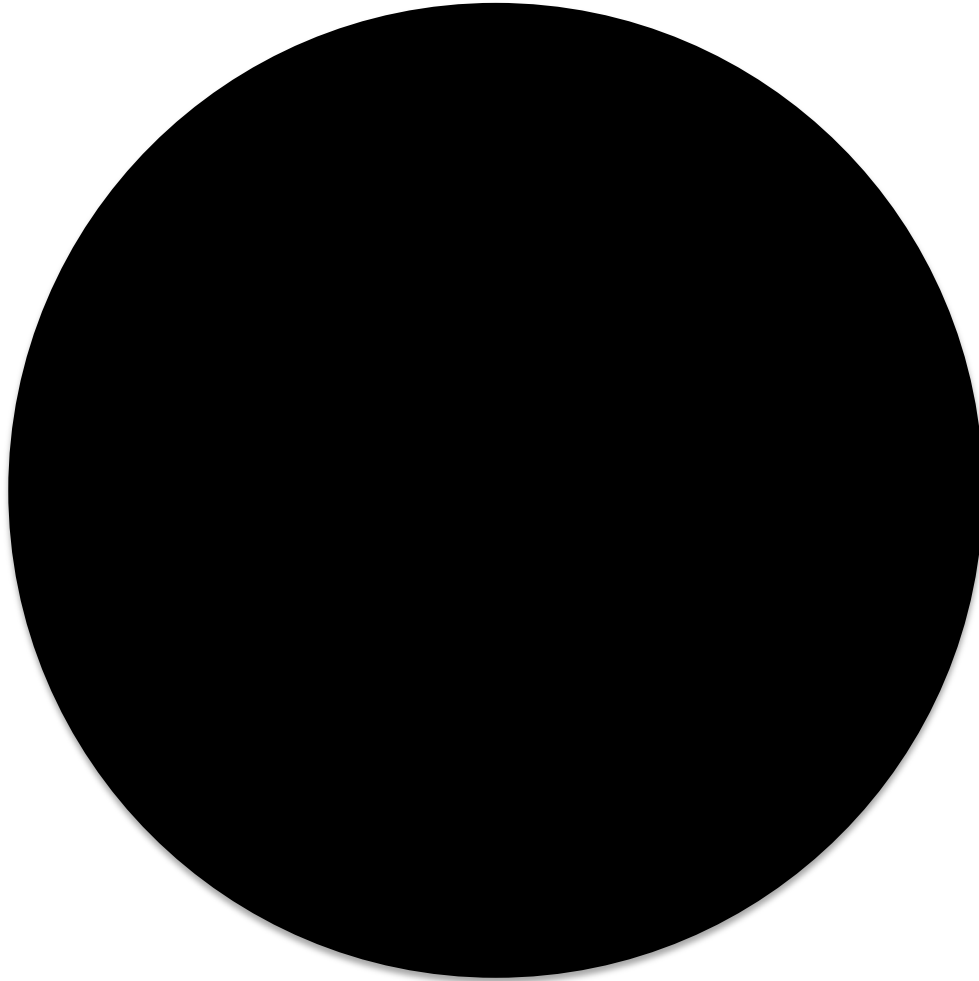
Me: New Delhi, India – Waterloo, Ontario, Canada – Lubbock, Texas –
Pasadena, California – San Diego, California – Charlottesville, Virginia – JLab –
Chicago, Illinois – Argonne National Lab – Garching/Munich, Germany –
East Lansing, Michigan – National Superconducting Cyclotron Lab –
Michigan State University – Facility for Rare Isotope Beams

Transformations and Symmetry: “Day and Night” by M.C. Escher (1938)



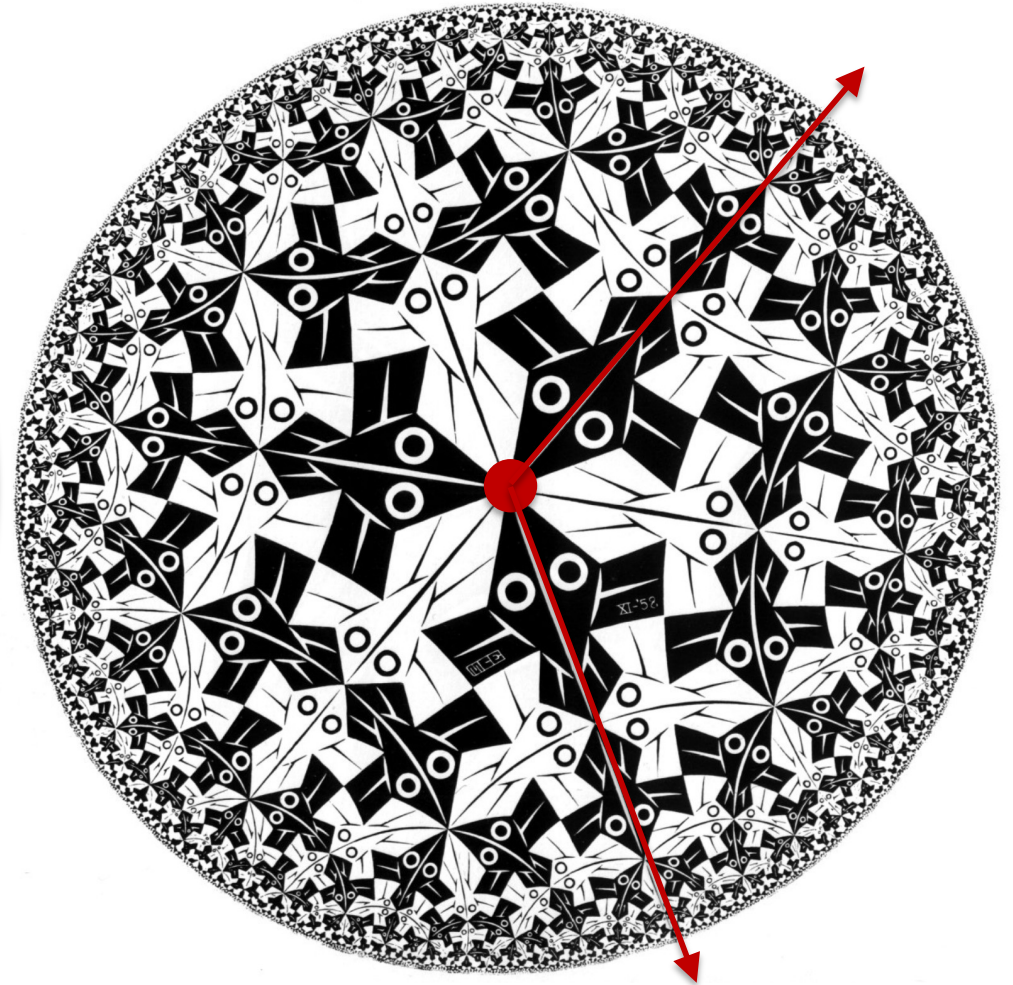
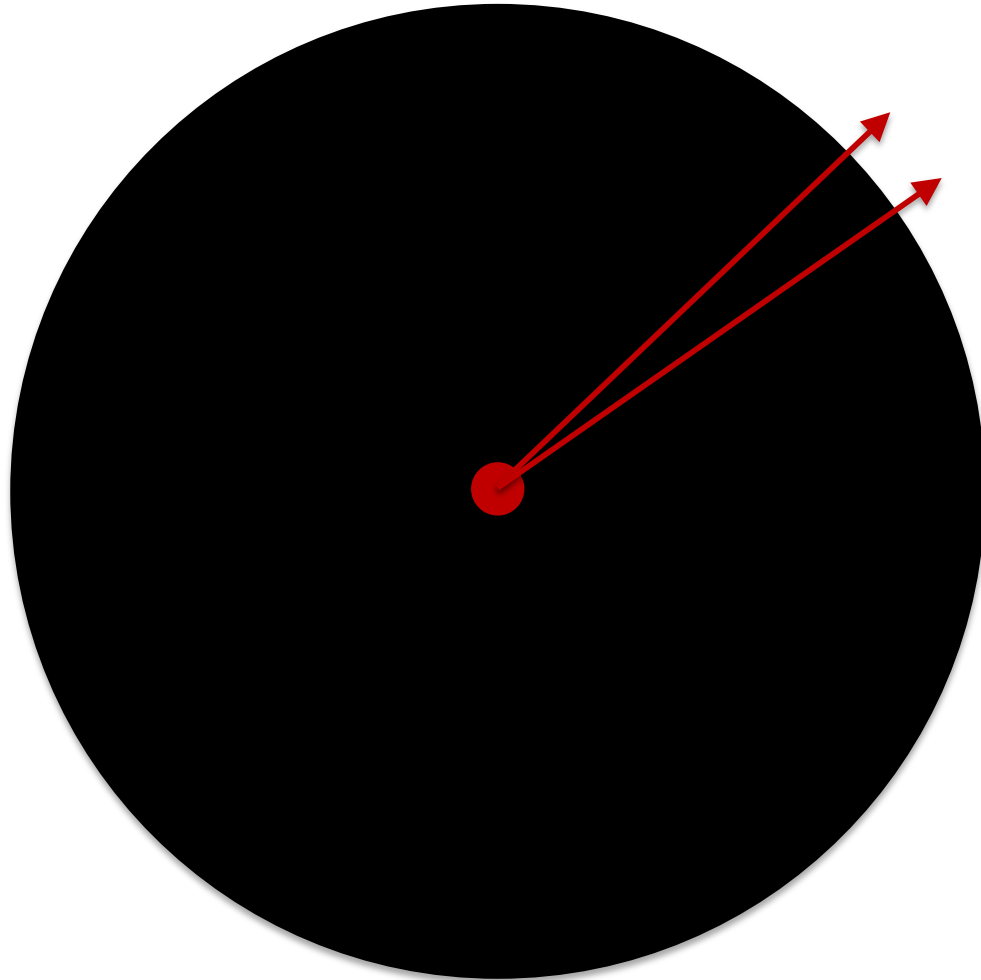
<https://www.wikiart.org/en/m-c-escher/day-and-night>

Continuous vs. Discrete Symmetries: “Circle Limit I” by M.C. Escher (1958)



<https://www.wikiart.org/en/m-c-escher/circle-limit-i>

Continuous vs. Discrete Symmetries: “Circle Limit I” by M.C. Escher (1958)



<https://www.wikiart.org/en/m-c-escher/circle-limit-i>

Noether's Theorem (1918) (Only For Continuous Symmetries)



The presence of a continuous symmetry implies the existence of a conserved quantity.

Symmetry under temporal translations

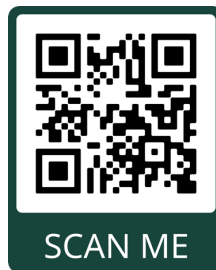
➤ conservation of energy

Symmetry under spatial translations

➤ conservation of linear momentum

Symmetry under rotations

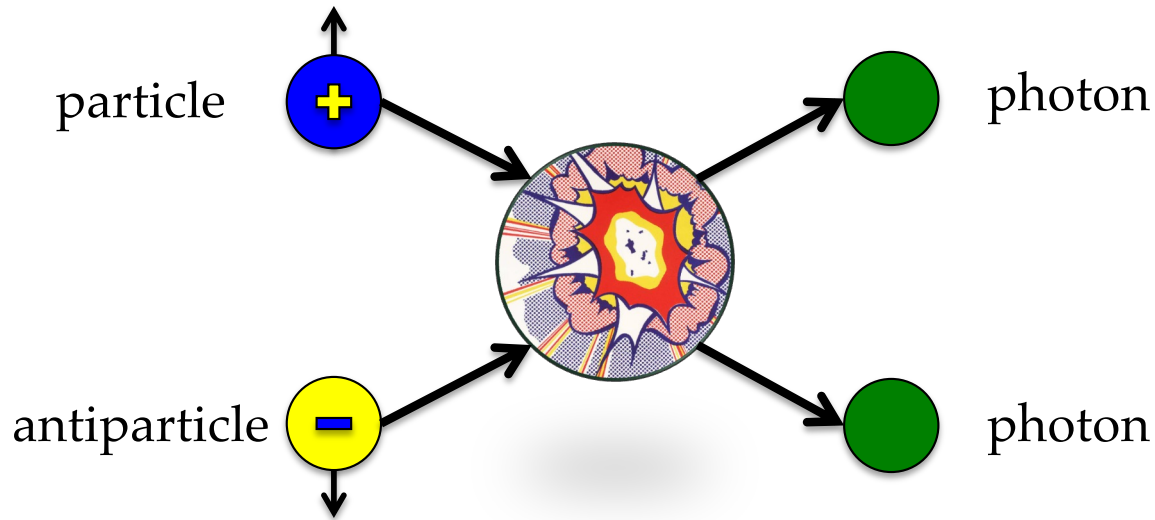
➤ conservation of angular momentum



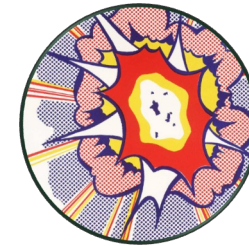
**Emmy Noether:
My All-Time Favorite Theorist!**

https://en.wikipedia.org/wiki/Emmy_Noether

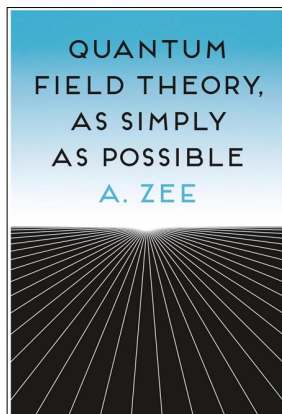
Quantum Field Theory Provides The Mathematical Apparatus Used To Calculate The Interaction Probability



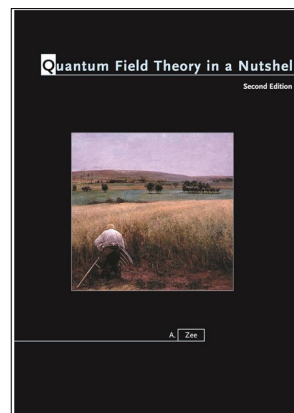
“Explosion” by
Roy Lichtenstein (1965-6)



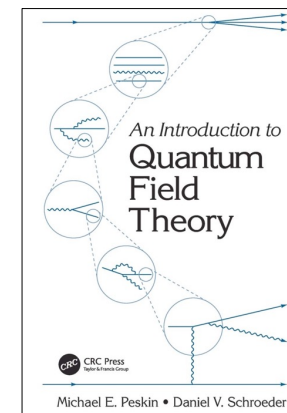
An infinite sum of
multidimensional integrals



Anthony Zee (2023)
For The Curious



Anthony Zee (2010)
For Self-Study

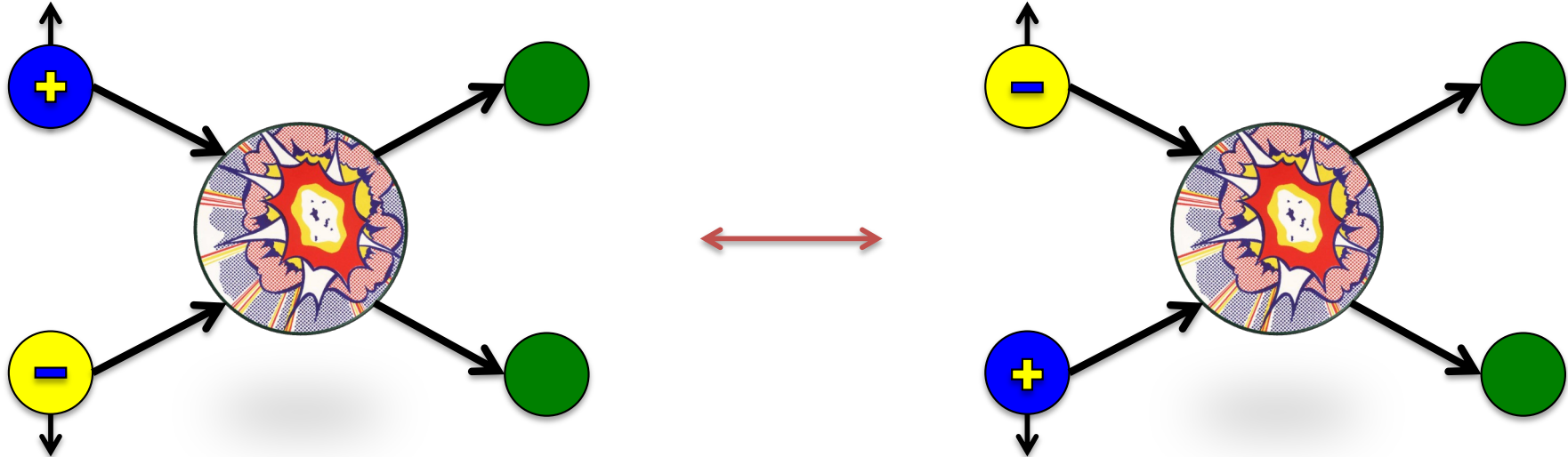


Peskin & Schroeder (1995)
For QFT Practitioners

Discrete Symmetry Transformation

C: Charge Conjugation

Replace particle with antiparticle



<https://www.tate.org.uk/kids/explore/who-is/who-roy-lichtenstein>

2024-07-22

NNPSS 2024 - EDM 1/2

8

Discrete Symmetry Transformation

P: Parity (Spatial Inversion)

Mirror reflection

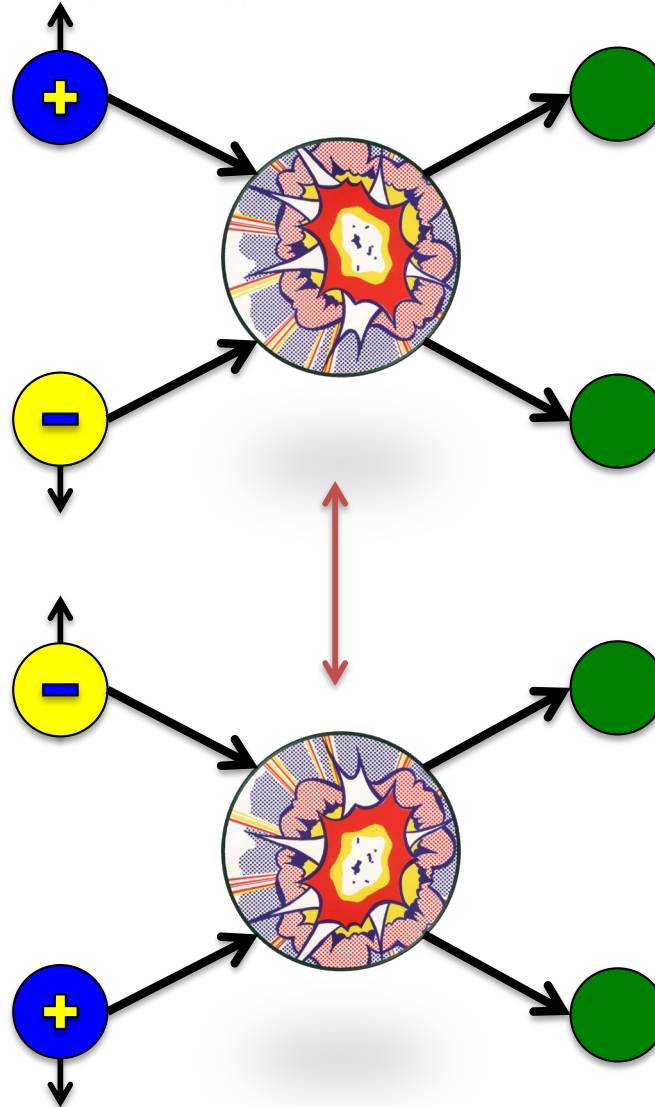
+

180° rotation

+x to -x

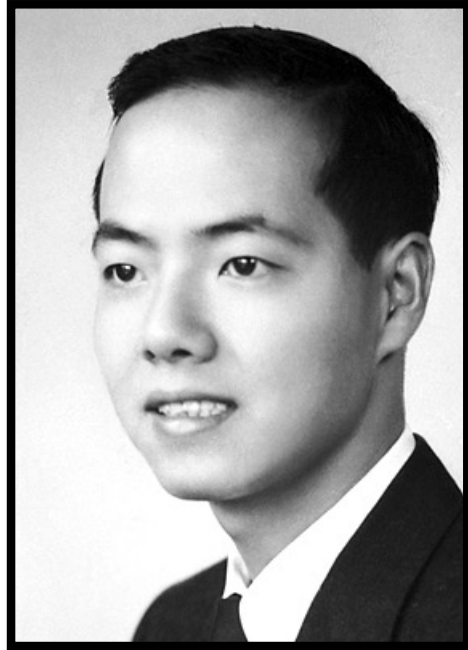
+y to -y

+z to -z

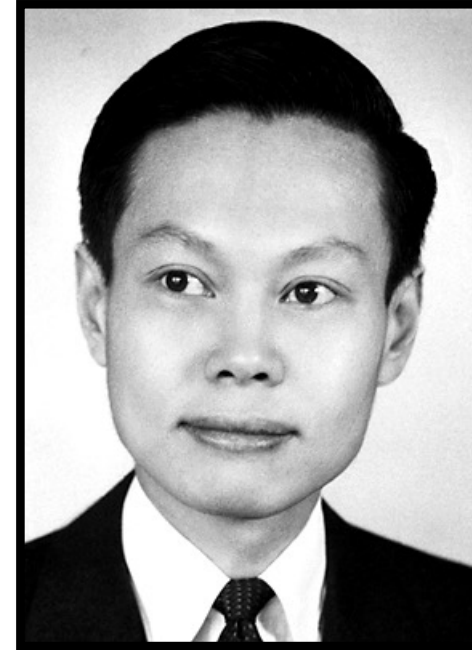


<https://www.tate.org.uk/kids/explore/who-is/who-roy-lichtenstein>

1956: Is Parity Conserved?



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The Nobel Foundation

PHYSICAL REVIEW

VOLUME 104, NUMBER 1

OCTOBER 1, 1956

Question of Parity Conservation in Weak Interactions*

T. D. LEE, *Columbia University, New York, New York*

AND

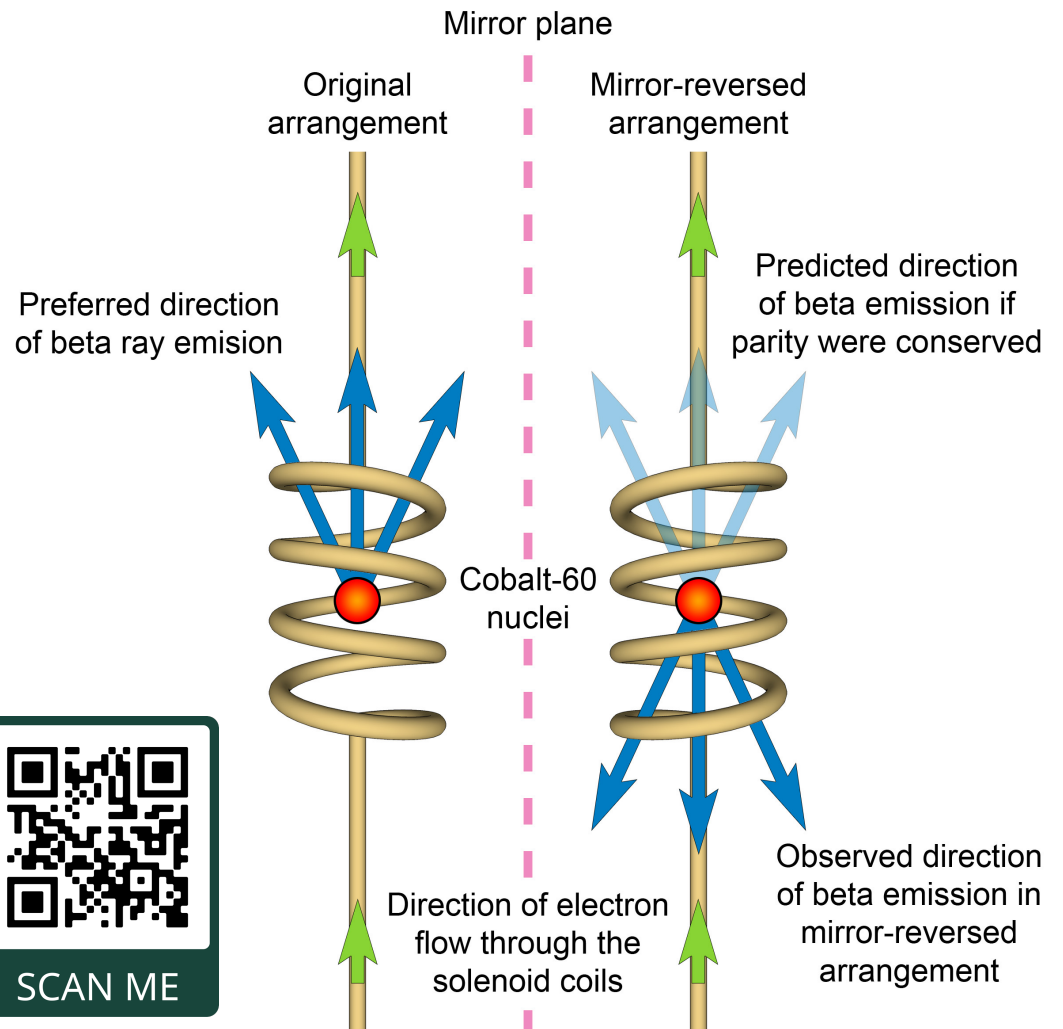
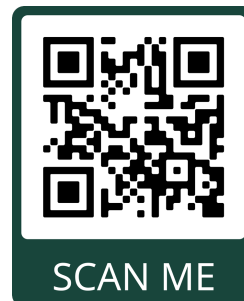
C. N. YANG, † *Brookhaven National Laboratory, Upton, New York*

(Received June 22, 1956)

The question of parity conservation in β decays and in hyperon and meson decays is examined. Possible experiments are suggested which might test parity conservation in these interactions.

