

# Shape and size of highly concentrated micelles CTAB/NaSal by small angle neutron scattering



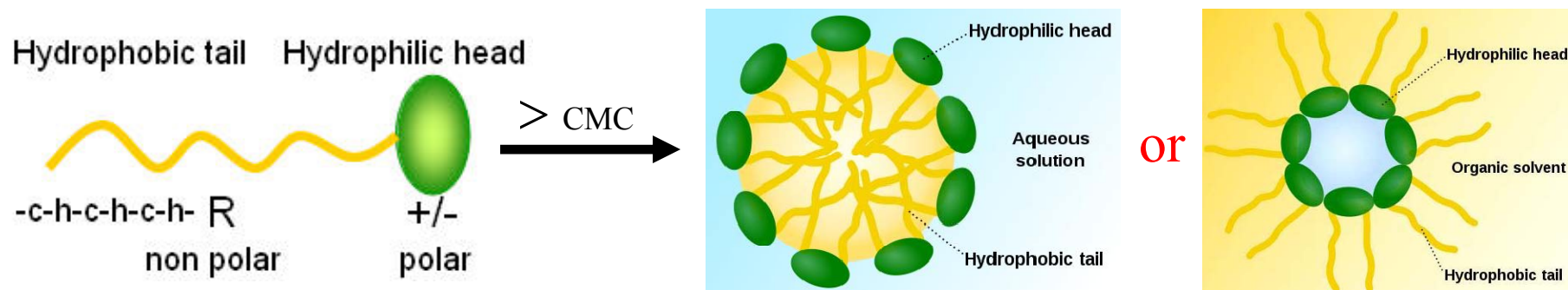
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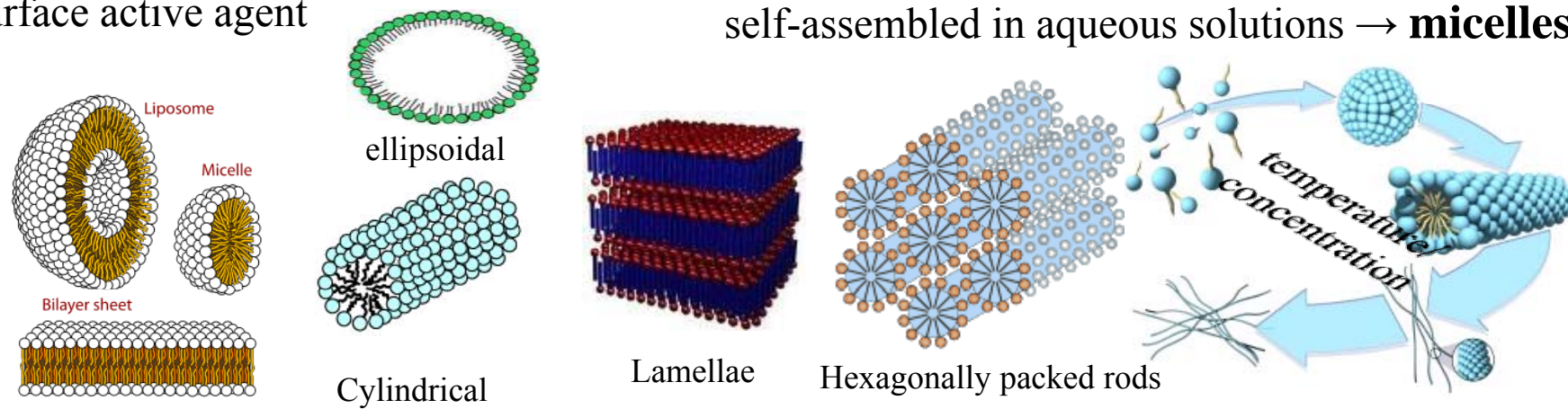


# Surfactants and Micelles



A surfactant molecule (organic amphiphilic)  
= surface active agent

Aggregates of surfactant molecules  
self-assembled in aqueous solutions → **micelles**



Size of head group; length and number of tails; charge on surfactant; temperature; concentration; pH; ionic strength; flow conditions

# Applications of micelles

## Oil field applications:

Viscoelastic type micelles used for fracturing fluids in the oil fields. Small molecule; recovers back; fewer additives req.