1957: Nope, Parity is Violated (Maximally)!

AIP Emilio Segre Visual Archives



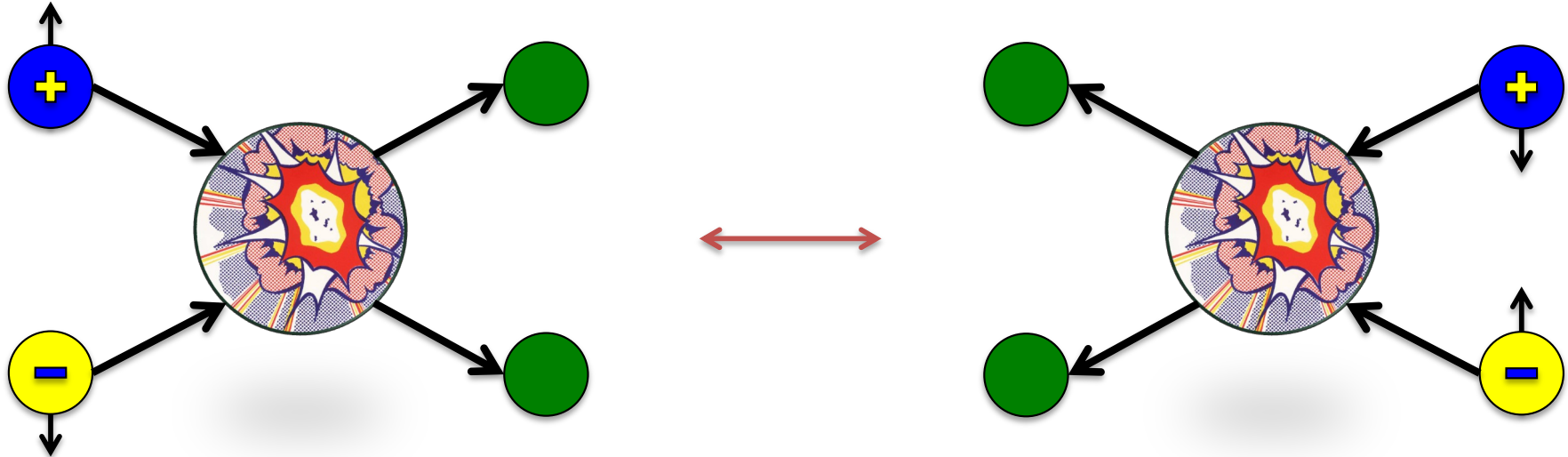
C.S. Wu: My All-Time Favorite Science Super-Hero!

http://en.wikipedia.org/wiki/File:Wu_experiment.jpg

Discrete Symmetry Transformation

T : Time-Reversal

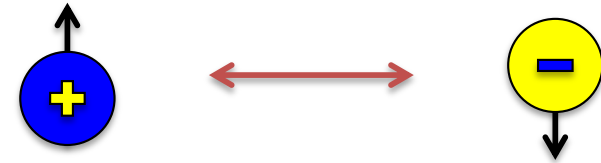
Reverse the arrow of time: $+t$ to $-t$



Special Combinations of Discrete Symmetry Transformations

CP-transformation

replace a “right-handed” particle with its “left-handed” antiparticle counterpart



CPT-transformation

replace a “right-handed” particle with its “left-handed” antiparticle counterpart moving in the opposite direction

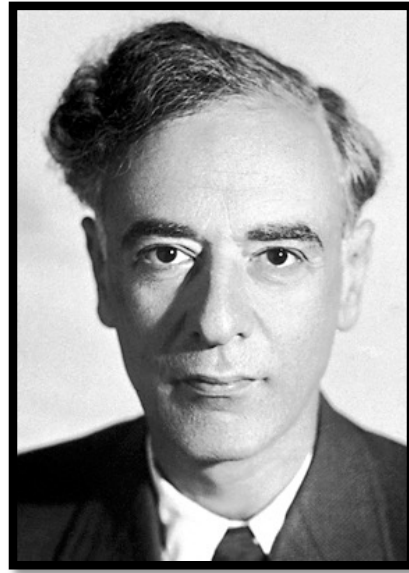
The CPT Theorem (Taylor’s Version):

The quantum interaction probability remains the same after a CPT-transformation if the underlying theory is consistent with special relativity.



https://en.wikipedia.org/wiki/Shake_It_Off#Lawsuits

1957: Is CP Conserved?



The Nobel Foundation

ON THE CONSERVATION LAWS FOR WEAK INTERACTIONS

L. LANDAU

Institute for Physical Problems, USSR Academy of Sciences, Moscow

Received 9 January 1957

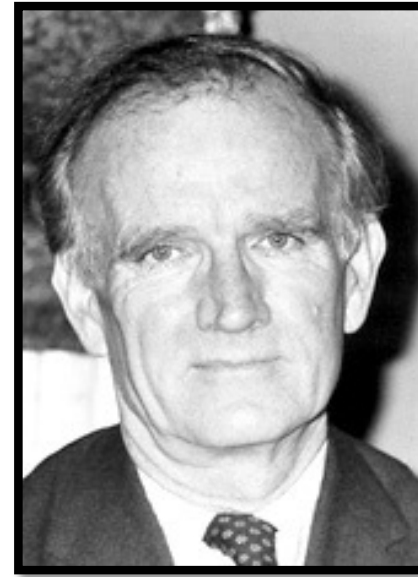
Abstract: A variant of the theory is proposed in which non-conservation of parity can be introduced without assuming asymmetry of space with respect to inversion.

Nuclear Physics 3 (1957) 127-131

1964: Nope, CP is Violated (Just a Little Bit)!



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VOLUME 13, NUMBER 4

PHYSICAL REVIEW LETTERS

27 JULY 1964

EVIDENCE FOR THE 2π DECAY OF THE K_2^0 MESON*†

J. H. Christenson, J. W. Cronin,‡ V. L. Fitch,‡ and R. Turlay§

Princeton University, Princeton, New Jersey

(Received 10 July 1964)

Does The Quantum Interaction Probability Remain The Same Under A Discrete Symmetry Transformation?

	Strong Interaction	Weak Interaction	Electricity + Magnetism	Gravity	New Physics
<i>C</i>	Yup, so far	No, never	Yup, so far	Yup, so far	depends
<i>P</i>	Yup, so far	No, never	Yup, so far	Yup, so far	depends
<i>T & CP</i>	Yup, so far, (but we are ready for no: θ_{QCD} parameter)	Yes, most of the time, but... <i>occasionally</i> not when dealing with quarks (CKM matrix) and maybe also neutrinos (PMNS matrix)	Yup, so far	Yup, so far	depends
<i>CPT</i>	Yup, so far	Yup, so far	Yup, so far	Yup, so far	depends

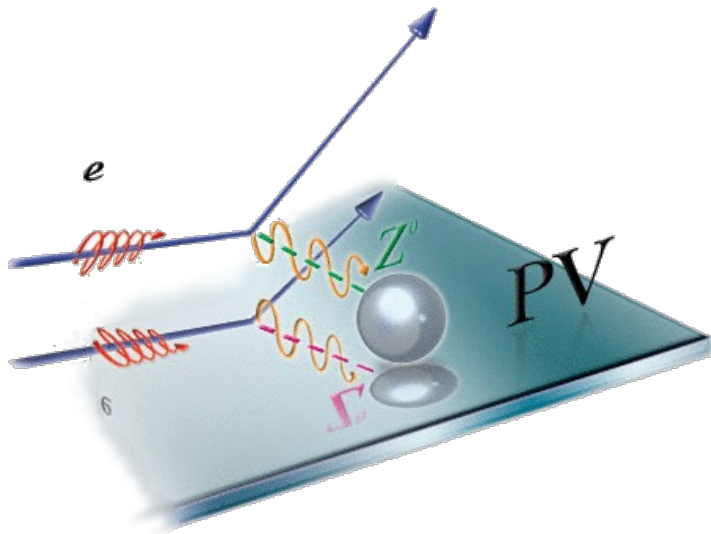
If the quantum interaction probability is not the same under a discrete symmetry transformation, then we say that discrete symmetry transformation is “violated.”

If the quantum interaction probability stays the same under *CPT*-transformations:

- then *T*-violation implies *CP*-violation and vice versa
- then *P*-violation implies *C*-violation or *T*-violation

Testing “Fundamental Symmetries” (Discrete Symmetry Transformations) Provides Access to “New Physics”

Fundamental Symmetries (E. Mereghetti)



Asymmetries in scattering and reaction rates (C. Palatchi)

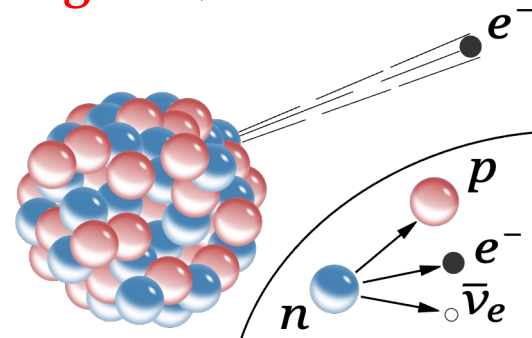
<https://hallaweb.jlab.org/parity/prex/prextalks.html>

https://en.wikipedia.org/wiki/Beta_decay

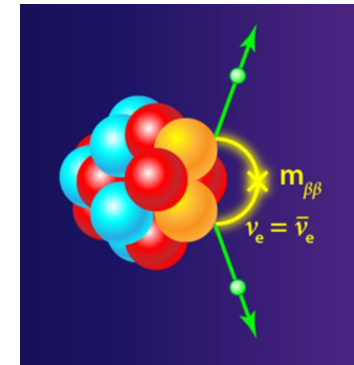
<https://physics.aps.org/articles/v11/30>

<https://www.eurekalert.org/multimedia/925121>

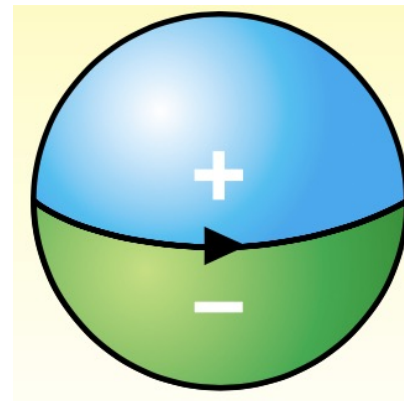
Physics Today, June 2003



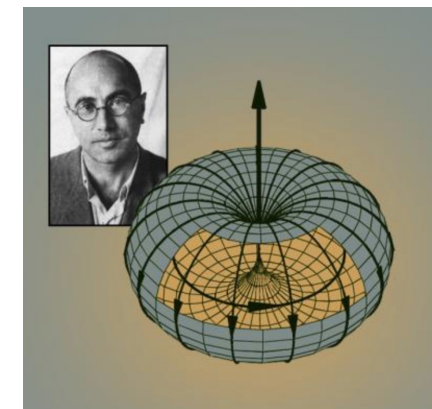
Nuclear Beta Decay (B. Jones & A. Holley)



Neutrinoless Double Beta Decay (B. Jones)



Electric Dipole Moments (JTS)



Nuclear Anapole Moments (JTS)

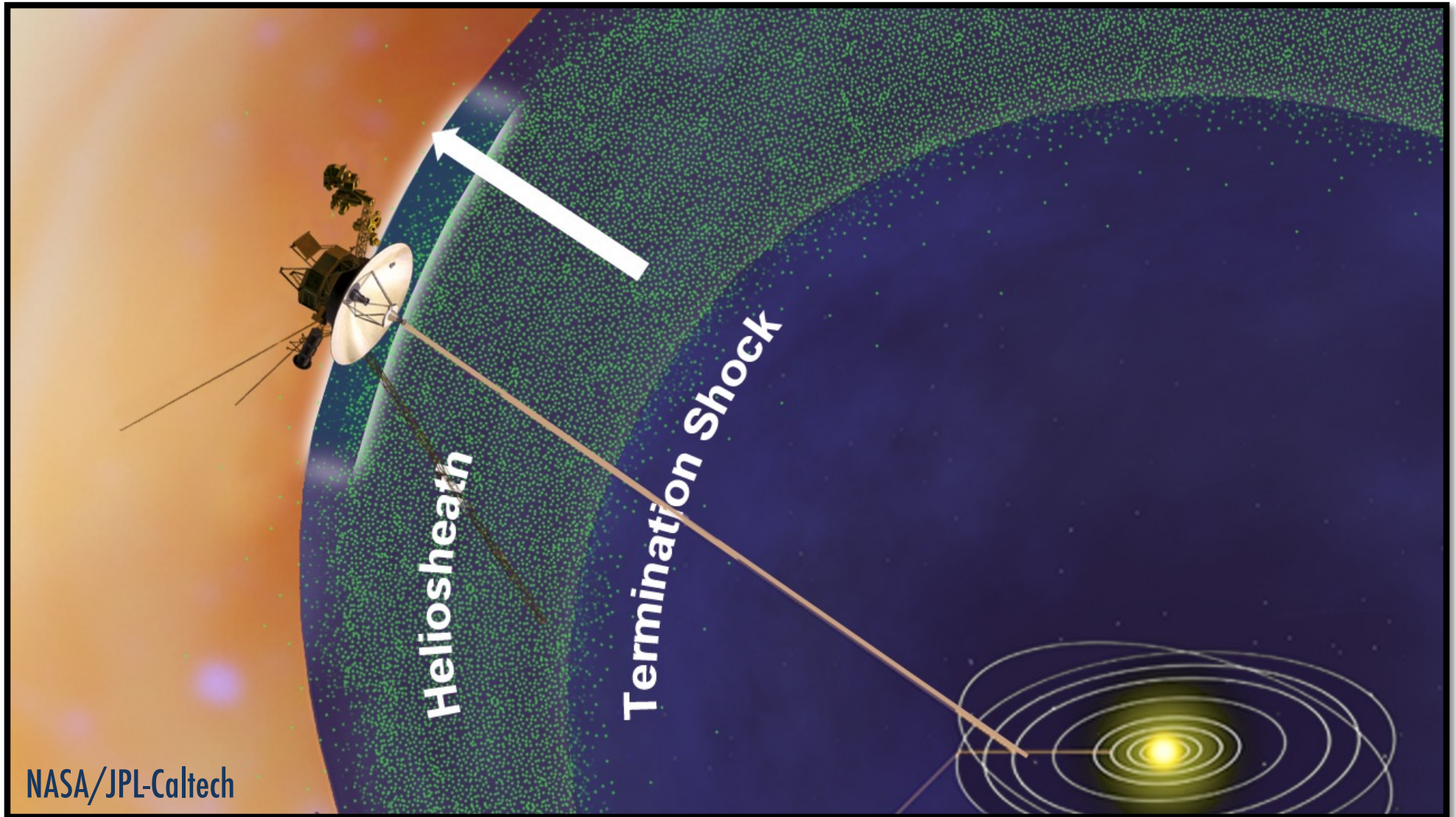
Intermission

Questions?

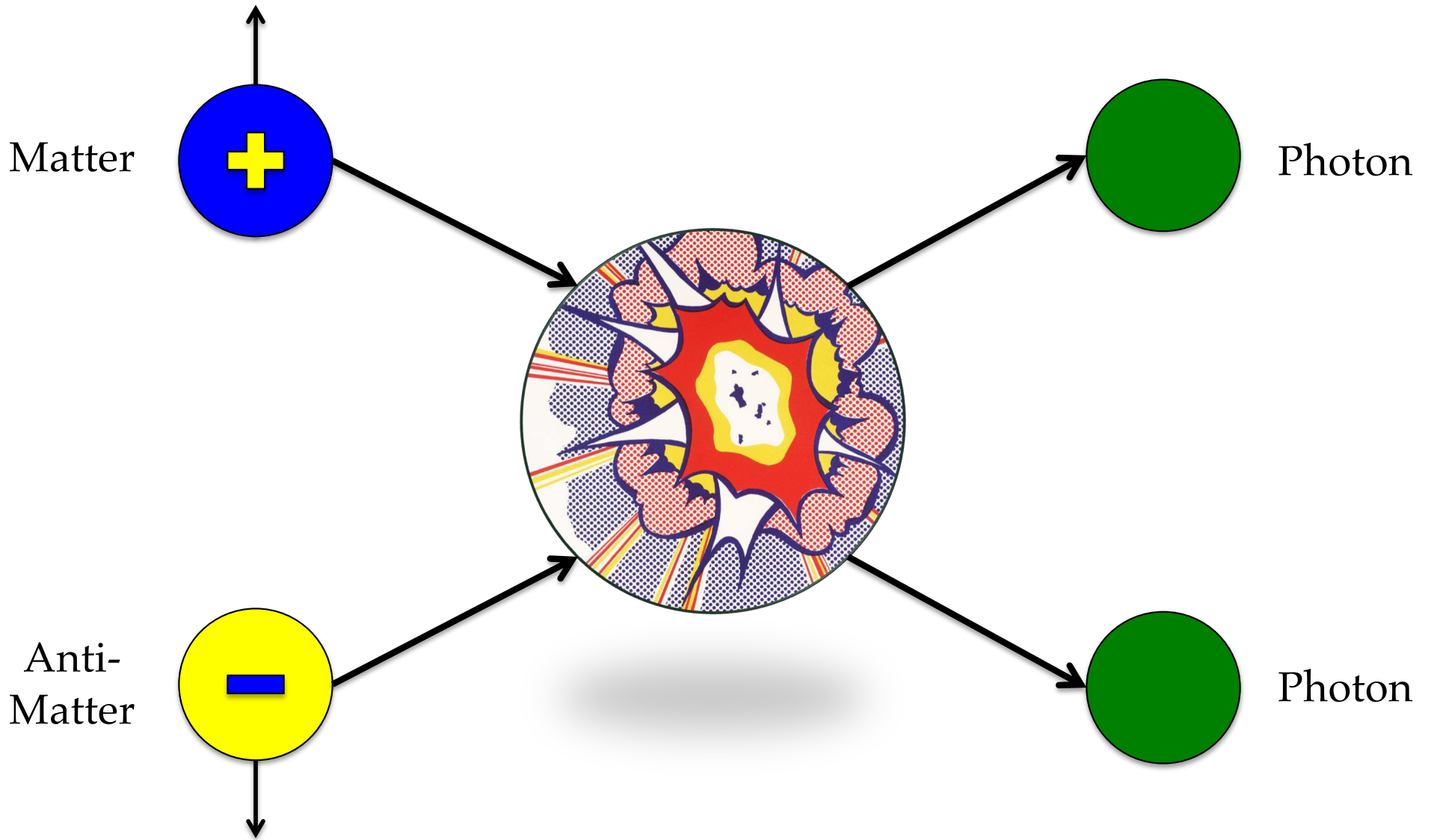
1. stuff

Voyager 1 is Still OK!

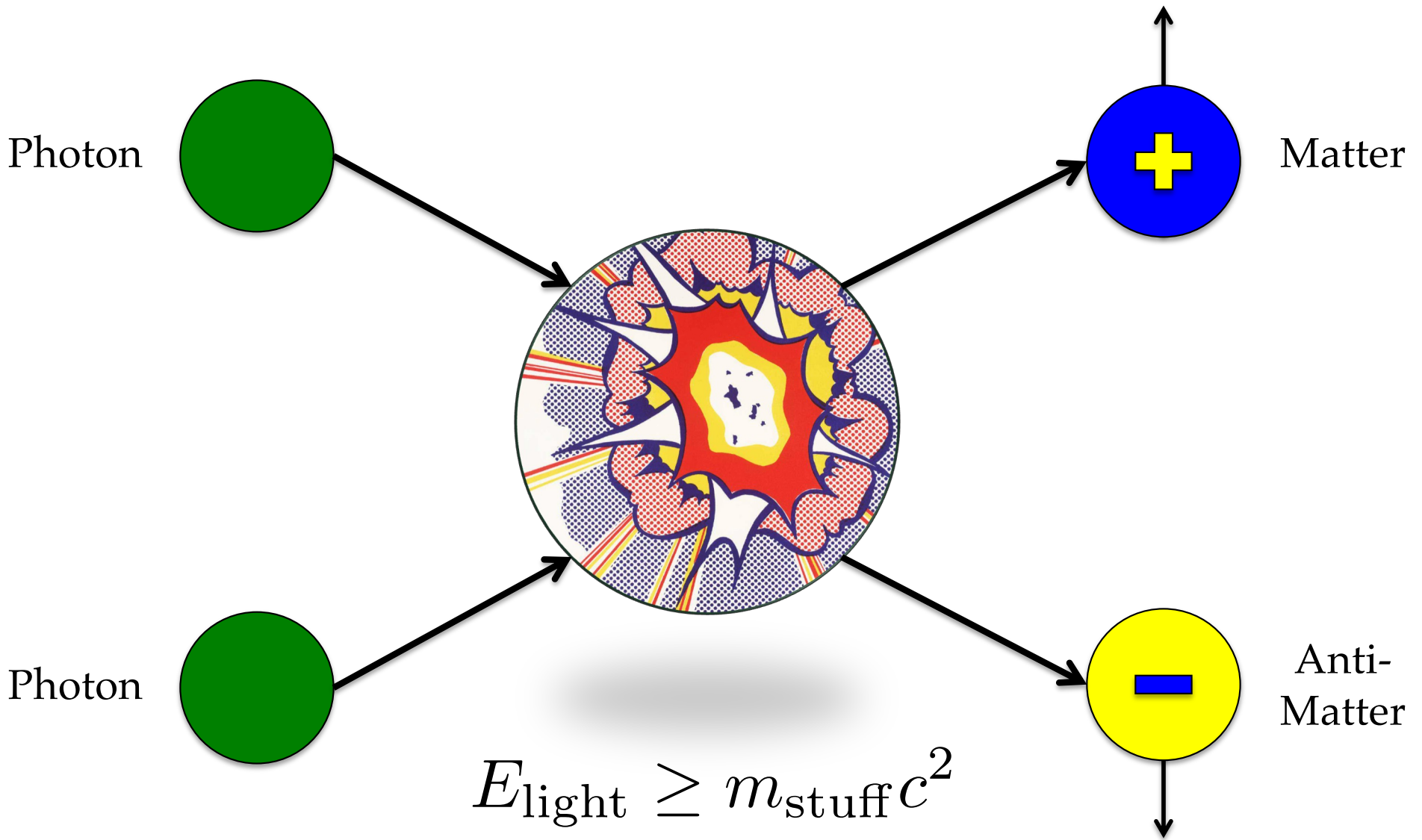
for the rest of the Universe: Annual Review of Astronomy and Astrophysics 14:339-372 (1976)