## Hydrodynamic engineering (drag reducing agent):

Heating-cooling fluid. Warm-like micelles: dynamic associated structure-like living polymers



## Rheological modifiers for paints, detergents, lubricant...



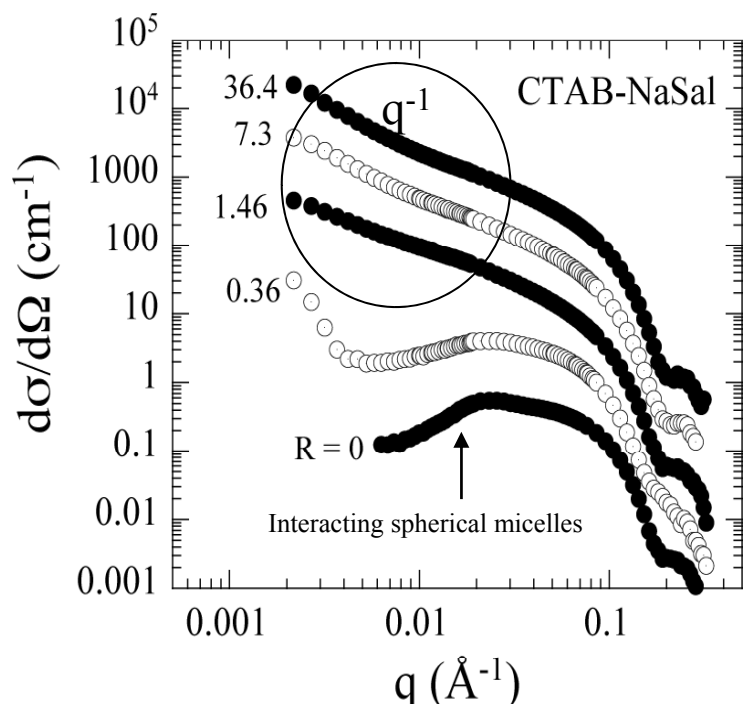
## Home and personal cares:

Viscoelastic property-Warm-like micelles. c.g., hard surface cleaners and drain-opener liquid plumber.