Matter & Antimatter Annihilate Into Photons

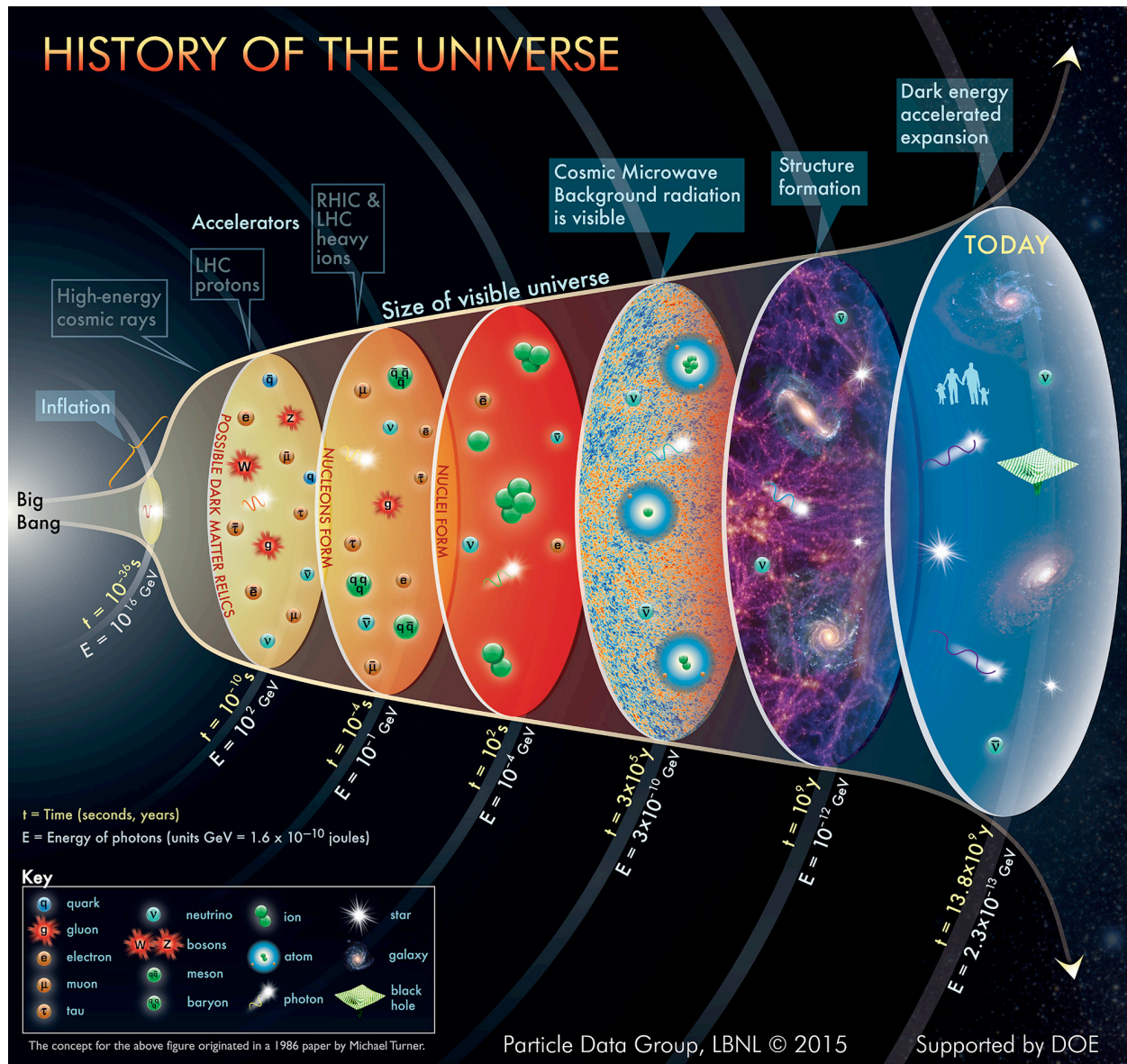


Photons Annihilate Matter & Antimatter



Big Bang...Expanding Universe

**HOT &
DENSE**

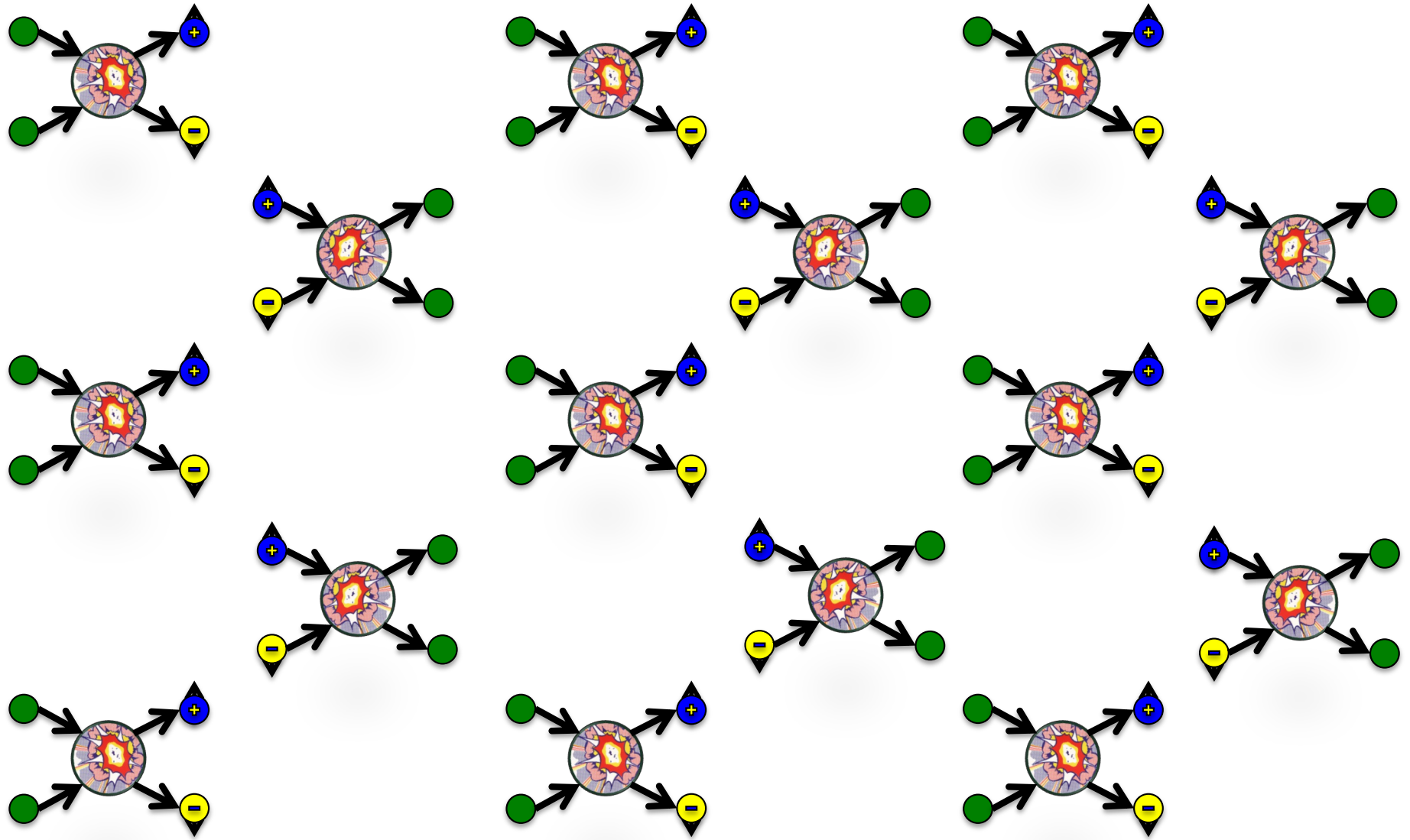


**cold &
dilute**

Everything Everywhere All At Once!

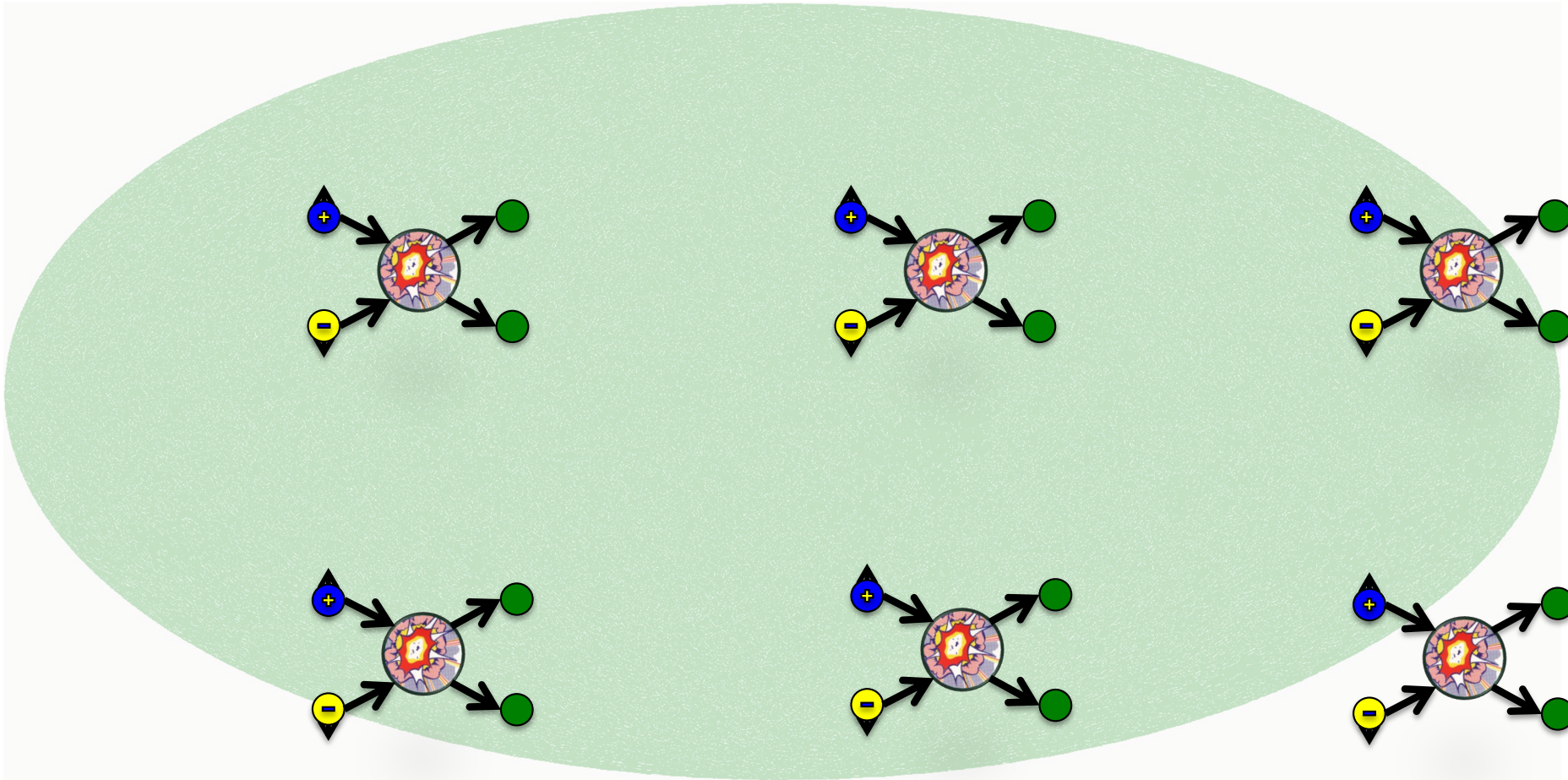


<https://www.bbc.com/news/entertainment-arts-64938320>



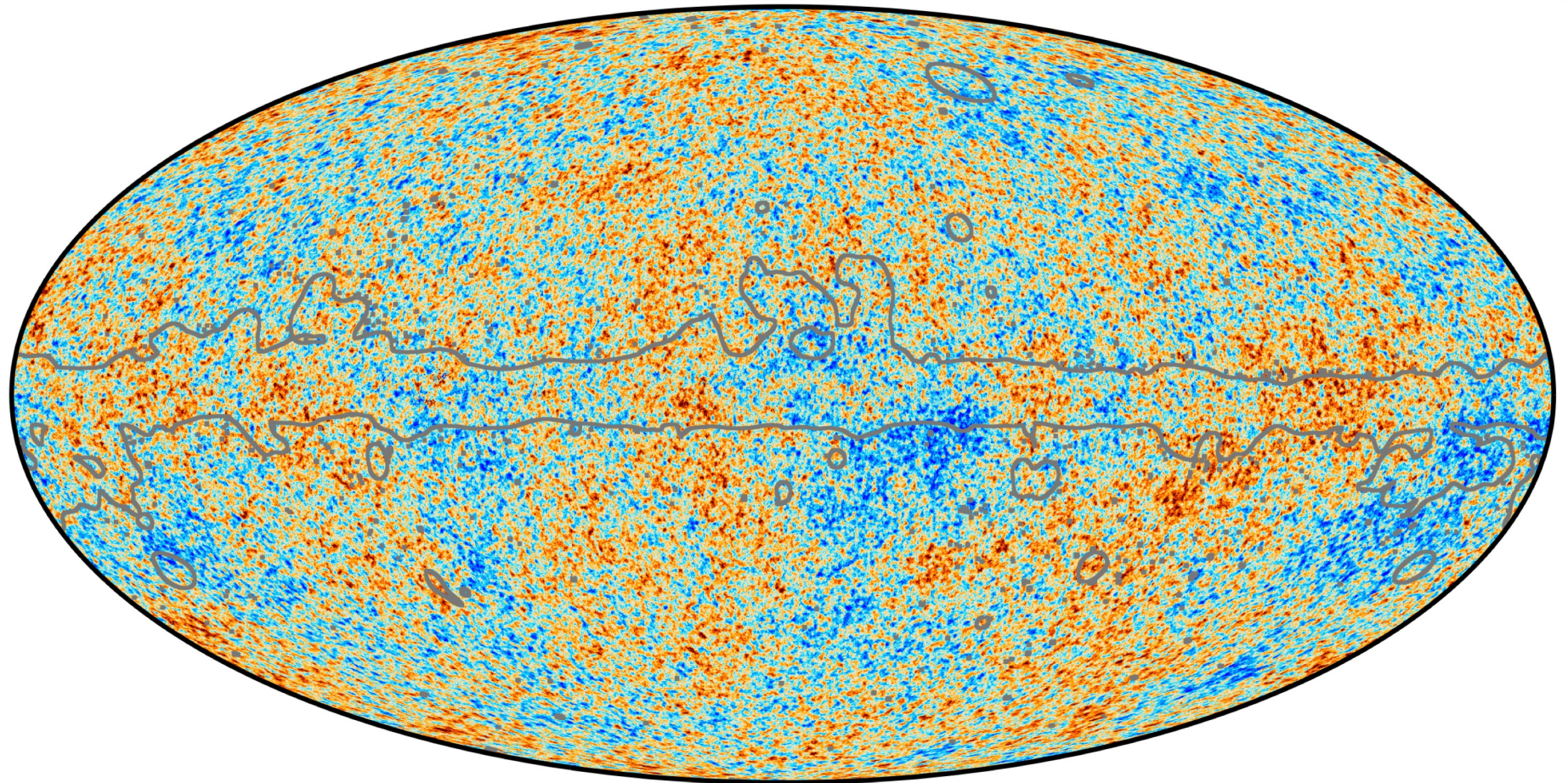
<https://www.tate.org.uk/kids/explore/who-is/who-roy-lichtenstein>

Expansion Means Cooling: 2.73 K Everywhere



Cosmic Microwave Background Anisotropy

“Baby Picture” of the Universe



-300



300 μK

~ 100 ppm
fluctuations

<https://www.cosmos.esa.int/web/planck/picture-gallery>

Planck 2018

2024-07-22

NNPSS 2024 - EDM 1 / 2

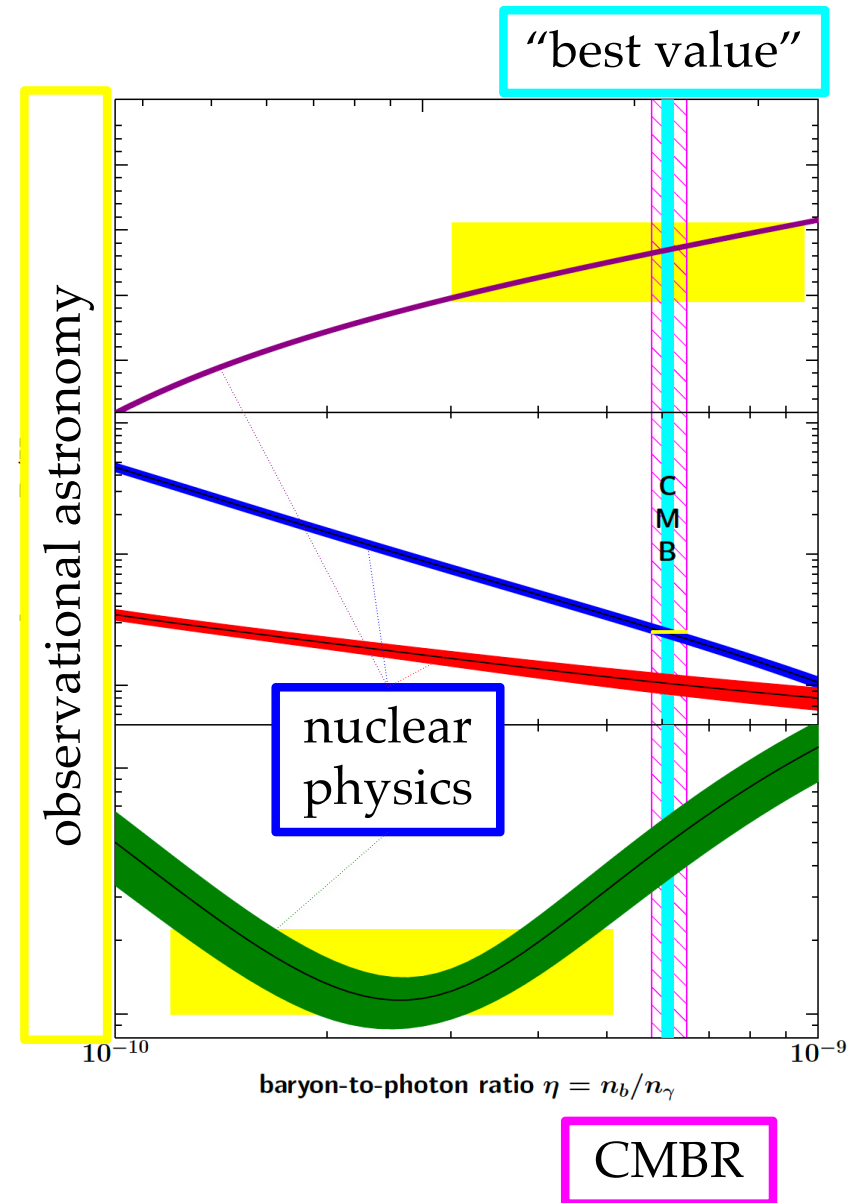
25

There Is No Visible Antimatter In The Universe

$$\eta \text{ " = " } \frac{(\text{matter}) - (\text{antimatter})}{\text{relic photons}}$$

$$\eta = 0.0000000006129 \text{ (0.6\%)} \quad \text{PDG2022}$$

$$\approx 10^{-9}$$



Sakharov's Conditions: Need CP -Violation



VIOLATION OF CP INVARIANCE, C ASYMMETRY, AND BARYON ASYMMETRY OF THE UNIVERSE

A. D. Sakharov

Submitted 23 September 1966

ZhETF Pis'ma 5, No. 1, 32-35, 1 January 1967

The theory of the expanding Universe, which presupposes a superdense initial state of matter, apparently excludes the possibility of macroscopic separation of matter from anti-matter; it must therefore be assumed that there are no antimatter bodies in nature, i.e., the Universe is asymmetrical with respect to the number of particles and antiparticles (C asymmetry). In particular, the absence of antibaryons and the proposed absence of baryonic neutrinos implies a non-zero baryon charge (baryonic asymmetry). We wish to point out a possible explanation of C asymmetry in the hot model of the expanding Universe (see [1]) by making use of effects of CP invariance violation (see [2]). To explain baryon asymmetry, we propose in addition an approximate character for the baryon conservation law.

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1. A baryon number violating interaction exists.
2. Departure from thermal equilibrium.
3. *Both C- & CP-symmetry must be violated.*

CKM Matrix: Weak Interaction for Quarks



http://en.wikipedia.org/wiki/File:Nicola_Cabibbo.jpg

C



The Nobel Foundation

K



The Nobel Foundation

M

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$\delta = CP$ -violating “phase”

Standard Model CP -Violation: Not Enough

$$\eta = \frac{(\text{matter}) - (\text{antimatter})}{\text{relic photons}} \propto \sin(\delta)$$

$$\eta_{\text{exp}} \approx 10^{-9} \quad \text{PDG2022}$$

$$\eta_{\text{CKM}} \approx 10^{-26} \quad \text{Huet \& Sather PRD 51:379 (1995)}$$

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$\delta = CP$ -violating “phase”

New Massive Particles = More Phases

$$\text{number of phases} = (N_g - 1)(N_g - 2) / 2$$

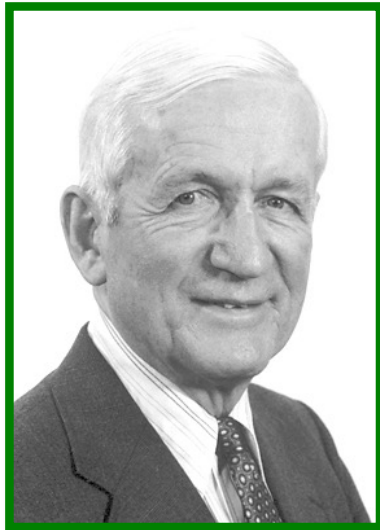
$$\text{number of generations} = N_g \quad \text{Hocker \& Ligeti, Annu. Rev. Nucl. Part. Sci. 2006. 56:501-67}$$

This is generically why “New Physics” can produce more CP -violation!

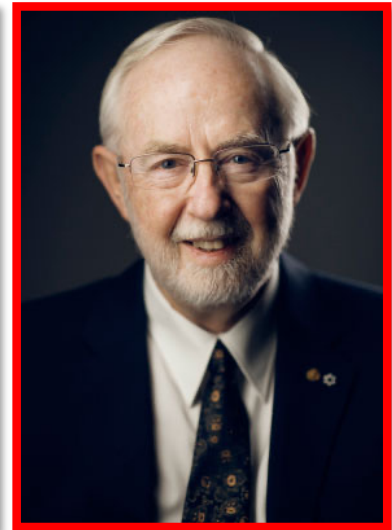
$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$\delta = CP$ -violating “phase”

Where Do We Look For More CP -Violation?



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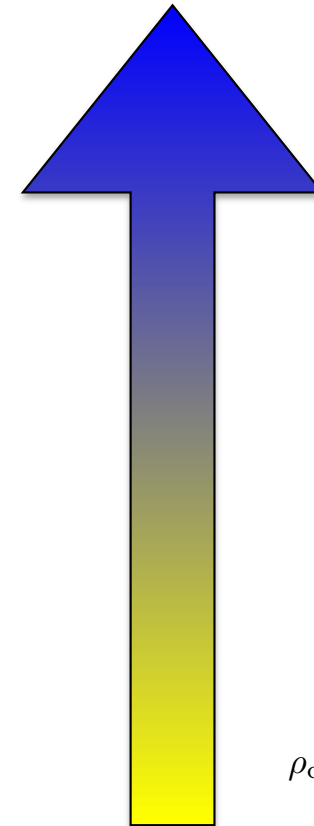


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- Decays of B -mesons [Belle II]
- Rare decays of b -hadrons [LHCb]
- Angular decay correlations of positronium [Wittenberg/MSU]
- D -coefficient in nuclear beta-decay [The MORA Project]
- Nuclear magnetic quadrupole moments [Caltech, UNLV, ODU]
- Double polarized neutron transmission [**NOPTREX – Mike Snow @ Indiana**]
- **Neutrinos have mass! (PMNS matrix) [neutrino oscillations + $0\nu 2\beta$: B. Jones]**
- ***electric dipole moments: If CPT is good, then T -violation can be used to search for new sources of CP -violation!***

Electric Dipole Moment (EDM): Measures the Separation of Charges

$$\vec{d} = \int \rho_{\text{charge}} \left(\vec{r} - \vec{R}_{\text{CM}} \right) d^3r = \langle \rho_{\text{charge}} \vec{r} \rangle - Q \vec{R}_{\text{CM}}$$



ρ_{charge} = charge distribution

\vec{r} = position vector

\vec{R}_{CM} = center of mass

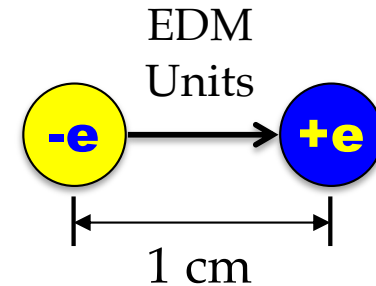
Q = net charge

“Thunder Cloud as Generator #2” (1971) by Paterson Ewen [Art Gallery of Ontario]

Electric Dipole Moments Couple to E-fields

Magnetic Dipole Moments Couple to B-fields

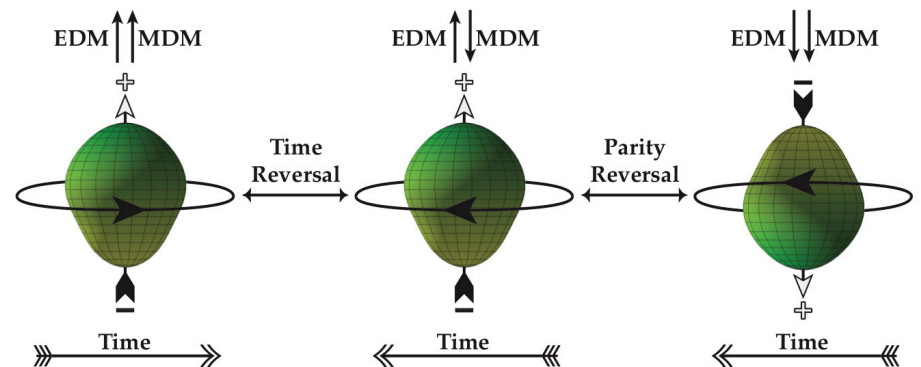
$$\mathcal{H} = -\mu \left(\frac{\vec{S} \cdot \vec{B}}{S} \right) - d \left(\frac{\vec{S} \cdot \vec{E}}{S} \right)$$



adapted from B. Filippone:

	<i>P</i> -parity	<i>T</i> -time reversal
\vec{S}	+	-
\vec{B}	+	-
\vec{E}	-	+
$\vec{S} \cdot \vec{B}$	+	+
$\vec{S} \cdot \vec{E}$	-	-

$$\vec{S} = \text{spin}$$

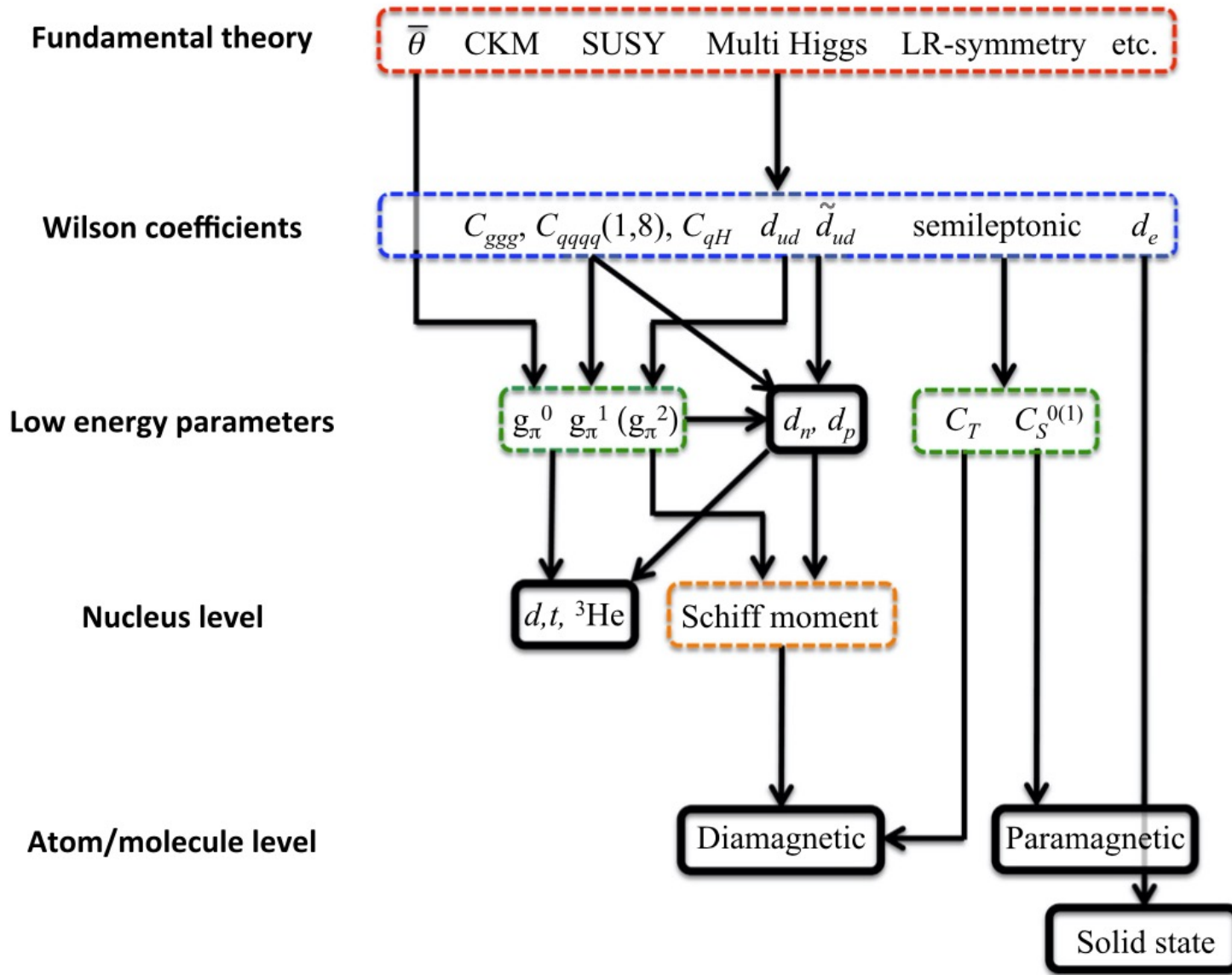


Theorist: ...trivial application of the Wigner-Eckart Theorem...

Experimentalist: ...blah blah blah Wigner-someone something...

Connecting New Physics to EDMs

T.E. Chupp, P. Fierlinger, M. Ramsey-Musolf, JTS, RMP 91:015001



Sources of *CP*-violation

Particle Physics Theory

Effective Field Theory

Lattice QCD Theory

Nuclear Theory

+

Nuclear Experiment

Atomic Theory

+

Atomic Experiment

Molecular Theory

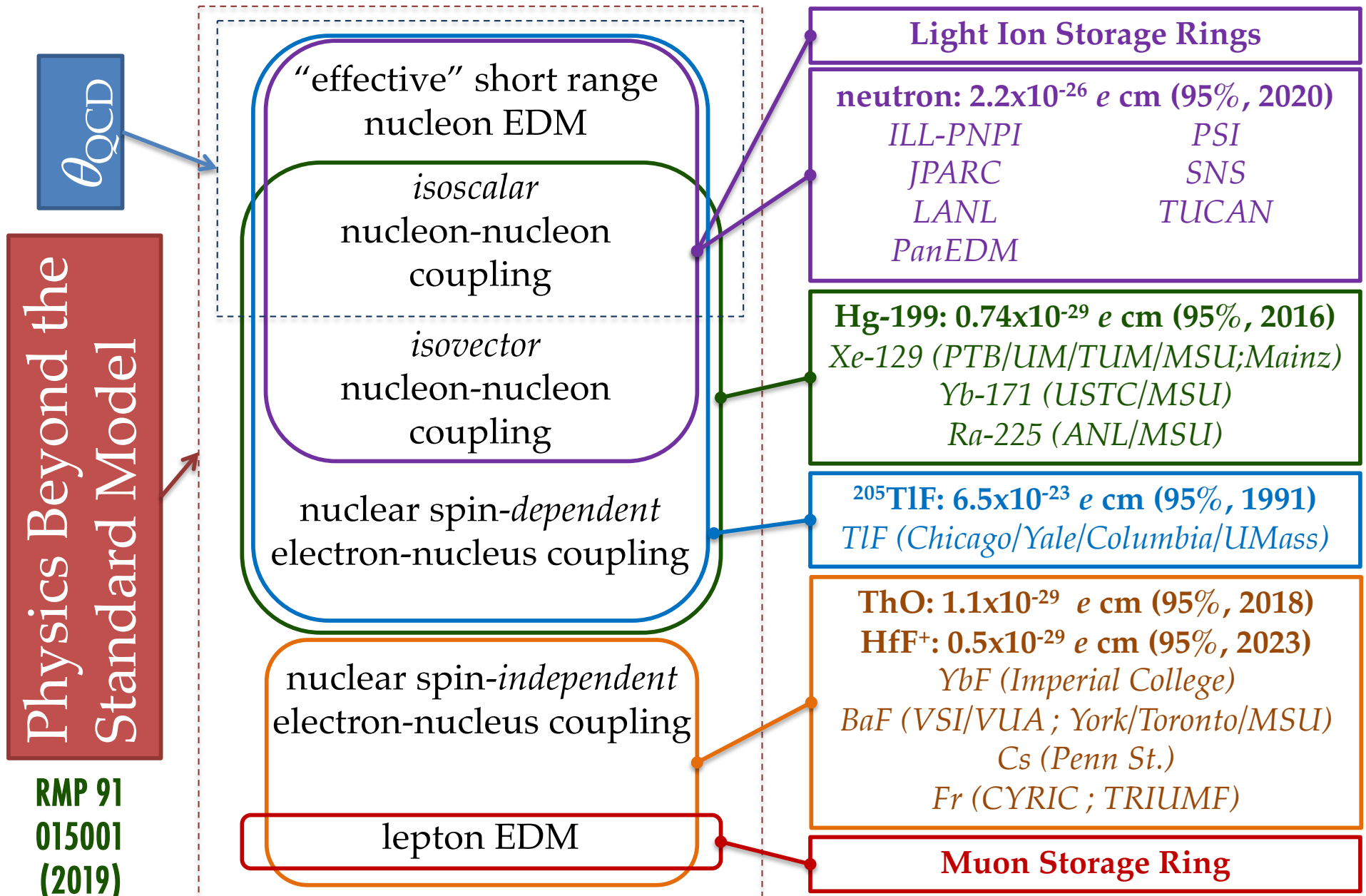
+

Molecular Experiment

Radiochemistry

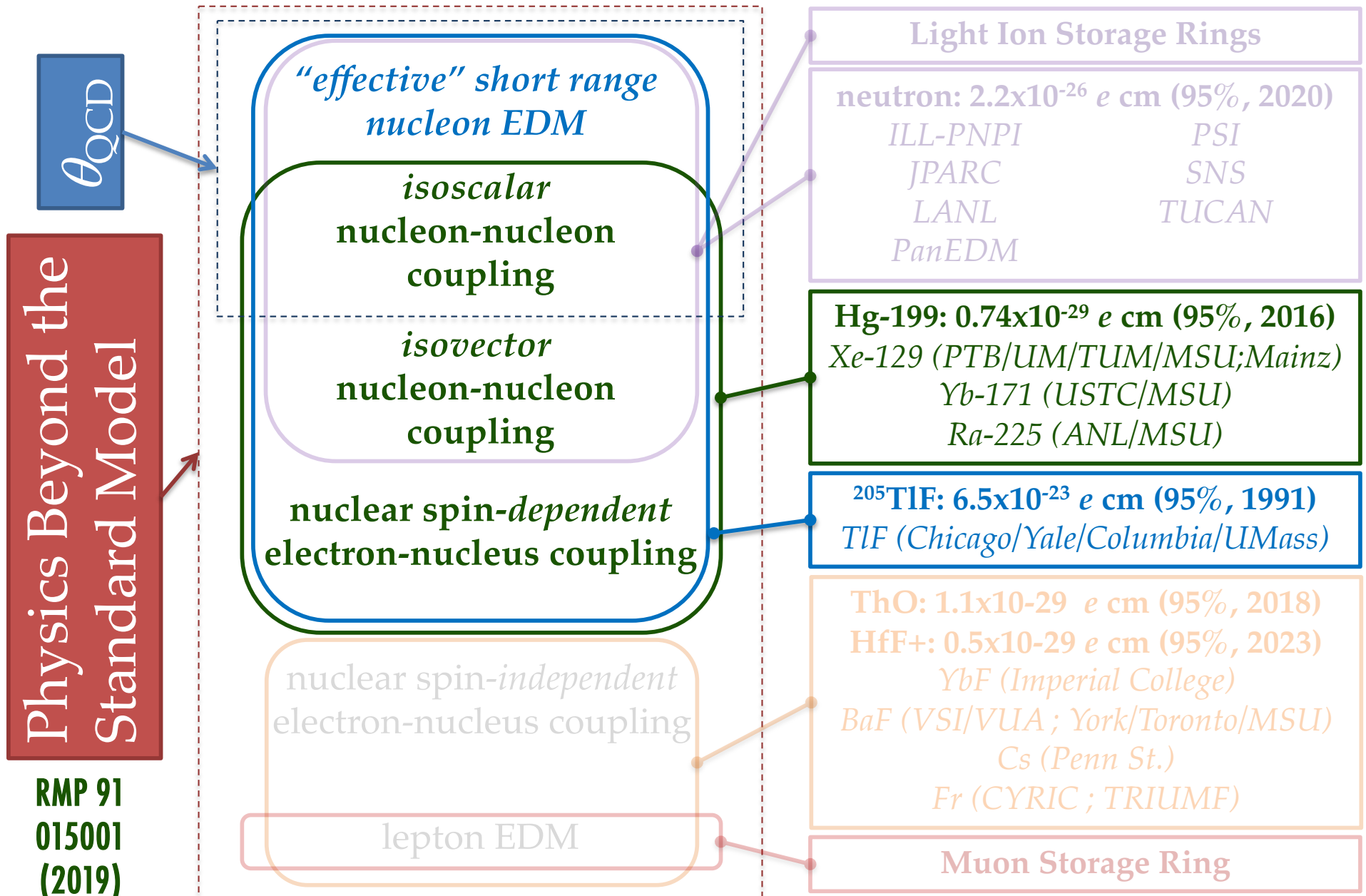
...EDMs

Different Sources of $\mathcal{T} \Leftrightarrow$ EDM of Different Systems



RMP 91
015001
(2019)

Different Sources of $\mathcal{T} \Leftrightarrow$ EDM of Different Systems

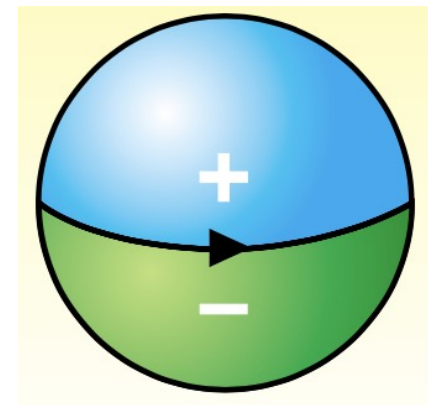


2023 EDM Limits: “Free” of Standard Model (SM) “Backgrounds”

Chupp, Fierlinger, Ramsey-Musolf, *JTS RMP* 91:015001 (2019) & *Nature* 562:355 (2018)
& *PRL* 124:081803 (2020) & *PRL* 129:231801 (2022) & *Science* 381:46 (2023)

System	Best Limit (95%) 1E-28 e cm	SM estimate 1E-28 e cm	Method (Location)
Neutron	220	$\sim 10^{-4}$	ultracold neutrons in a bottle (PSI)
“Electron”	0.11 0.05	$\sim 10^{-7}$	cold ThO beam (Chicago/Harvard/Northwestern) trapped HfF ⁺ (JILA/Boulder)
Hg-199	0.074	$\sim 10^{-6}$	atoms in vapor cell (UW-Seattle)

Imagine a Hg-199 atom that is composed of two oppositely charged hemispherical shells each with charge magnitude e ...



Physics Today, June 2003

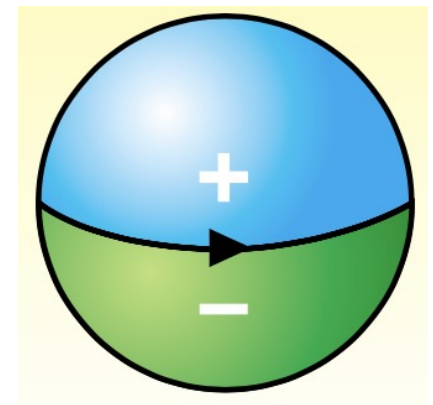
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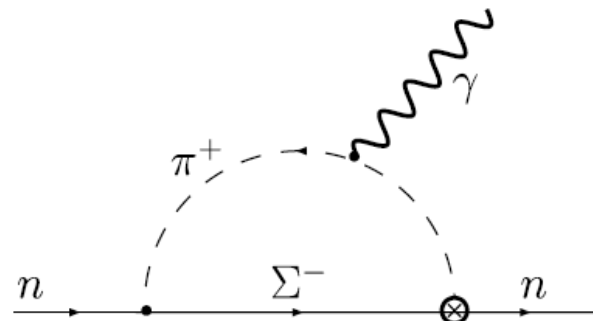
Imagine a Hg-199 atom that is composed of two oppositely charged hemispherical shells each with charge magnitude e ...

...if the Hg-199 atom was the size of the Earth, then the maximum thickness of these shells would be less than the diameter of a strand of human hair.

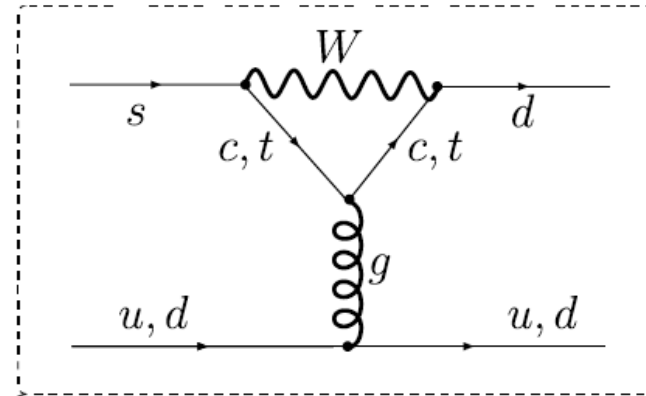


Physics Today, June 2003

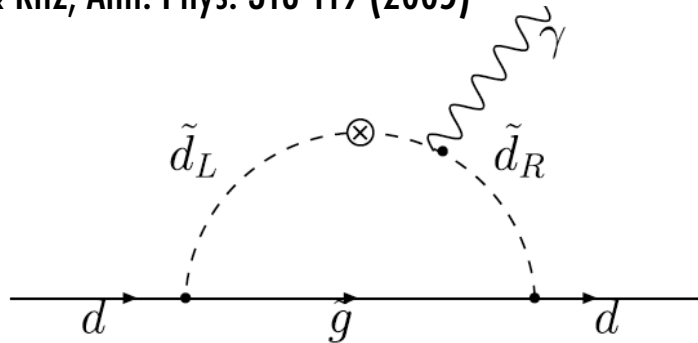
EDMs From Standard Model vs. New Physics



Pospelov & Ritz, Ann. Phys. 318 119 (2005)



Standard Model: higher order “penguin” diagram



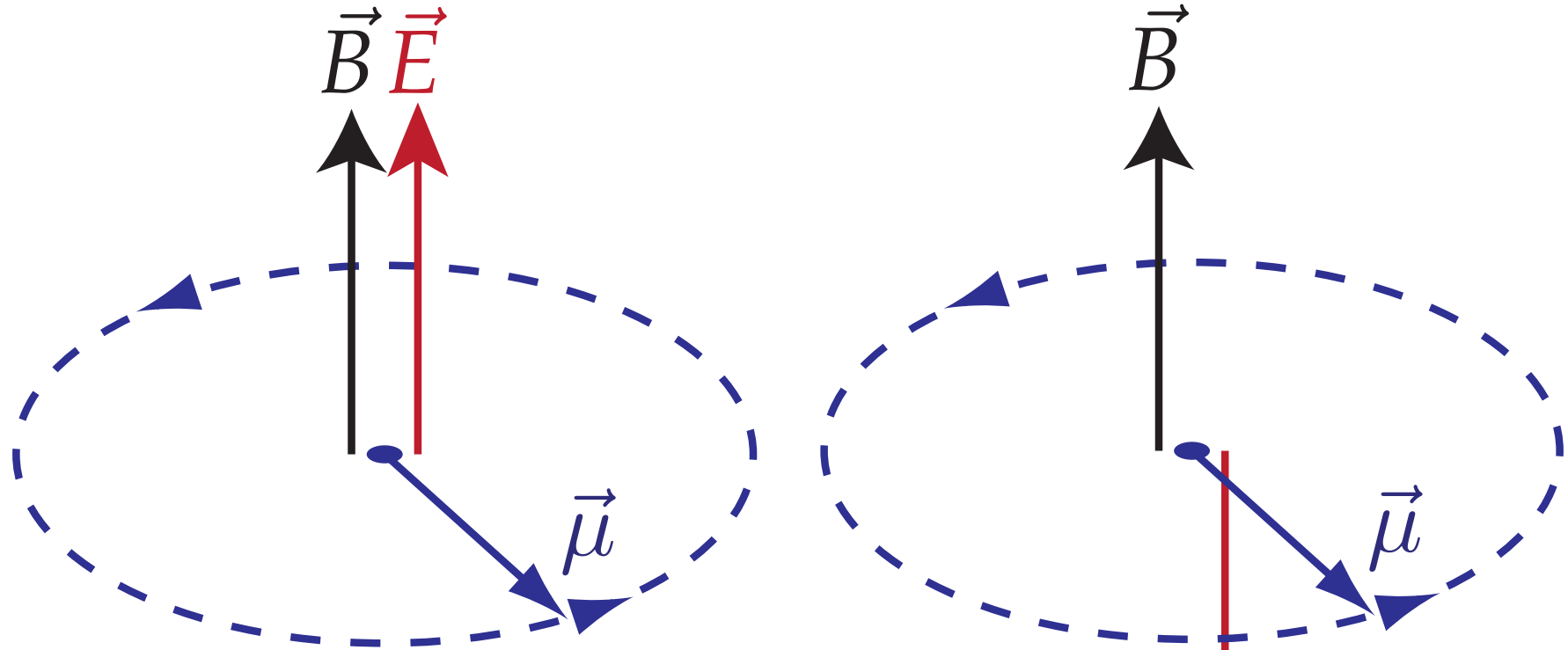
Supersymmetry: lower order

RMP 91:015001 (2019)

$$\frac{d}{10^{-28} \text{ e cm}} \approx \sin(\phi_{CP}) \left[\frac{1 \text{ TeV}}{\text{mass scale of new particles}} \right]^2$$

Always Measure Frequency = ν

Example: Spin Precession of a Spin-1/2 Particle



E = electric field
 B = magnetic field
 μ = magnetic dipole moment
 d = electric dipole moment
 h = Planck constant

$$h\nu_{\uparrow} = 2(\mu B_{\uparrow} + dE)$$

$$h\nu_{\downarrow} = 2(\mu B_{\downarrow} - dE)$$

Statistics & Systematics

$$\sigma_\nu = \frac{\Gamma_{\text{linewidth}}}{\text{SNR}}$$

$$\Delta\nu = \nu_\uparrow - \nu_\downarrow = \frac{4dE}{h} + \frac{2\mu(B_\uparrow - B_\downarrow)}{h}$$

Quantum Projection Noise (100% efficiency):

$$\frac{\sigma_d}{\sqrt{N_m}} = \frac{\hbar}{4E\sqrt{N_d T \tau}}$$

Electric
field

number of
detected particles

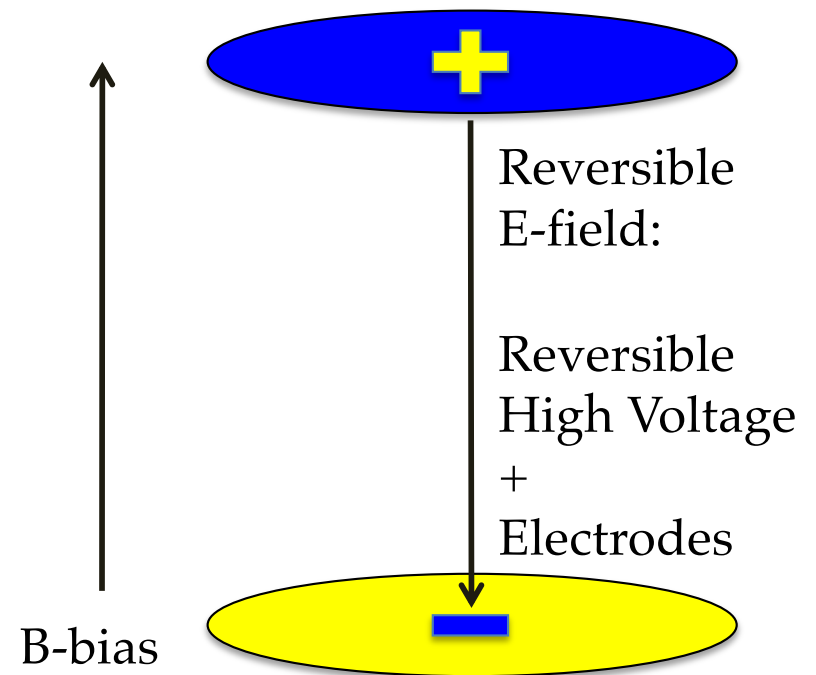
integration
time

interrogation
time

Magnetic Field Instabilities: Annoying

$$\Delta\nu = \nu_{\uparrow} - \nu_{\downarrow} = \frac{4dE}{h} + \frac{2\mu(B_{\uparrow} - B_{\downarrow})}{h}$$

Instabilities adds noise & limits the statistical precision.