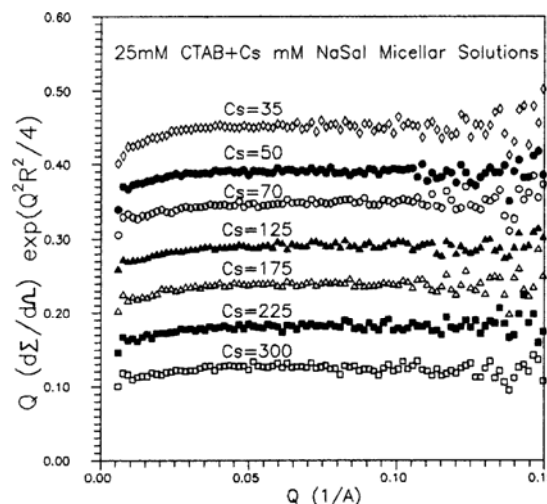


# SANS about CTAB/NaSal

CTAB = 0.2wt.% (5.5mM),  $R=[SAL^{-1}]/[CTAB^{+1}]$



J F Berret Molecular Gels, 667, 2006

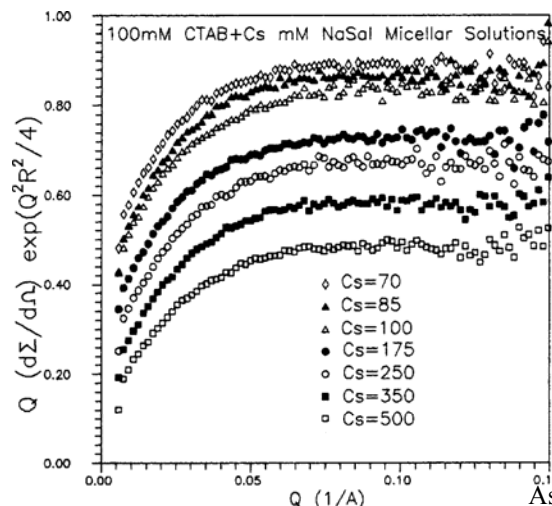


25mM CTAB  
(x mM NaSal)  
**Long rod-like  
Micelles ( $L \gg r$ )**

$$I(Q) \sim \exp(-(Qr)^2/4)/Q$$

$$r_b = 22 \pm 1 \text{\AA},$$

$$L = 250 \pm 25 \text{\AA}$$



100 mM CTAB  
(x mM NaSal)  
**Ellipsoid Micelles**

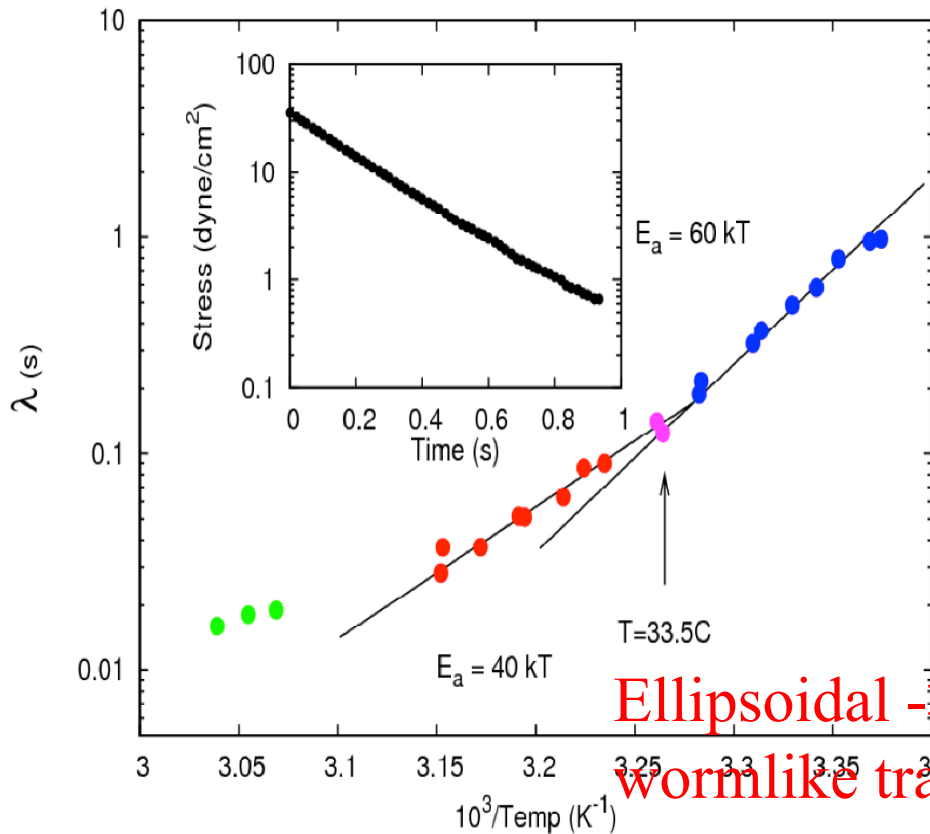
$$r_b = 22 \pm 1 \text{\AA},$$

$$r_a = 44 \pm 5 \text{\AA}$$

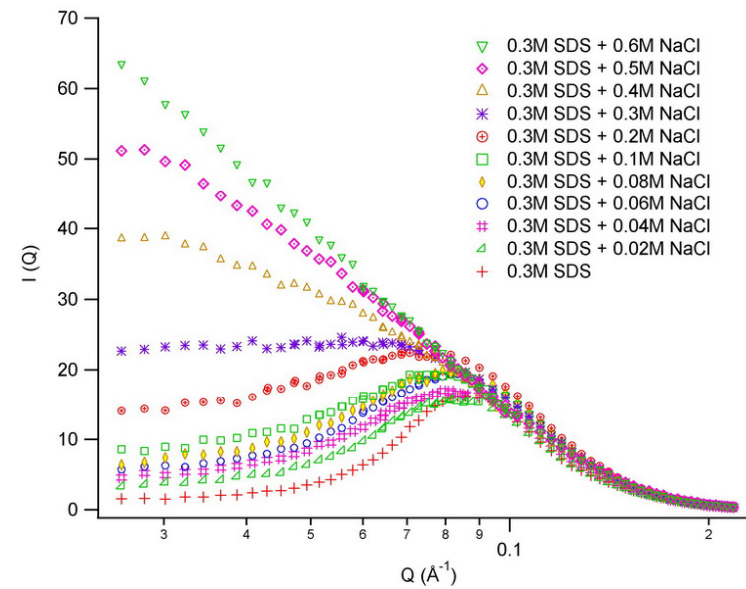
Aswal et al. J. Phys. Chem. B, 102, 2469, 1998

# Motivation and Objective

## Rheological Relaxation time measurements



Ellipsoidal →  
 wormlike transition?



Major axis: 22 → 250Å  
 (ellipsoidal → worm like micelles)

Ref: Small Angle Neutron Scattering BATAN

Joseph (Josh) Gladden, Dept. of Physics, University of Mississippi

## Low Energy Neutron Source at Indiana University



Accelerator	13 MeV
Moderator	Coupled < 20 K solid methane
Wavelength Range	4 Å - 14 Å
Q Range	0.005 to 0.3 Å <sup>-1</sup>
Pulse Width	600us
Source Frequency	10 to 30 Hz
Collimation	Circular pinhole collimation
Area Detector ( <sup>3</sup> He 2D ORDELA)	
Active Volume	64 x 64 cm <sup>2</sup> , 4.4 cm thick
Pixel Size	1 x 1 cm <sup>2</sup>
Detector Efficiency	71% for 5 Å neutrons, 52% for 3 Å neutrons
Count-Rate Capability	10 <sup>4</sup> n/s for 10% coincidence losses (10 <sup>5</sup> n/s max.)
Integrated Flux on Sample	2*10 <sup>4</sup> n/cm <sup>2</sup> /s (at full accelerator power of 13 kW)

### SANS Science Applications

#### Polymers

Molecular self-assembly and interactions in complex fluids; Colloids and microemulsions; Micelles;