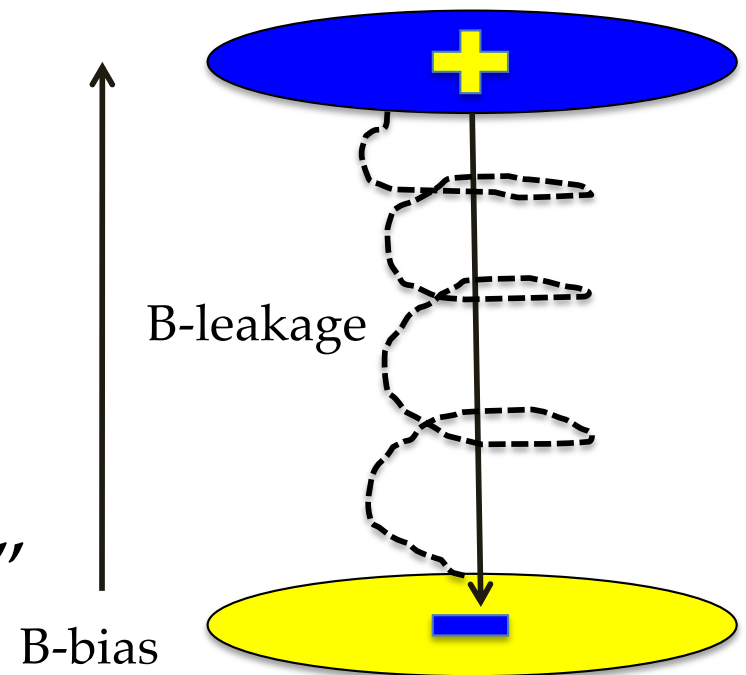
Electric Field-Correlated Systematic: Killer

$$\Delta\nu = \nu_{\uparrow} - \nu_{\downarrow} = \frac{4dE}{h} + \frac{2\mu(B_{\uparrow} - B_{\downarrow})}{h}$$

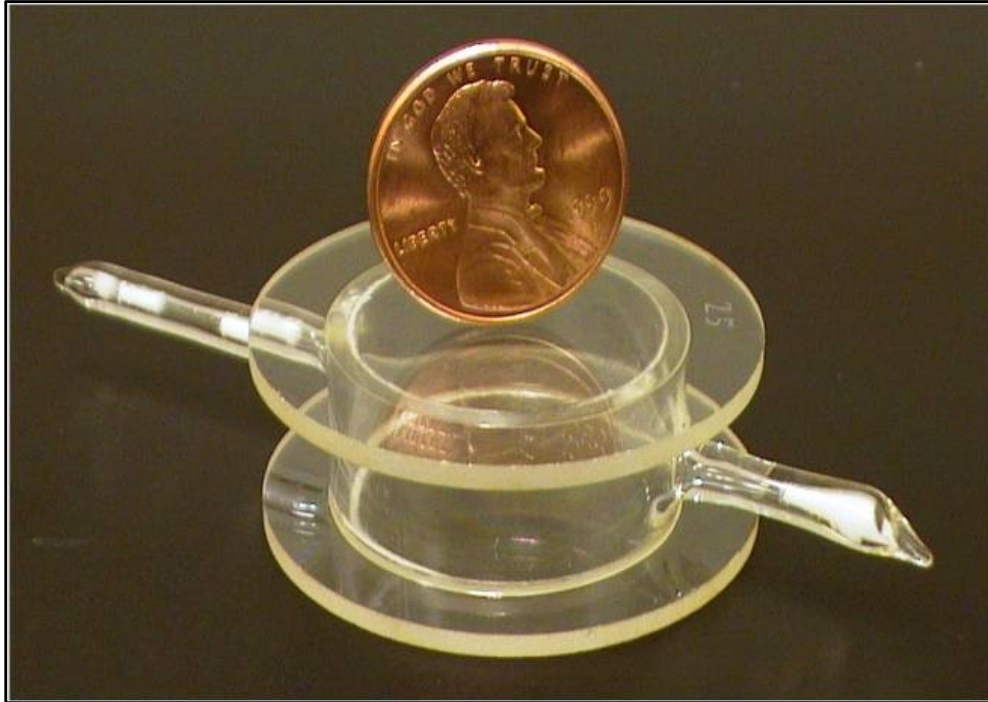
challenge!

Instabilities adds noise & limits the statistical precision.

“False” effects, things which change sign with the electric field, are nasty: “leakage current”



The Gold Standard: Hg-199 EDM Search



- diamagnetic, 1S_0 ground state
- $I = 1/2$, no elect. quad. moment
- high Z , (80) rel. atomic struct.
- stable, (17% n.a.) 92% enriched
- high vapor pressure, ($10^{13} / \text{cm}^3$)
- modest electric field, 10 kV / cm
- 30+ year old experiment!

B. Graner

$$\nu = 8.3 \text{ Hz}$$

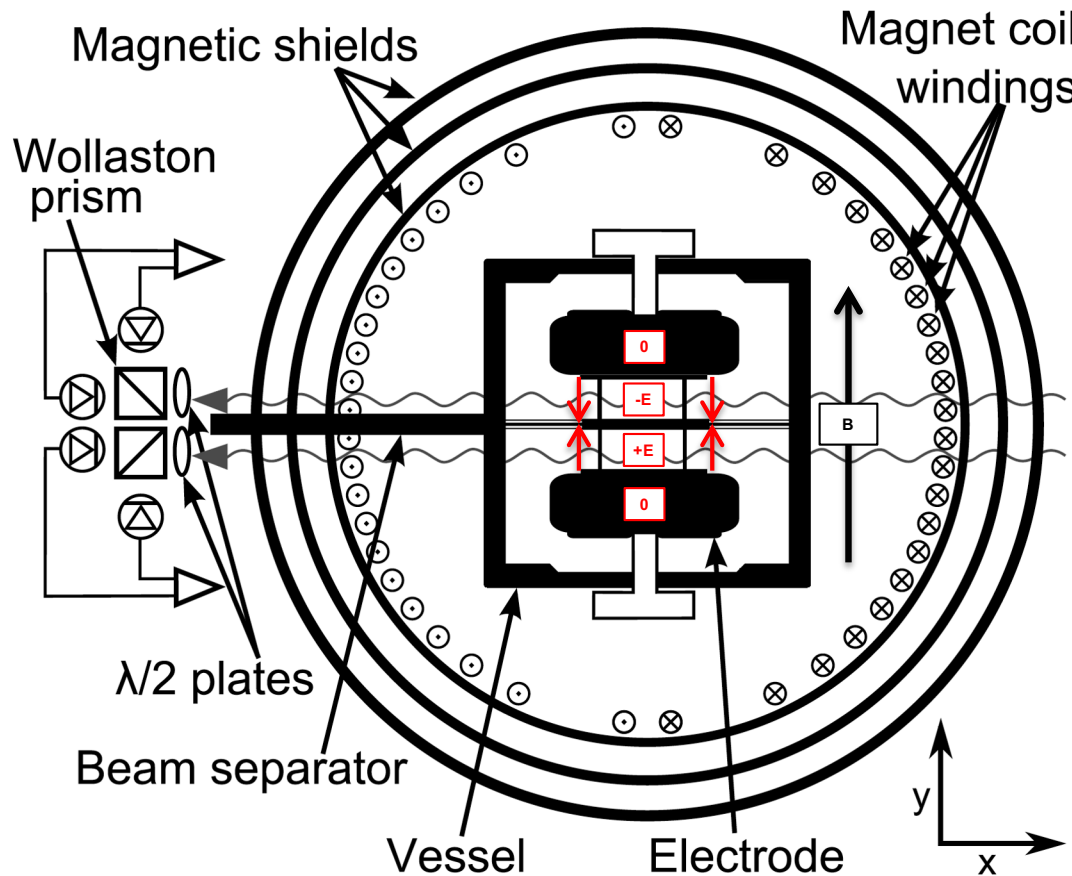
$$\Delta\nu \leq 0.1 \text{ nHz}$$

The best limit on atomic EDM:

$$\text{EDM}(^{199}\text{Hg}) < 0.74 \times 10^{-29} \text{ e-cm (95\% C.L.)}$$

Graner et al., PRL 116:161601 (2016)

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Limiting systematic appears to be ~ 10 nm scale motion of vapor cells when HV is switched in the presence of 2nd order B -field gradients.

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Intermission

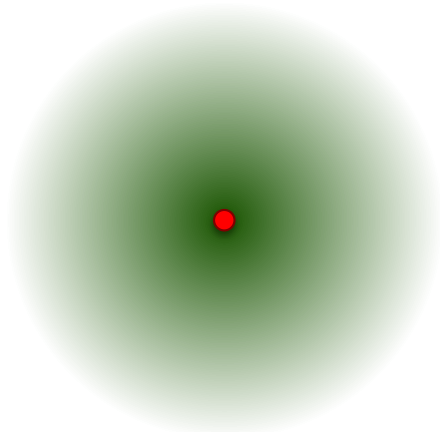
Questions?

1. stuff

Diamagnetic Atoms: All Electrons Are Paired

Neutral Atom

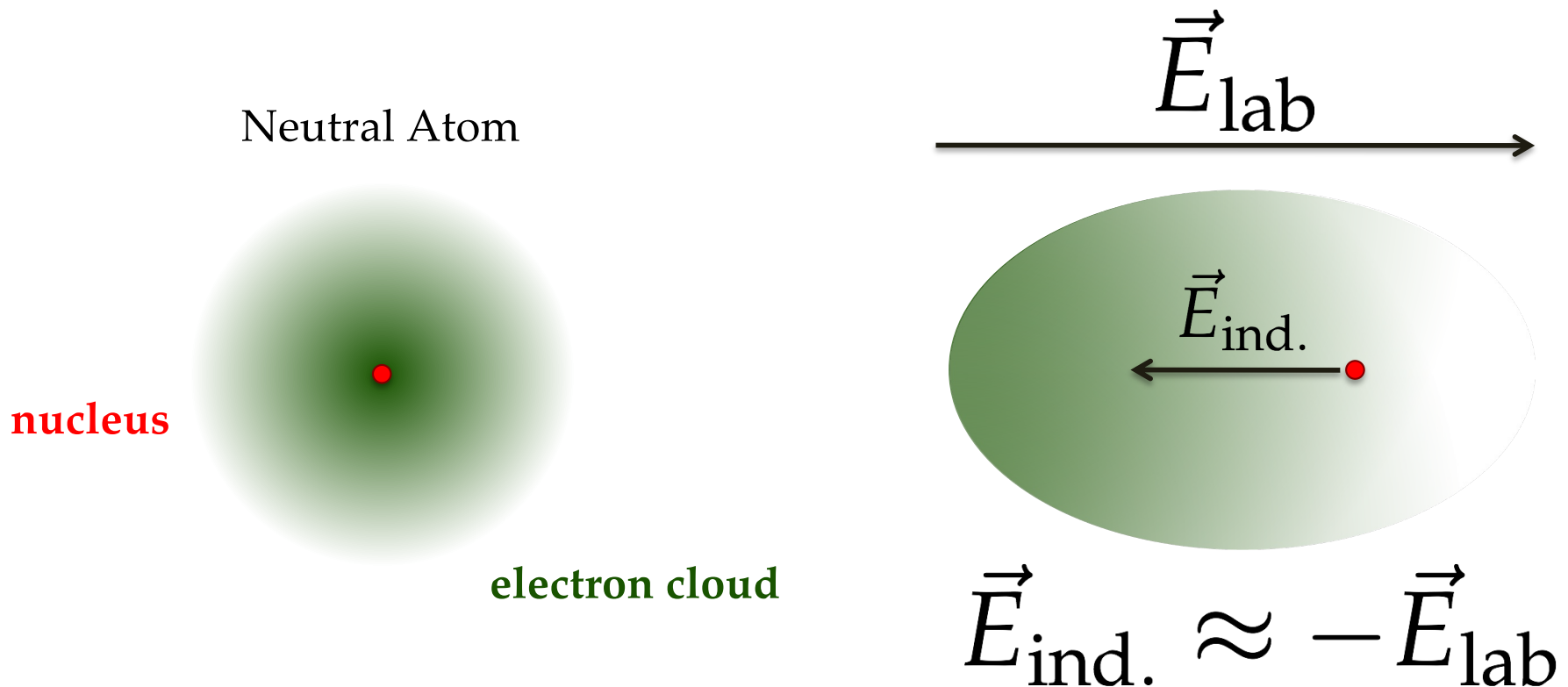
nucleus



electron cloud

Schiff Shielding in Diamagnetic Atoms

- **Shielding in Diamagnetic Atoms**
Schiff PR 132:2194 (1963)



Shielding Imperfect in Relativistic Atoms With Nonzero Nuclear Size

- Shielding in Diamagnetic Atoms

Schiff PR 132:2194 (1963)

- Relativistic atoms: The Sandars-Bouchiat Z^3 "Law"

Physics Letters 22:290 (1966) & Physics Letters 48B:111 (1974)

- ^{225}Ra vs ^{199}Hg vs. ^3He : 2.8 to 1 to 10^{-5}

JPB:AMOP 53:195004 (2020) & Phys. Rev. A 106, 022817 (2022)

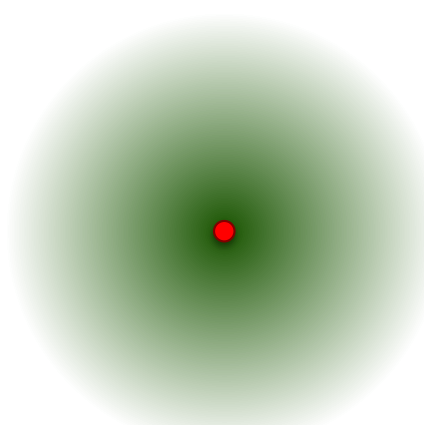
Madame
Professor
Marie-Anne
Bouchiat



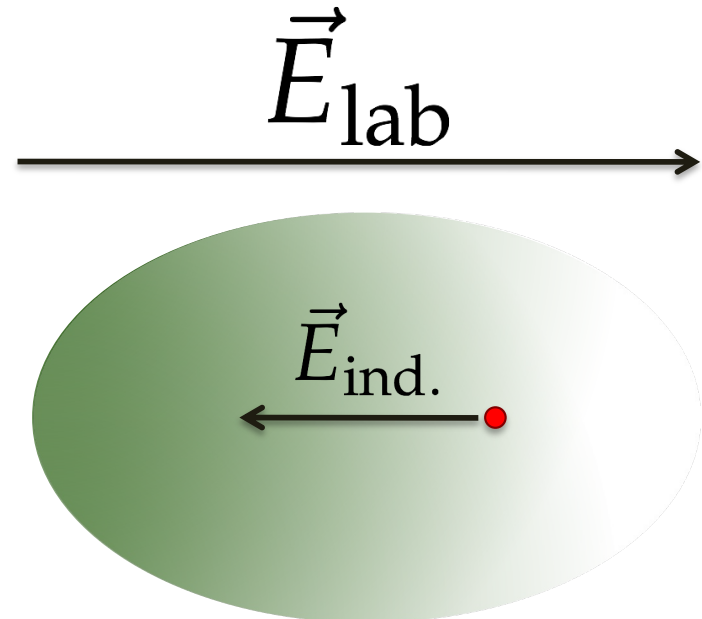
SCAN ME

Neutral Atom

nucleus



electron cloud



$$\vec{E}_{\text{ind.}} \approx -\vec{E}_{\text{lab}}$$

Residual \mathbb{P} & \mathbb{F} Observable: Nuclear Schiff Moment

- Shielding in Diamagnetic Atoms

Schiff PR 132:2194 (1963)

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$$\vec{d}_{\text{atom}} = \kappa_{\text{atom}} Z^3 \vec{S}$$

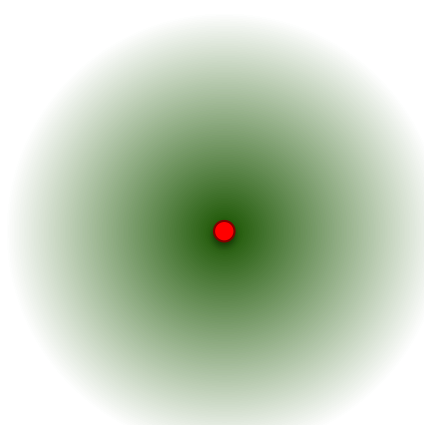
Schiff Moment

$$\vec{S} = \frac{\langle er^2 \vec{r} \rangle}{10} - \frac{\langle r^2 \rangle \langle e\vec{r} \rangle}{6}$$

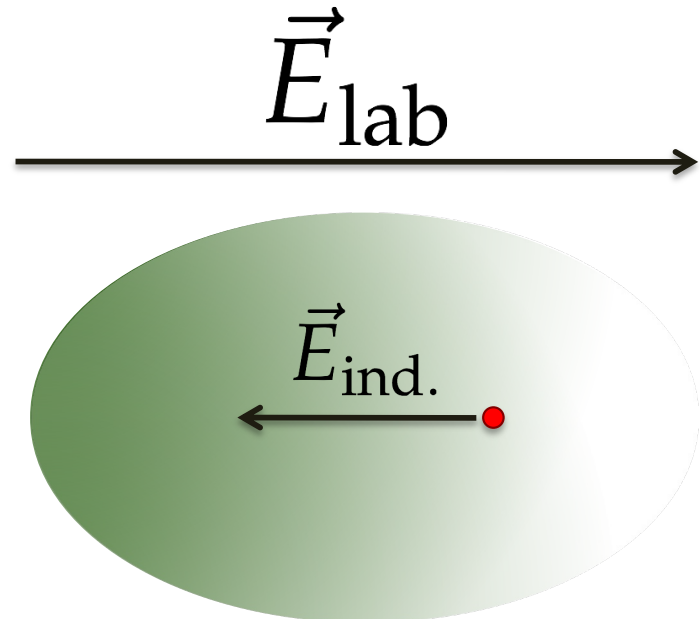
Zh. Eksp. Teor. Fiz. 87, 1521-1540 (1984)

Neutral Atom

nucleus



electron cloud



$$\vec{E}_{\text{ind.}} \approx -\vec{E}_{\text{lab}}$$

\mathbb{P} & \mathbb{T} Physics: First Order Perturbation Theory

$$S_z = \frac{\langle er^2 z \rangle}{10} - \frac{\langle r^2 \rangle \langle ez \rangle}{6}$$

$$S \equiv \langle \Psi_0 | S_z | \Psi_0 \rangle = \sum_{k \neq 0} \frac{\langle \Psi_0 | S_z | \Psi_k \rangle \langle \Psi_k | V_{\mathbb{P}\mathbb{T}} | \Psi_0 \rangle}{E_0 - E_k} + \text{c.c.}$$

- The \mathbb{P} and \mathbb{T} physics that we seek (unknown & common to all isotopes)

Isotopes With Nearly Degenerate Nuclear States

$$S_z = \frac{\langle er^2 z \rangle}{10} - \frac{\langle r^2 \rangle \langle ez \rangle}{6}$$

$$S \equiv \langle \Psi_0 | S_z | \Psi_0 \rangle = \sum_{k \neq 0} \frac{\langle \Psi_0 | S_z | \Psi_k \rangle \langle \Psi_k | V_{\mathbb{P}\mathbb{T}} | \Psi_0 \rangle}{E_0 - E_k} + \text{c.c.}$$

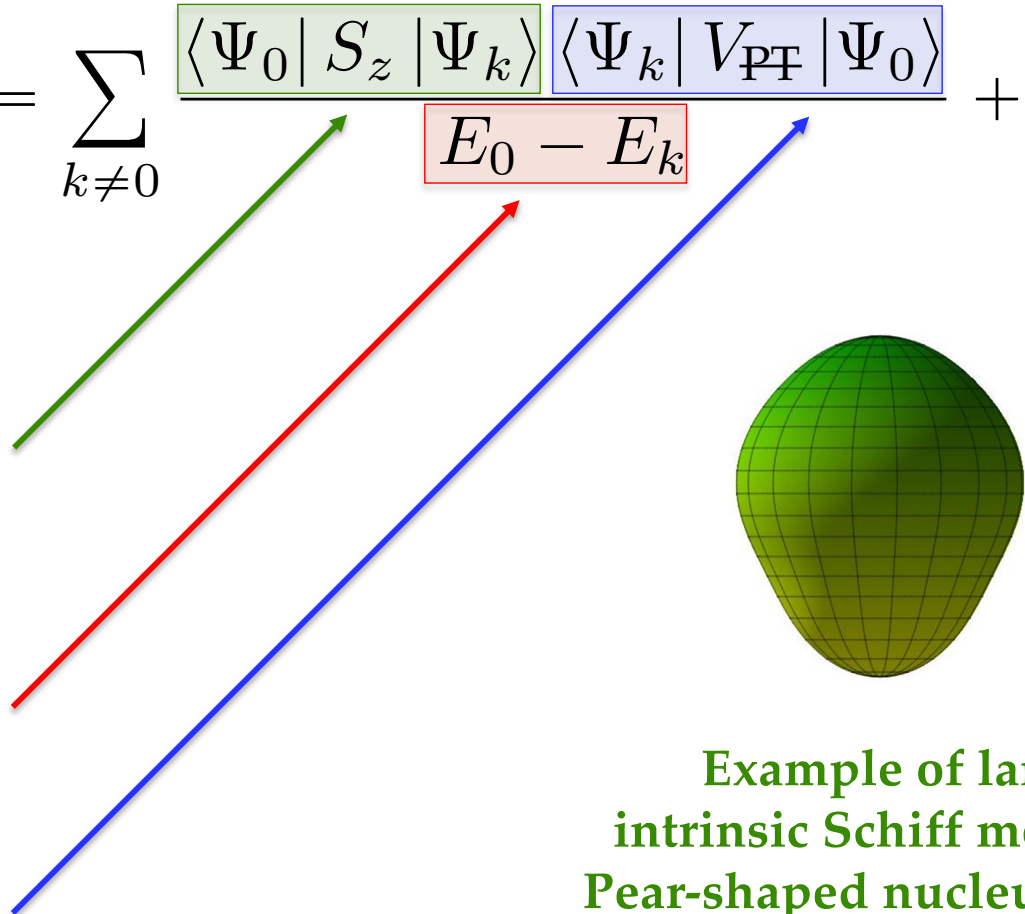
- Difference in lab-frame nuclear energy levels
- The \mathbb{P} and \mathbb{T} physics that we seek (unknown & common to all isotopes)

Nuclear Schiff Moment in the Lab Frame

$$S_z = \frac{\langle er^2 z \rangle}{10} - \frac{\langle r^2 \rangle \langle ez \rangle}{6}$$

$$S \equiv \langle \Psi_0 | S_z | \Psi_0 \rangle = \sum_{k \neq 0} \frac{\langle \Psi_0 | S_z | \Psi_k \rangle \langle \Psi_k | V_{\mathbb{P}\mathbb{T}} | \Psi_0 \rangle}{E_0 - E_k} + \text{c.c.}$$

- Body-frame Schiff moment – large when there are intrinsic nuclear deformations
- Difference in lab-frame nuclear energy levels
- The \mathbb{P} and \mathbb{T} physics that we seek (unknown & common to all isotopes)



Example of large intrinsic Schiff moment: Pear-shaped nucleus in the “body-frame”

Pear-Shaped Nuclei = Nearly Degenerate Parity Doublets

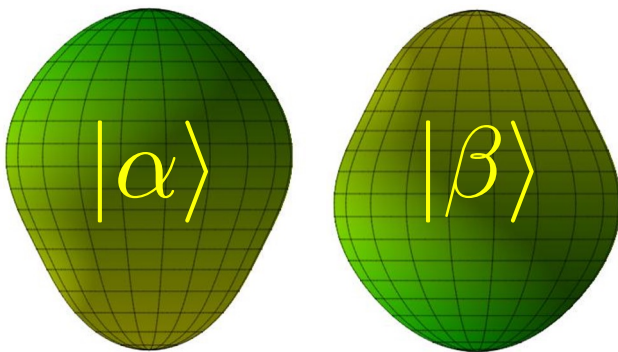
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$$S \equiv \langle \Psi_0 | S_z | \Psi_0 \rangle = \sum_{k \neq 0} \frac{\langle \Psi_0 | S_z | \Psi_k \rangle \langle \Psi_k | V_{\text{PT}} | \Psi_0 \rangle}{E_0 - E_k} + \text{c.c.}$$

Parity Doublet

- Nearly degenerate parity doublet

Haxton & Henley PRL 51:1937 (1983)



$$\begin{array}{l} \text{---} \\ \uparrow \Delta E \\ \text{---} \end{array} \quad |\Psi_1\rangle = \frac{|\alpha\rangle \mp |\beta\rangle}{\sqrt{2}}$$

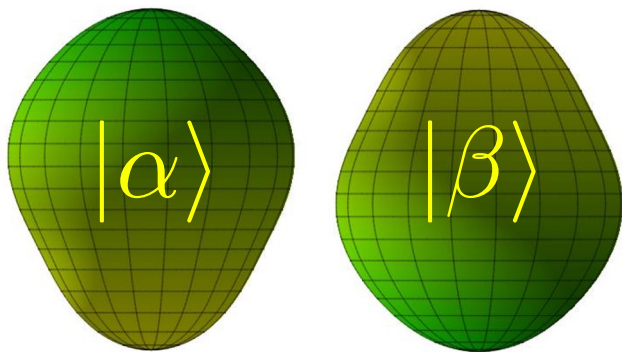
$$\quad \quad \quad |\Psi_0\rangle = \frac{|\alpha\rangle \pm |\beta\rangle}{\sqrt{2}}$$

Pear-Shaped Nuclei = Enhanced Intrinsic Schiff Moments

$$S_z = \frac{\langle er^2 z \rangle}{10} - \frac{\langle r^2 \rangle \langle ez \rangle}{6}$$

$$S \equiv \langle \Psi_0 | S_z | \Psi_0 \rangle = \sum_{k \neq 0} \frac{\langle \Psi_0 | S_z | \Psi_k \rangle \langle \Psi_k | V_{\text{PT}} | \Psi_0 \rangle}{E_0 - E_k} + \text{c.c.}$$

Parity Doublet



- Nearly degenerate parity doublet

Haxton & Henley PRL 51:1937 (1983)

- Large intrinsic Schiff moment due to octupole deformation

Auerbach, Flambaum, & Spevak PRL 76:4316 (1996)

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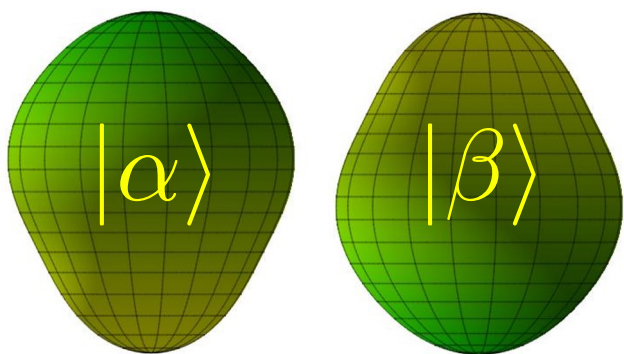
$$\quad \quad \quad |\Psi_0\rangle = \frac{|\alpha\rangle \pm |\beta\rangle}{\sqrt{2}}$$

Example: Enhanced Sensitivity in Radium-225

$$S_z = \frac{\langle er^2 z \rangle}{10} - \frac{\langle r^2 \rangle \langle ez \rangle}{6}$$

$$S \equiv \langle \Psi_0 | S_z | \Psi_0 \rangle = \sum_{k \neq 0} \frac{\langle \Psi_0 | S_z | \Psi_k \rangle \langle \Psi_k | V_{\text{PT}} | \Psi_0 \rangle}{E_0 - E_k} + \text{c.c.}$$

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Haxton & Henley PRL 51:1937 (1983)

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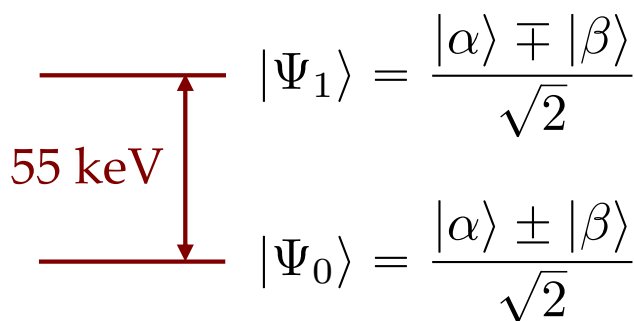
Auerbach, Flambaum, & Spevak PRL 76:4316 (1996)

Total Enhancement Factor: EDM (²²⁵Ra) / EDM (¹⁹⁹Hg)

Skyrme Model	Isoscalar	Isovector
SIII	300	4000
SkM*	300	2000
SLy4	700	9000

²²⁵Ra: Dobaczewski & Engel PRL 94:232502 (2005)

¹⁹⁹Hg: Ban et al. PRC 82:015501 (2010)



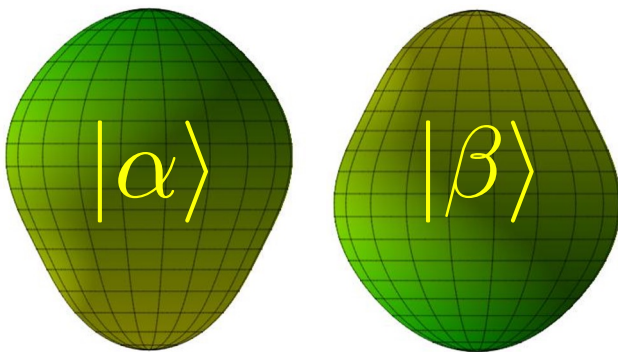
Protactinium-229 *May* Be Unusually Sensitive!

Choose an isotope with large deformations

$$S \equiv \langle \Psi_0 | S_z | \Psi_0 \rangle = \sum_{k \neq 0} \frac{\langle \Psi_0 | S_z | \Psi_k \rangle \langle \Psi_k | V_{PT} | \Psi_0 \rangle}{E_0 - E_k} + \text{c.c.}$$

Unknown

Parity Doublet



Pa-229: Haxton & Henley PRL 51:1937 (1983)

I. Ahmad et al Phys. Rev. C 92:024313 (2015)

Dobaczewski et al PRL 121, 232501 (2018)

$$\begin{array}{l} \text{---} \\ \uparrow \Delta E \\ \text{---} \\ |\Psi_1\rangle = \frac{|\alpha\rangle \mp |\beta\rangle}{\sqrt{2}} \\ \text{---} \\ \downarrow \Delta E \\ \text{---} \\ |\Psi_0\rangle = \frac{|\alpha\rangle \pm |\beta\rangle}{\sqrt{2}} \end{array}$$

Isotope	ΔE (keV)	$\tau_{1/2}$ (sec)	sensitivity
Hg-199	1800	stable	1
Rn-223	$\sim 10^2?$	10^3	10^2
Ra-225	55	10^6	10^3
Pa-229	(0.06 +/- 0.05)?	10^5	10^6

FRIB will make lots of Pa-229!

Intermission

Questions?

1. stuff

The Search For The Atomic EDM of Radium

$|d(^{225}\text{Ra})| < 50 \times 10^{-23} \text{ e-cm (95\%)}$

PRL 114:233002 (2015)

$|d(^{225}\text{Ra})| < 1.4 \times 10^{-23} \text{ e-cm (95\%)}$

equivalent to $\sim 1000 \times \text{EDM}(^{199}\text{Hg})$

PRC 94:025501 (2016)

Upgrades underway to improve sensitivity by x1000

Spectrochimica Acta Part B 172 105967 (2020)

^{226}Ra

nuclear spin = 0

$t_{1/2} = 1600 \text{ years}$

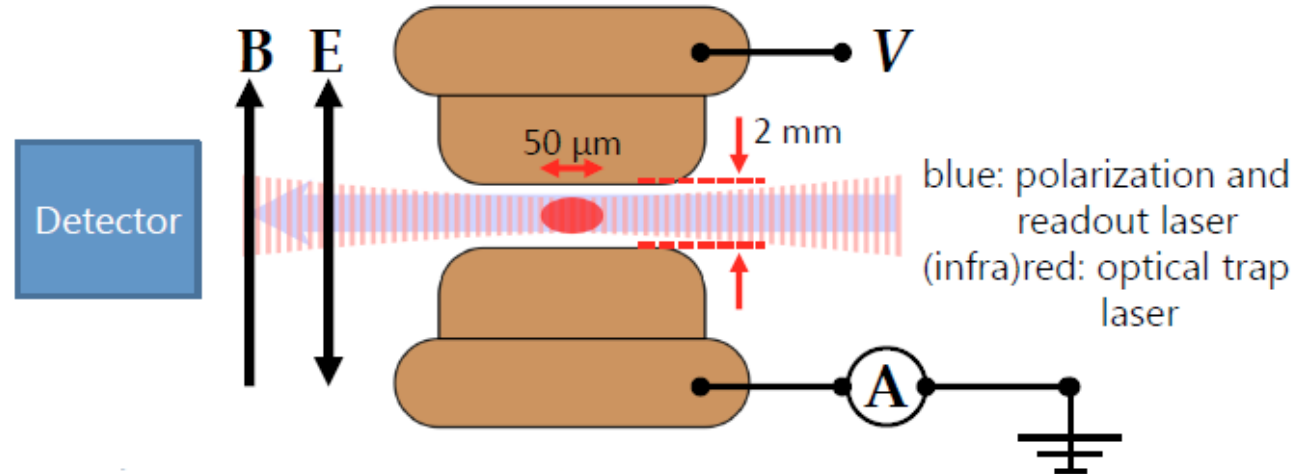
Low vapor pressure

^{225}Ra

Nuclear Spin = $\frac{1}{2}$

$t_{1/2} = 15 \text{ days}$

Low vapor pressure



EDM search using atoms held in Optical Lattice

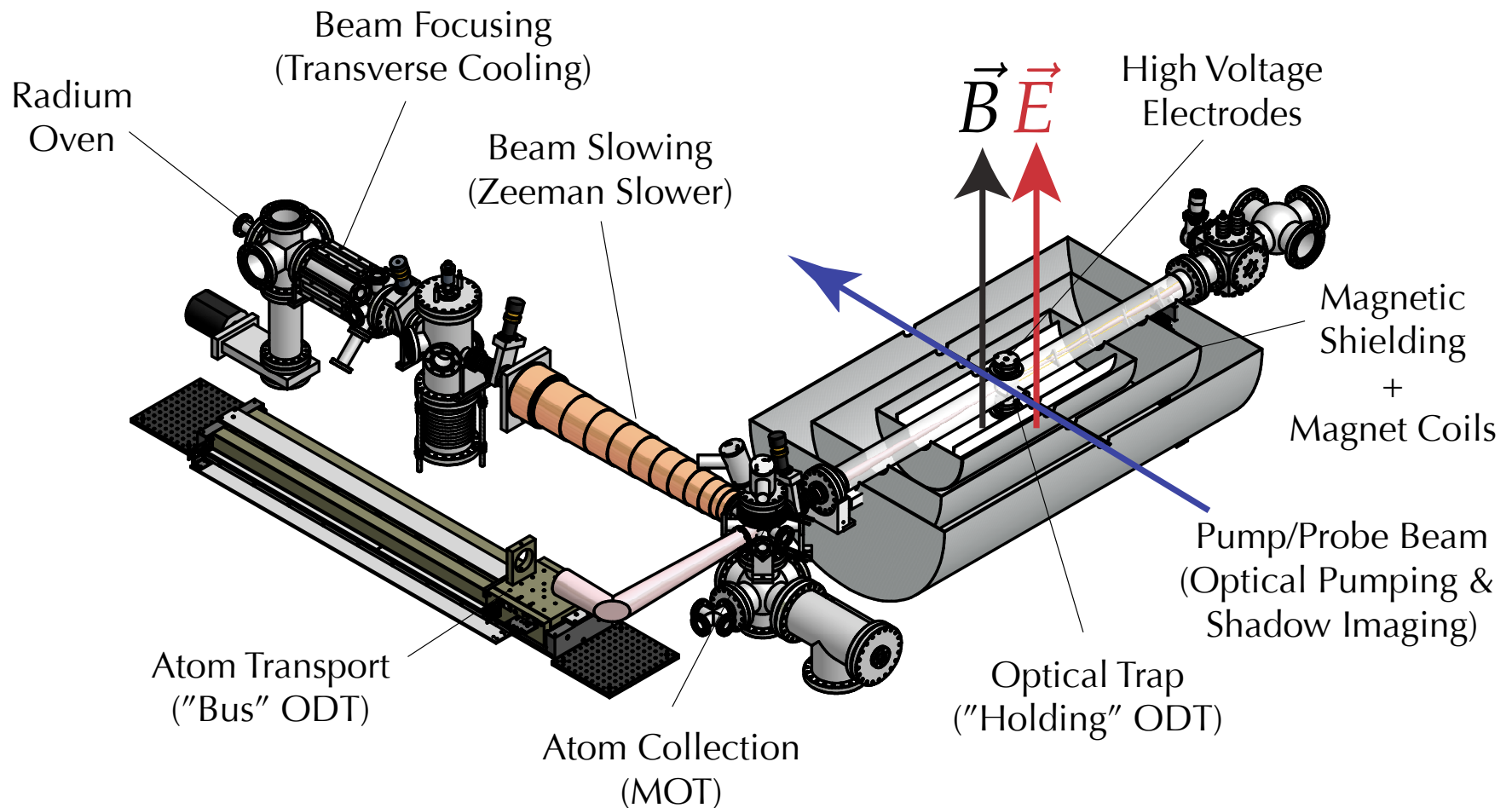
Romalis & Fortson PRA 59:4547 (1999)

Chin et al. PRA 63:033401 (2001)

Bishof et al. PRC 94:025501 (2016)

- Atoms concentrated in a very small region
- Long coherence time (100 s) PRL 129, 083001 (2022)
- negligible “ $v \times E$ ” systematics
- High electric field ($>300 \text{ kV/cm}$) in vacuum NIMA 1014 165738 (2021)
- Light-induced systematic effects can be controlled!

Laser Cooling & Trapping of Neutral Ra Atoms



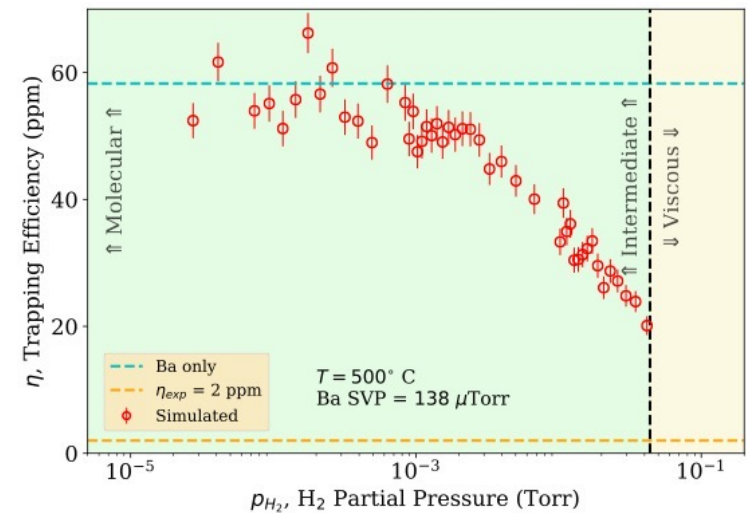
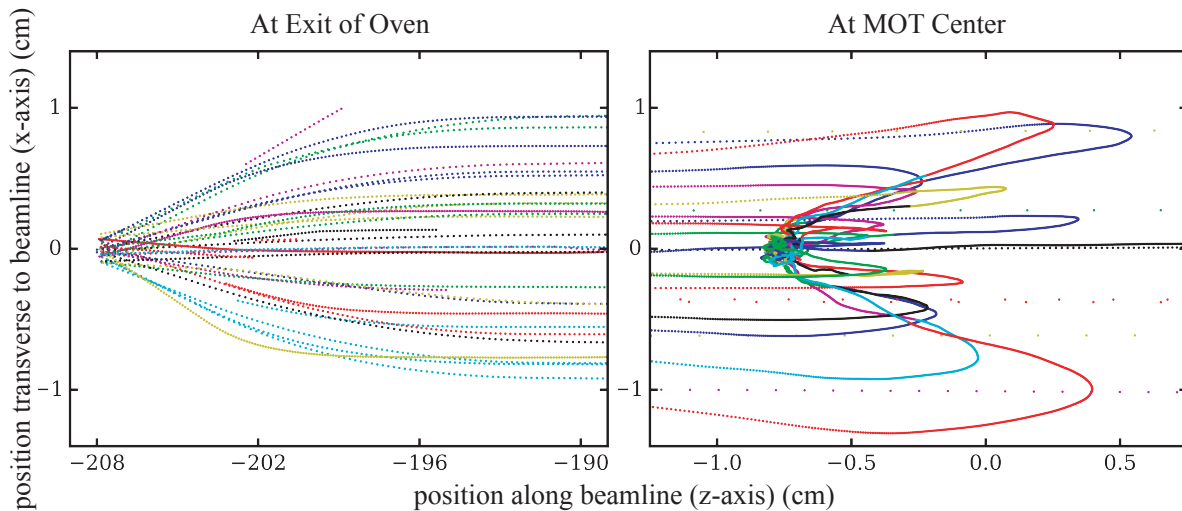
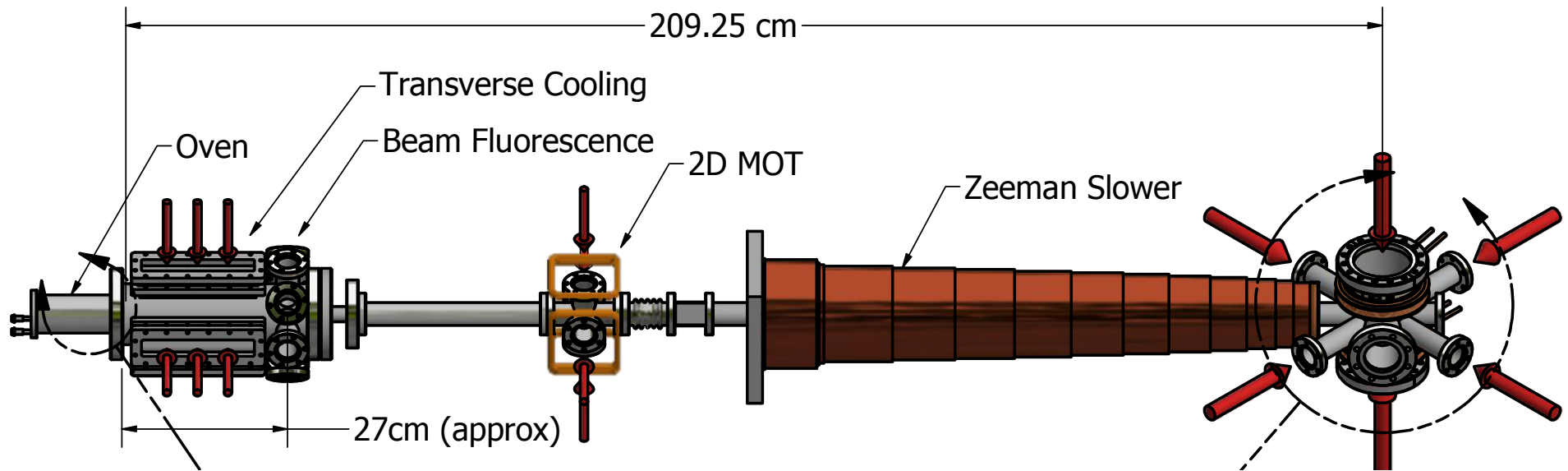
PRC 94:025501

$|d(\text{Ra-225})| < 1.4 \times 10^{-23} e \text{ cm (95\%)}$

completely statistics limited

several upgrades underway

Current Laser Trapping Efficiency: 2 ppm

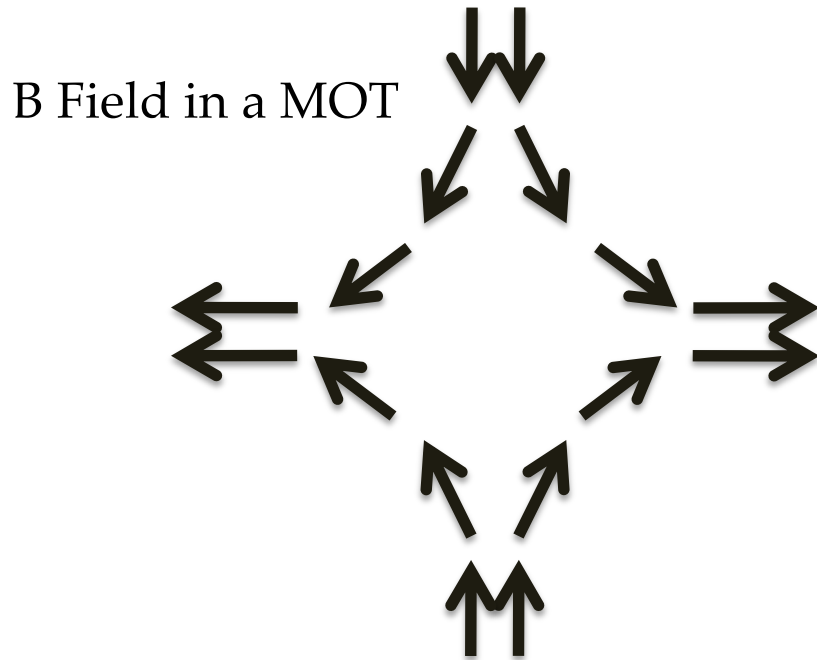


D. A. Potterveld, S. A. Fromm et al. (under review with PRA)

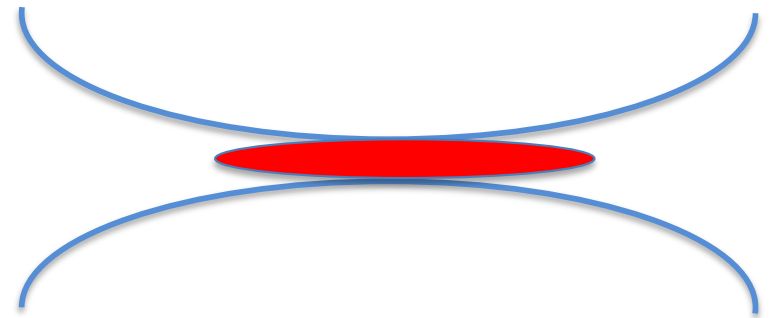
Neutral Atom Traps Using Lasers

Magneto-Optical Trap (MOT)

Optical Dipole Trap (ODT)



$$\mathcal{H} = -\vec{d}_{\text{ind}} \cdot \vec{E}_0 = \frac{\alpha}{4} E_0^2$$

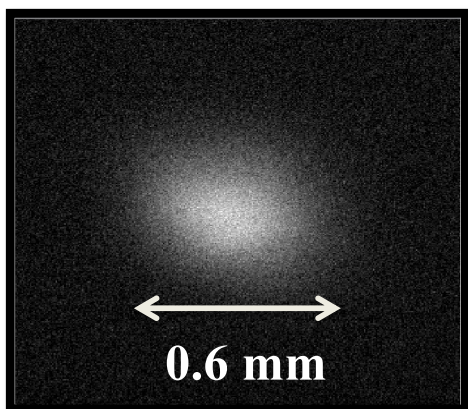


- Large capture volume 1 cm^3
- Efficient Collection
- Unsuitable B-field region
- Capture velocity $6 \text{ cm/s} = 30 \mu\text{K}$
- Laser cool @ 714 nm
- Only 1 repump @ 1429 nm

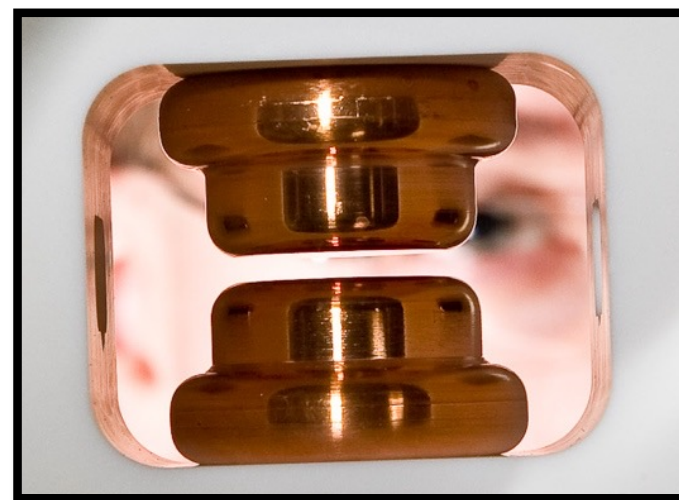
- Atoms trapped at beam focus
- 50 W @ 1550 nm
- 100 mm spot = Trap Depth of $400 \mu\text{K}$
- Good for transporting atoms
- Good for spatially confining atoms

Collecting & Transporting Ra-225 Atoms

Guest et al., PRL 98 093001 (2007)

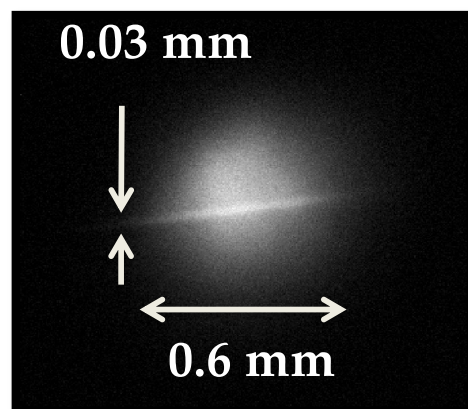


^{226}Ra MOT
20,000 atoms

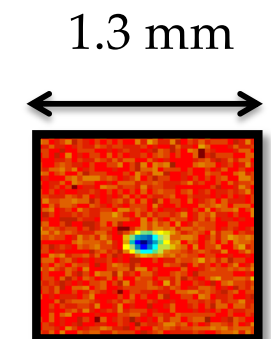


Copper
2.3 mm

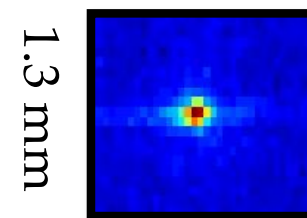
Parker et al., PRC 86 065503 (2012)



MOT + ODT
20,000 atoms



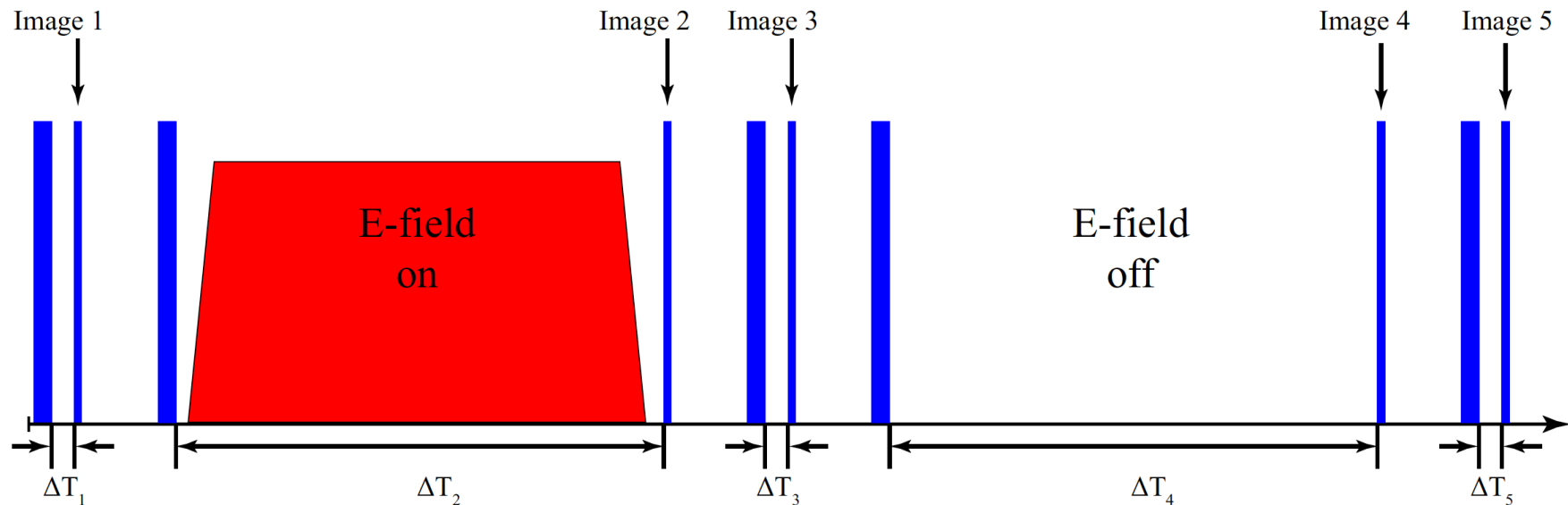
Absorption
Imaging



Fluorescence
Imaging

3000
atoms

Several Images Are Taken During One Cycle

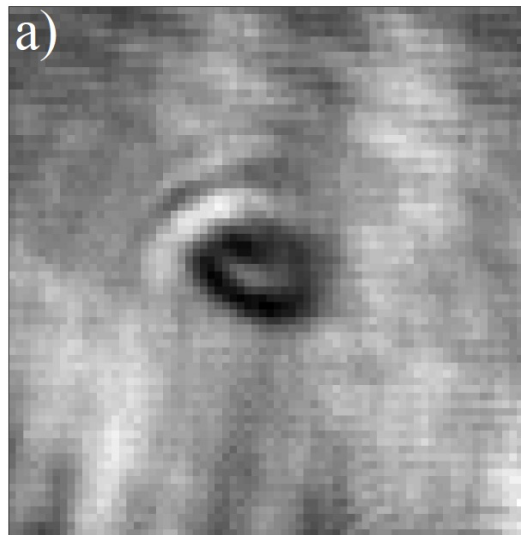


Images taken to account for changes in atom number and probe light intensity.

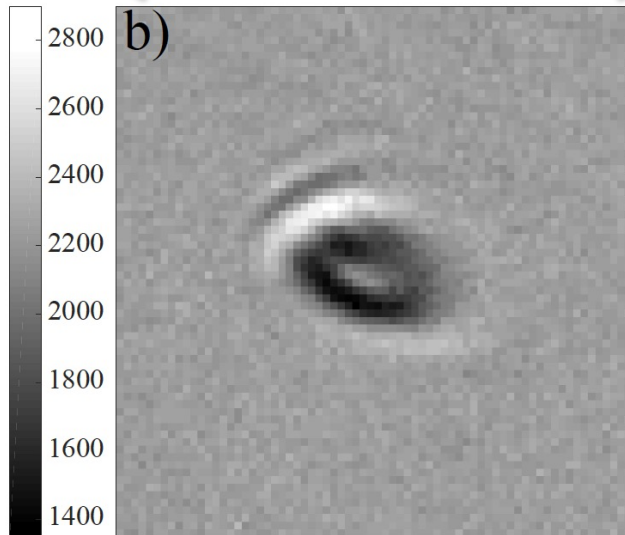
Data taken for electric field parallel, anti-parallel, and off for different time delays.

Image Background & Distortion Corrections

average of 8
raw images
of Ra-226

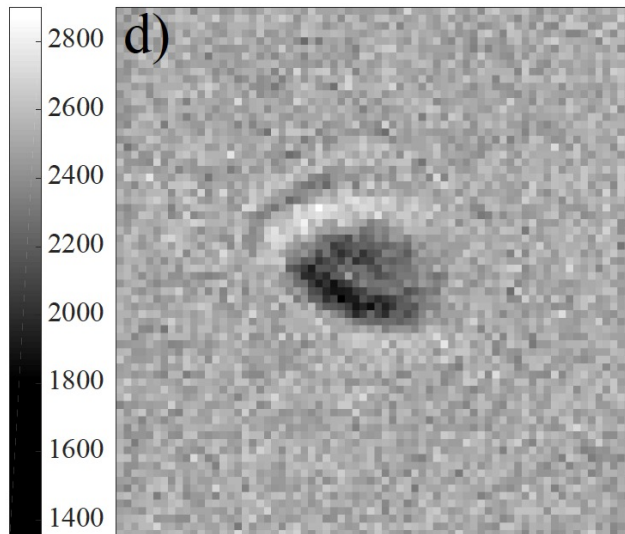
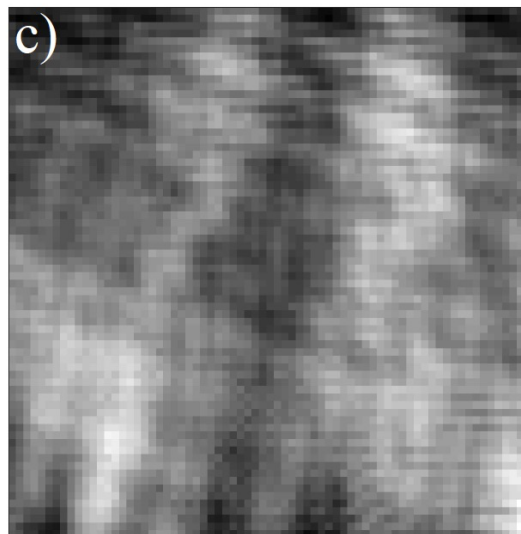


0.45 mm
←→



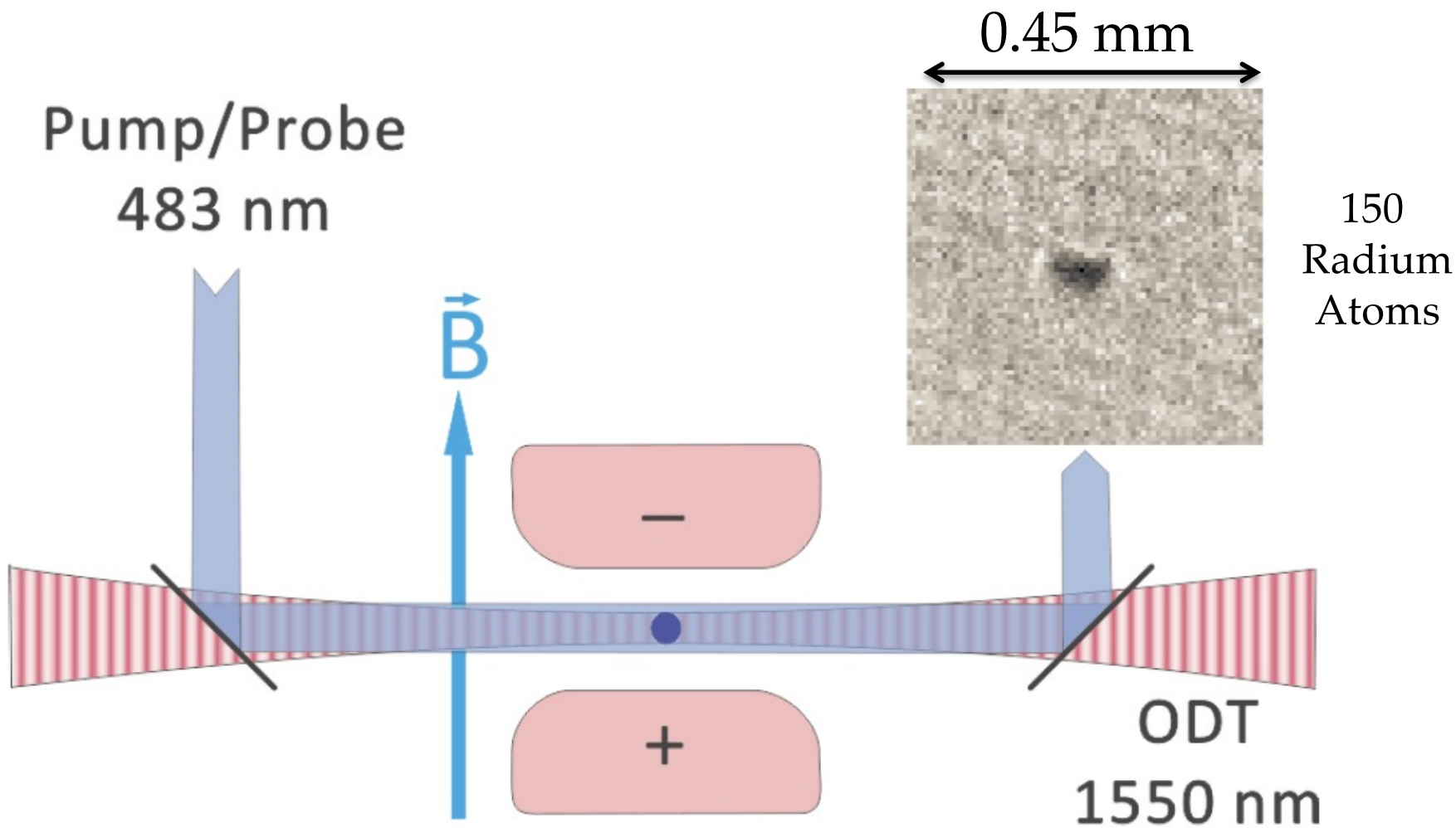
"clean"
Ra-226
image
 10^4 atoms

average of 63
raw images
of Ra-225



"clean"
Ra-225
image
 10^2 atoms

Radium Atoms Create a Shadow by Absorption

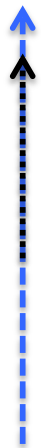
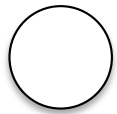


Parker et al. Phys. Rev. Lett. 114, 233002 (2015)

The Absorption Probability Oscillates at the Spin Precession Frequency (~ 20 Hz)

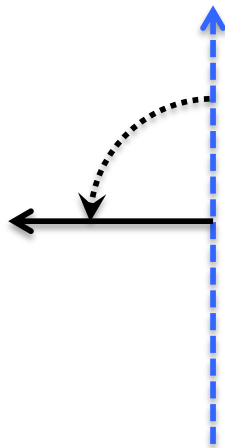
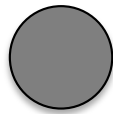
probability of absorbing probe light and creating a shadow:

0%

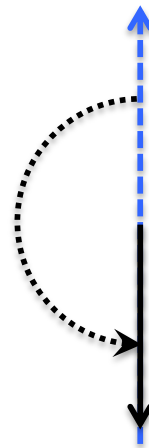


Atom spin

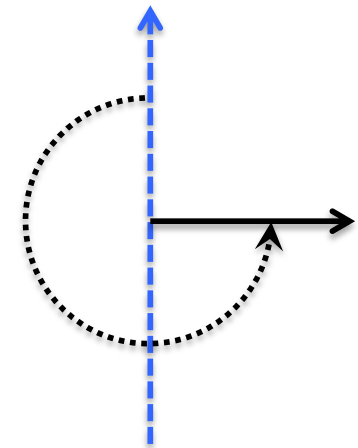
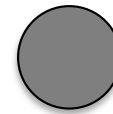
50%



100%



50%

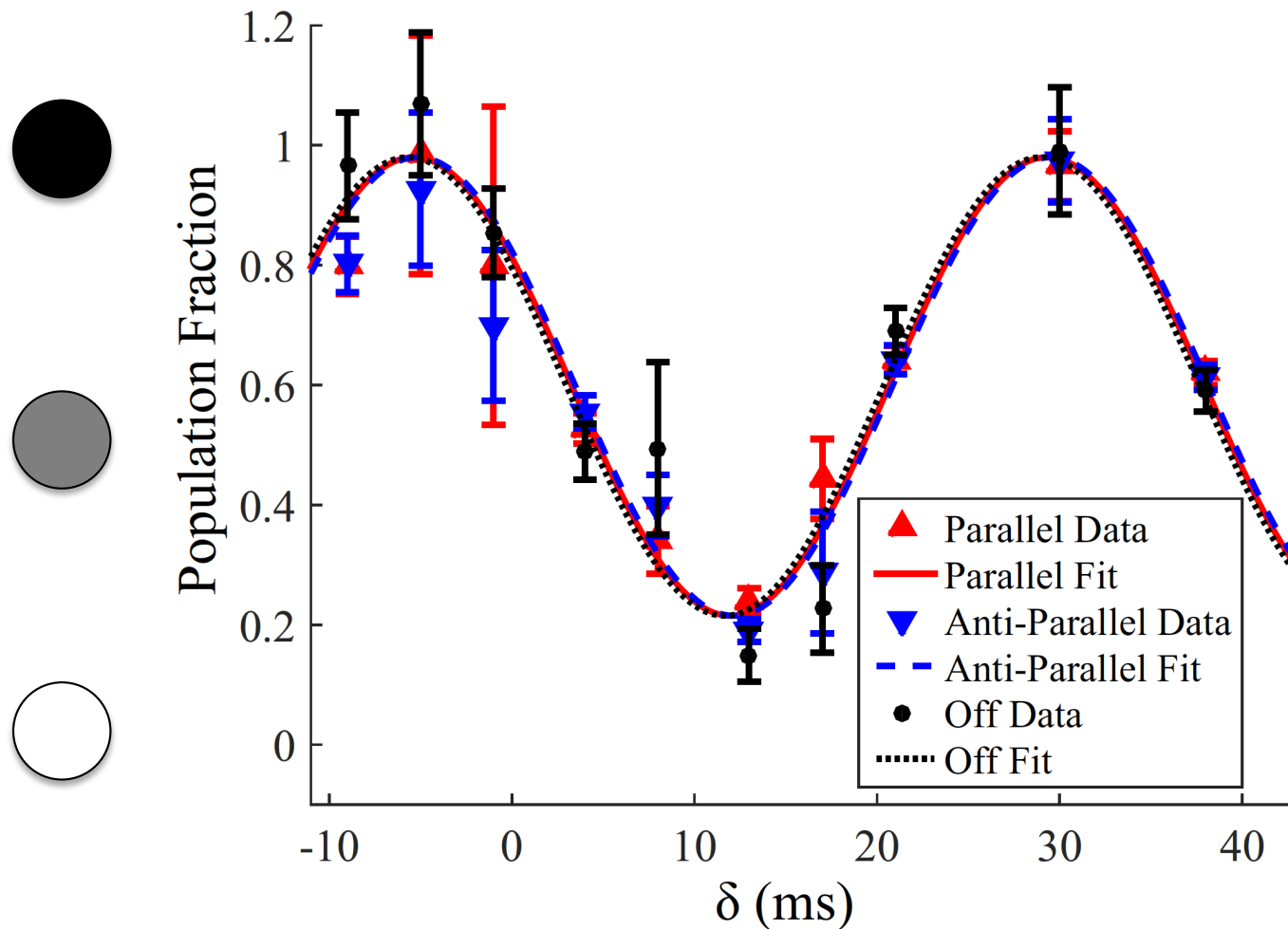


B-field & E-field point into or out of the screen

increasing time



Reconstructed Spin Precession Curve After $\tau = 20$ s (Shadow Measurements Taken At Different Time Delays)



$$d = \frac{h(\Delta\phi)}{4E\tau}$$

$\Delta\phi$ = phase shift between red and blue curves

Ra EDM: Completely Statistics Limited

Dec 2014: PRL 114:233002: $|d(\text{Ra-225})| < 50 \times 10^{-23} e \text{ cm}$ (95%)

June 2015: PRC 94:025501: $|d(\text{Ra-225})| < 1.4 \times 10^{-23} e \text{ cm}$ (95%)

Effect	Current uncertainty	α scenario uncertainty	β scenario uncertainty
E-squared effects	1×10^{-25}	7×10^{-29}	7×10^{-31a}
B-field correlations	1×10^{-25}	5×10^{-27}	3×10^{-29a}
Holding ODT power correlations	6×10^{-26}	9×10^{-30}	9×10^{-32a}
Stark interference	6×10^{-26}	2×10^{-27}	3×10^{-29a}
E-field ramping	9×10^{-28}	2×10^{-29}	N/A
Blue laser power correlations	7×10^{-28}	1×10^{-31}	1×10^{-31}
Blue laser frequency correlations	4×10^{-28}	8×10^{-30}	8×10^{-30}
$\mathbf{E} \times \mathbf{v}$ effects	4×10^{-28}	7×10^{-30}	N/A
Leakage current	3×10^{-28}	9×10^{-29}	N/A
Geometric phase	3×10^{-31}	7×10^{-30}	5×10^{-33}
Total	2×10^{-25}	5×10^{-27}	4×10^{-29a}

^aThis uncertainty will improve with the statistical sensitivity of the experiment.

More efficient detection of atoms: optical cycling

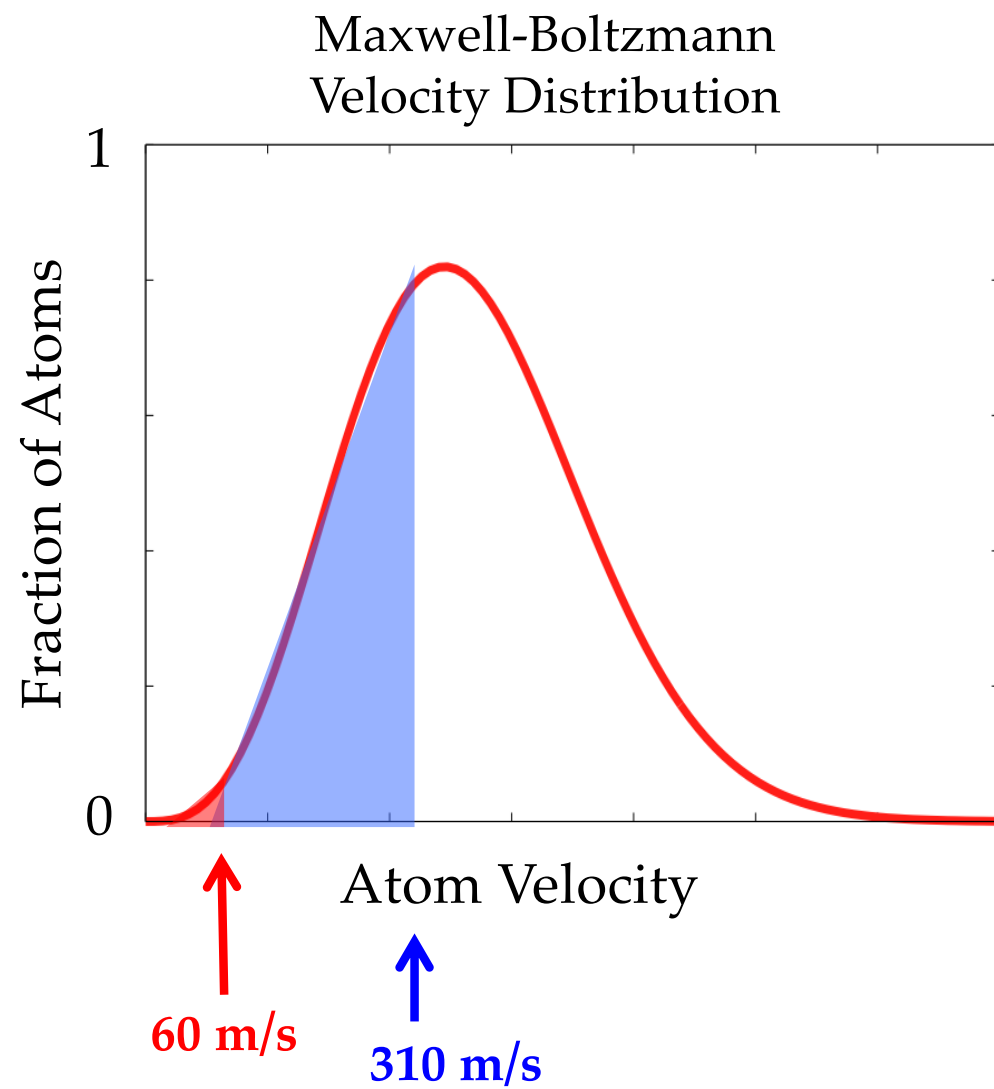
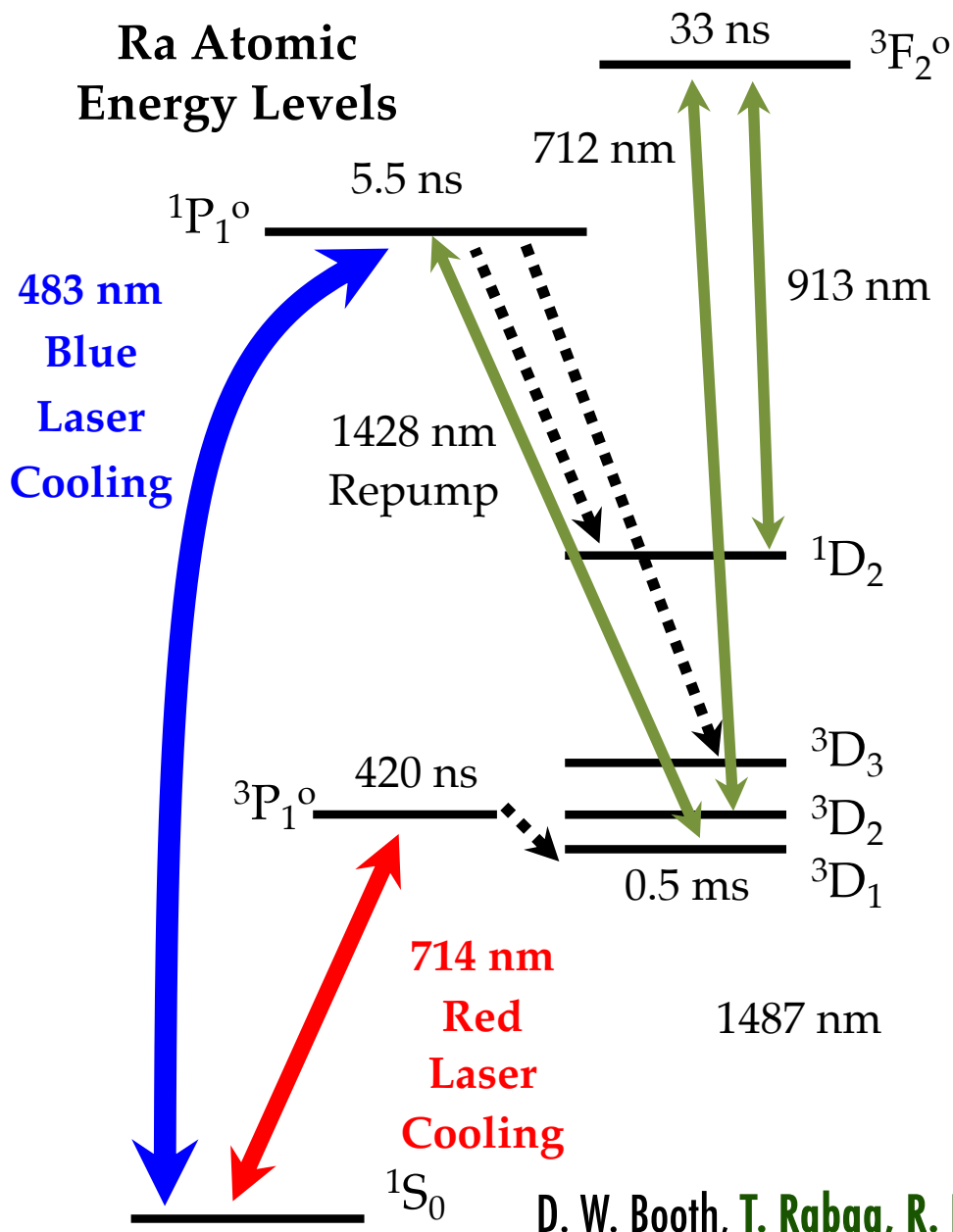
More efficient laser cooling and trapping: 1 ppm to 100 ppm

Higher electric field: 70 kV/cm to >350 kV/cm

More consistent supply of atoms: Isotope Harvesting @ FRIB

Goal is $<10^{-26} e \text{ cm}$ over 4 years and then $10^{-28} e \text{ cm}$ long term

“Blue” Upgrade: 2 ppm to >200 ppm



D. W. Booth, T. Rabga, R. Ready, et al. Spectrochimica Acta Part B 172 (2020) 105967

Towards Higher Electric Field: Bench Tests @ MSU

Increase E-field from 67 kV/cm without systematics:

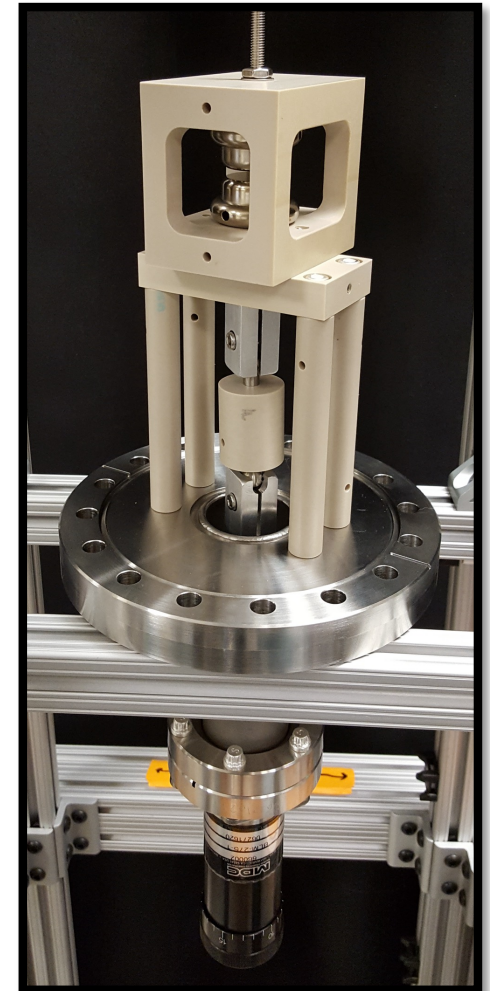
- higher voltage (15 kV to 25 kV)
- smaller gap (2.3 mm to 0.4 mm)
- **achieved >500 kV/cm = 50 MV/m
with Nb + High Pressure Rinse**

For the next run ($\leq 10^{-26} e^* \text{cm}$)

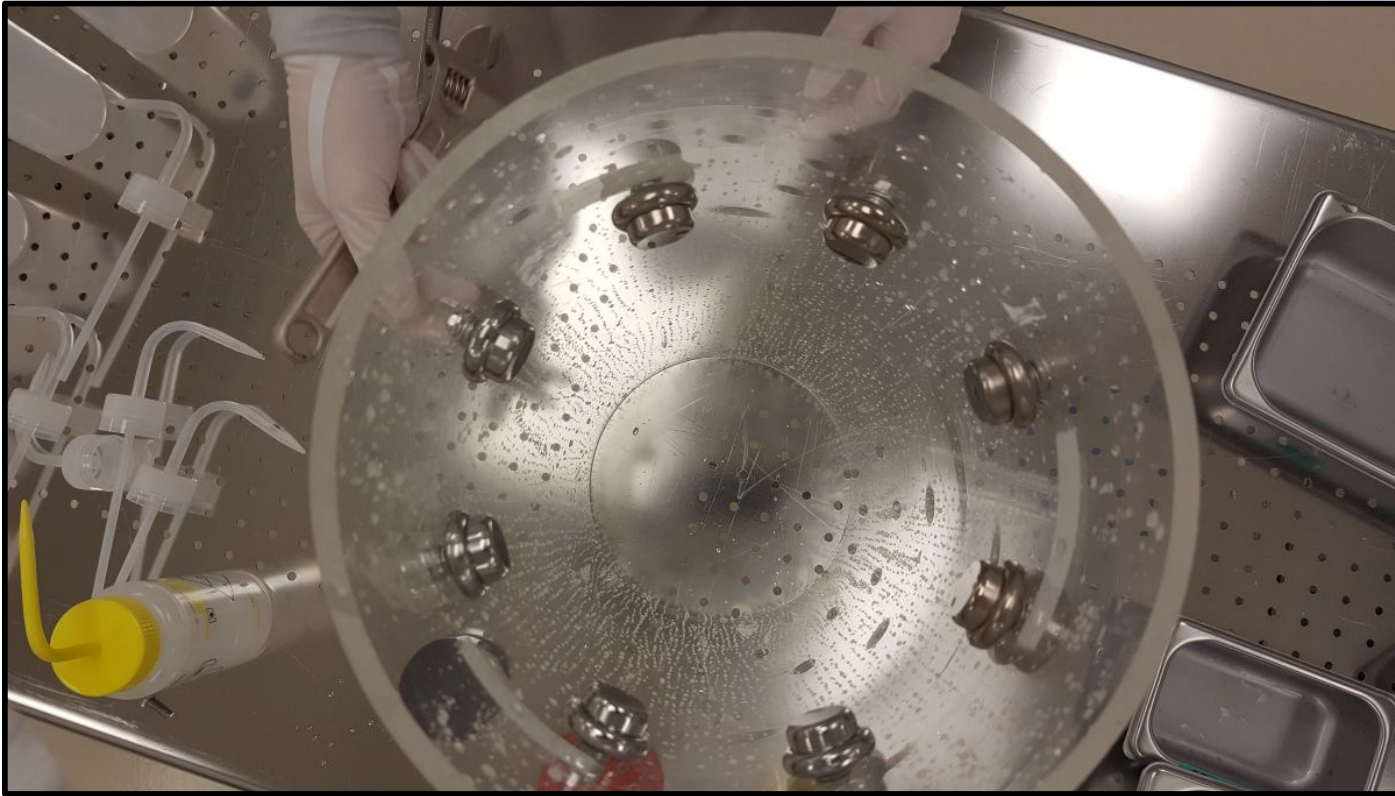
<1 pA leakage current

<10 pT residual magnetization

Cu, Nb, Ti Electrodes (below) and Adjustable Gap Mount (right)



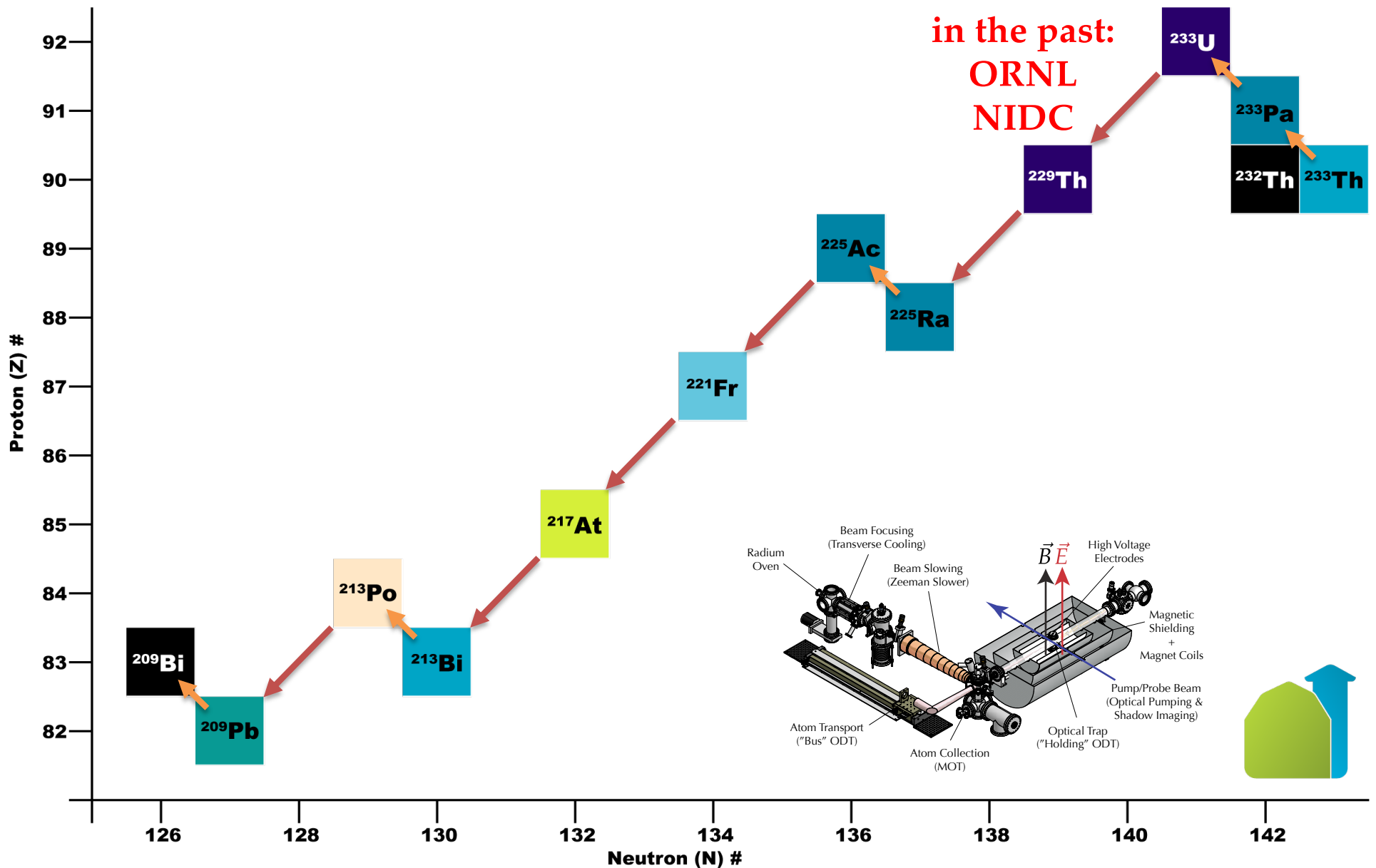
High Pressure Rinse Removes Particulate Contamination



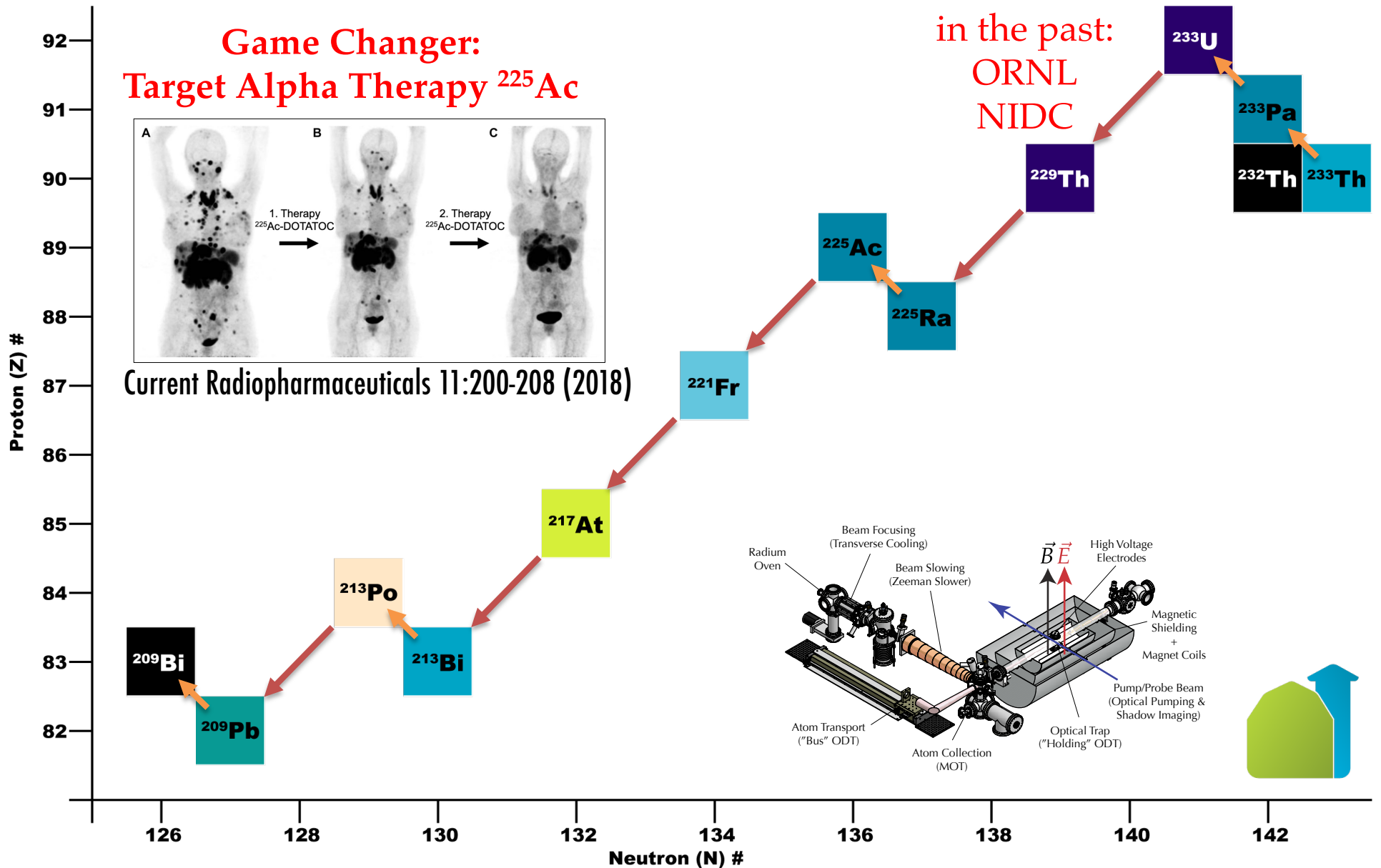
- 1200 psi for 20 minutes
- 18.1 M Ω -cm rinse resistivity
- Rinse & installation performed in class 100 environments

R. Ready, et al. NIMA 1014 165738 (2021)

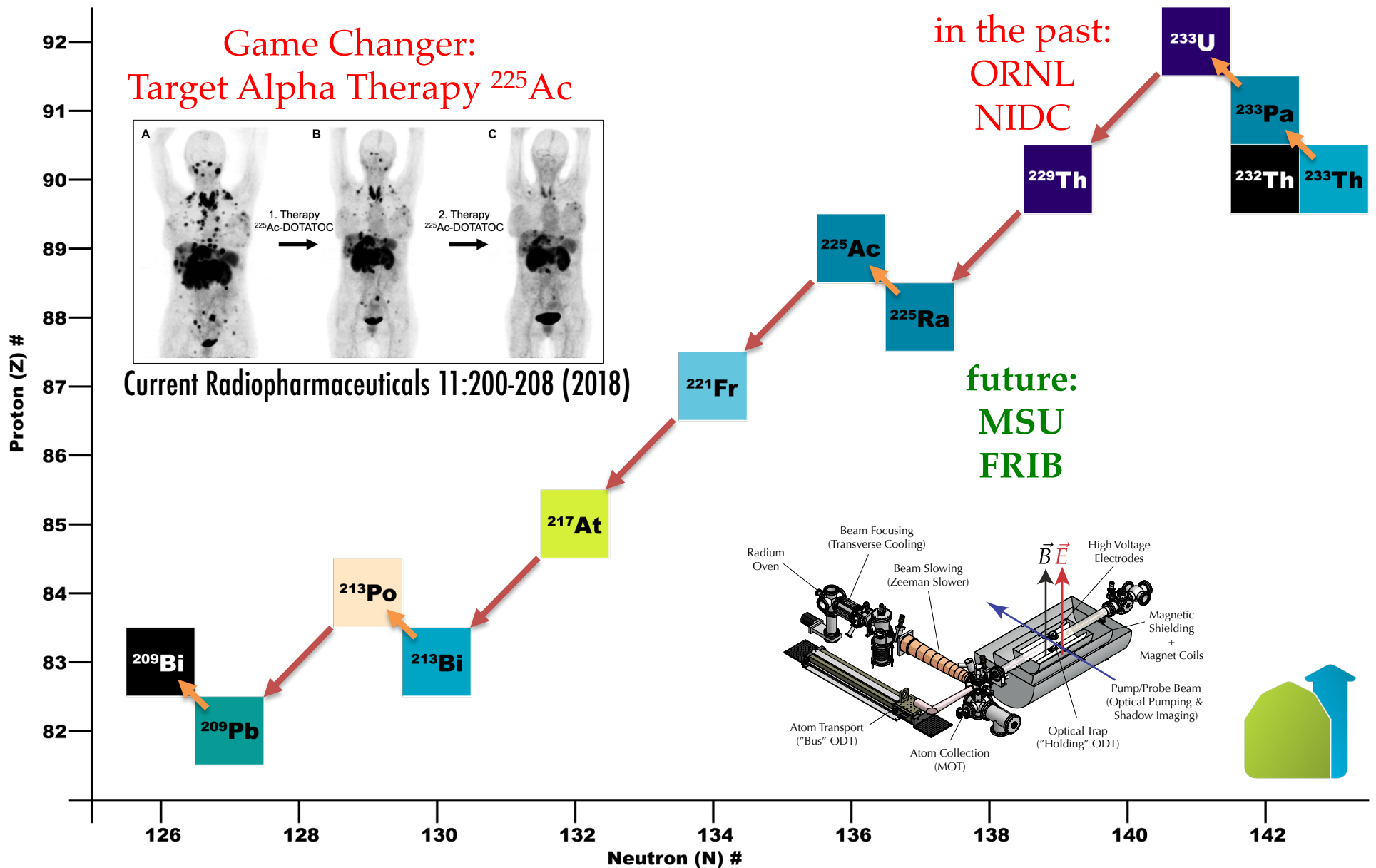
Source of Radium-225 Atoms ($\tau_{1/2} = 15$ days)



Source of Radium-225 Atoms ($\tau_{1/2} = 15$ days)



Source of Radium-225 Atoms ($\tau_{1/2} = 15$ days)



Facility for Rare Isotope Beams @ MSU

Michigan State University
East Lansing, MI
Very Bad at American Football
Home of FRIB



Google Maps & Wikipedia Commons

Facility for Rare Isotope Beams @ MSU

Michigan State University
East Lansing, MI
Very Bad at American Football
Home of FRIB

University of Michigan
Ann Arbor, MI
Very Good at American Football
no FRIB



Google Maps & Wikipedia Commons

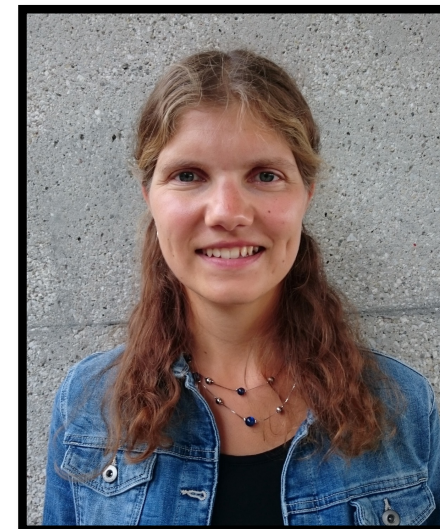
“Isotope Harvesting” at The Facility for Rare Isotope Beams (MSU/East Lansing)



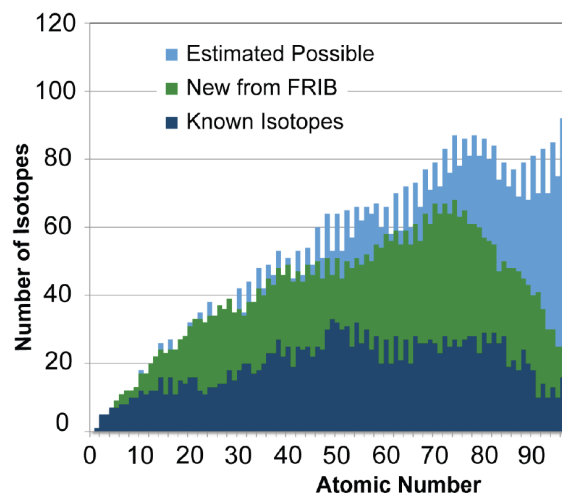
Prof. Greg Severin



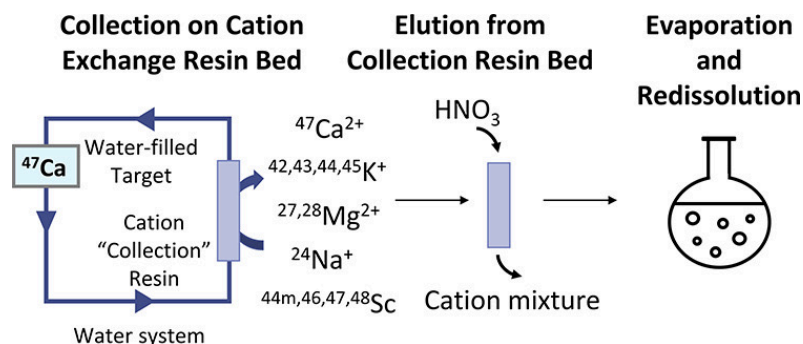
Prof. Alyssa Gaiser



Prof. Katharina Domnanich



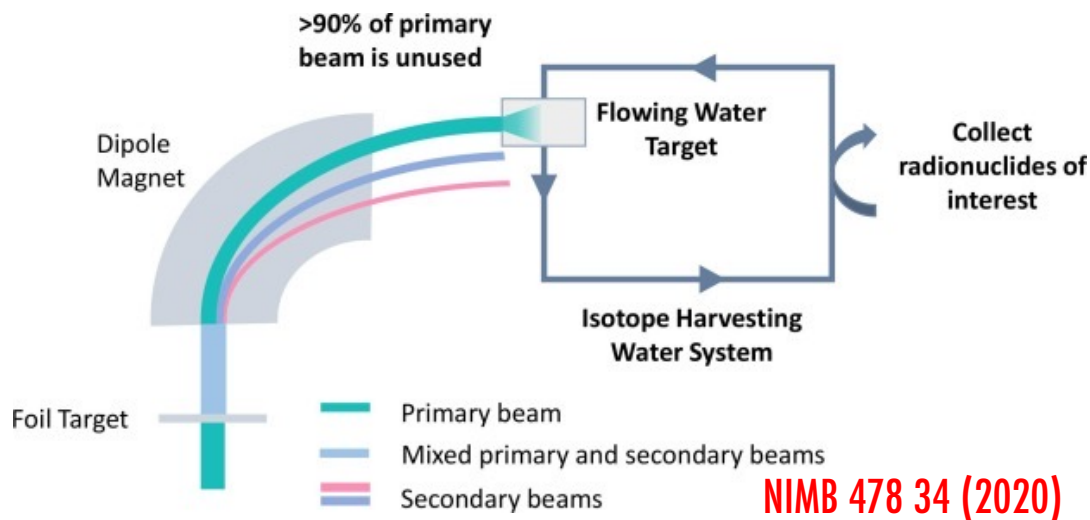
Nature 486, 509–512 (2012)



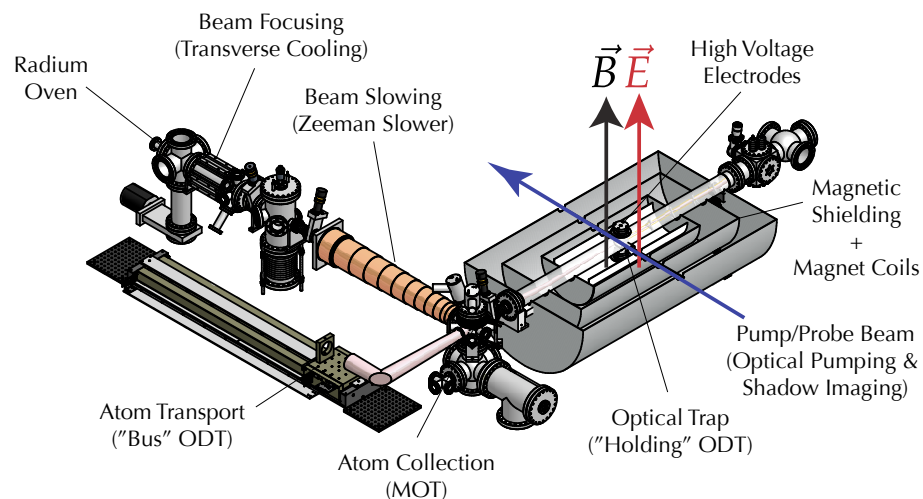
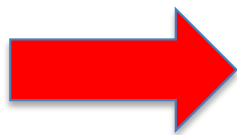
**Recovery of 92%
to 99%
of ⁴⁷Ca
(surrogate for
Radium)**

Abel et al., ACS Omega 5(43) 27864 (2020)

\$upport Needed For “Beaker to Experiment”



- FRIB Operations is supported by DOE-NP
- Isotope Harvesting @ FRIB is supported by DOE-Isotopes



Thanks For Your Attention! More Questions?

1. Tests of fundamental symmetries provide access to New Physics.
2. The discovery of a nonzero electric dipole moment would indicate the presence of New Physics which could explain the Baryon Asymmetry of the Universe.
3. Pear-shaped (octupole-deformed) nuclei have enhanced sensitivity to symmetry violations.
4. FRIB will provide access to rare heavy pear-shaped nuclei.
5. Tomorrow:
 - Other symmetry-violating static electromagnetic moments
 - Some New Physics context
 - Other systems including Radioactive Molecules

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U.S. DEPARTMENT OF
ENERGY

Office of
Science

DOE Early Career Award 2018
DE-SC0019015 (EDM3)
DE-SC0019455 (Ra EDM)

GORDON AND BETTY
MOORE
FOUNDATION



NSF CAREER 2017
#1654610 (SAM)