#### Materials Science

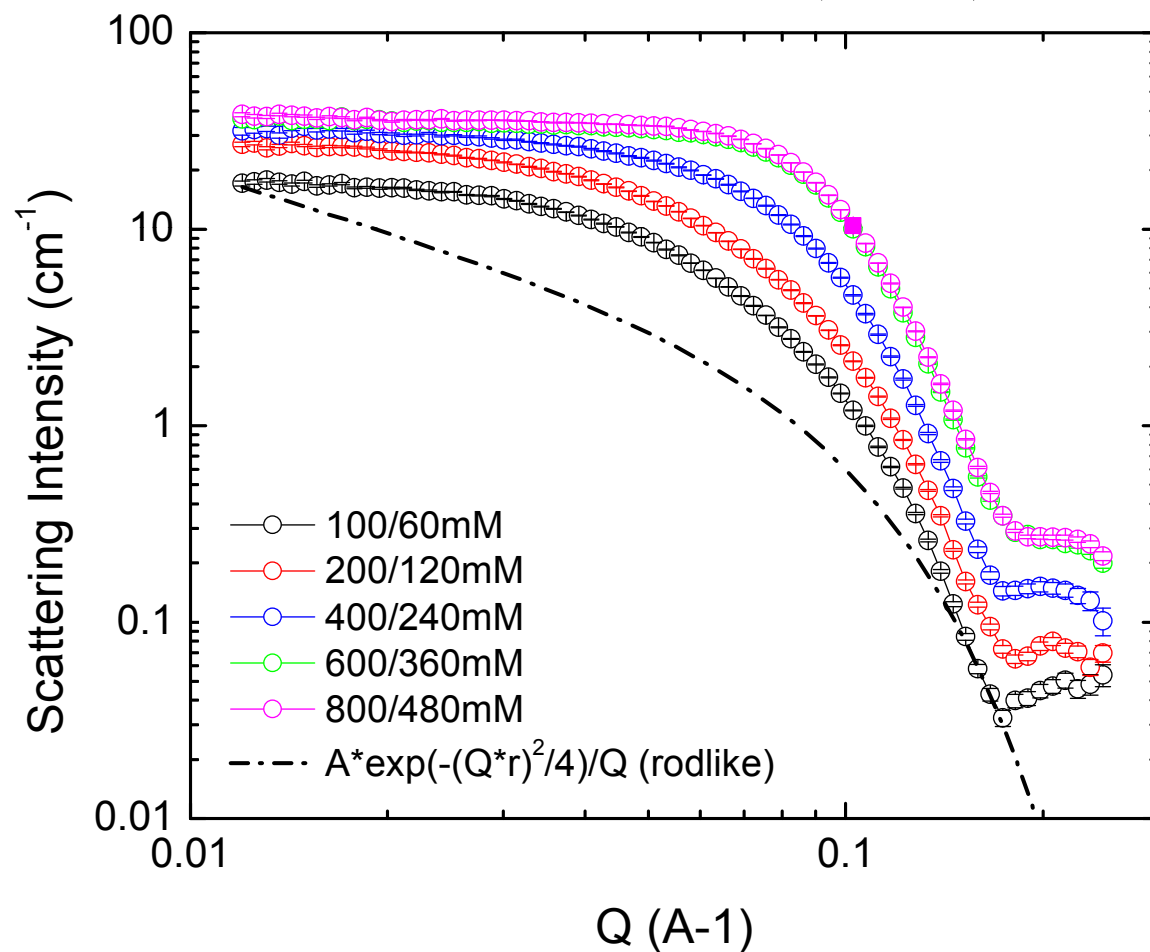
Phase separation in alloys and glasses; Morphologies of superalloys; Nanocomposites

#### Biological Macromolecules

Size and shape of proteins; macromolecular complexes  
Hierarchical biological structures; Biomembranes

## Preliminary Evaluation of Micelles Structures

Micelles CTAB/NaSal (=0.60),  $T = 293^{\circ}\text{C}$



**Possible Shapes:**

- Spheres
- Ellipsoid

# SANS Data Modeling

$$\frac{d\Sigma}{d\Omega} = n_m (\rho_m - \rho_s)^2 V_m^2 \langle F(Q) \rangle^2 S(Q) + bkgd$$

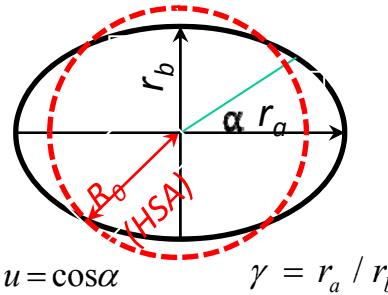
## ❖ Particles F(Q,x)– Ellipsoid

Density- $n_m$       Volume- $V_m(b) = 4\pi r_b r_a^2 / 3$

Neutron Contrast- $(\rho_m - \rho_s)^2$

Form factor-

$$F(Q, x) = 3(\sin u - u \cos u) / u^3, u = Q r_b [1 + x^2(\gamma^2 - 1)]^{1/2}, u = \cos \alpha \quad \gamma = r_a / r_b$$



## ❖ Size Distribution – Gaussian

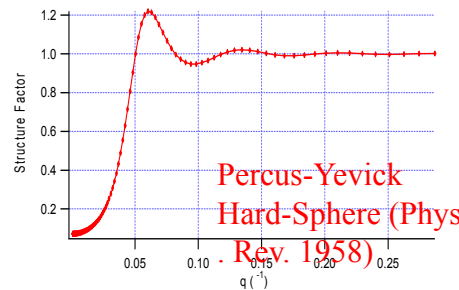
$$f(r_b) = \frac{1}{\sqrt{2\pi\delta^2}} \exp(- (r_b - \bar{r}_0)^2 / 2\delta^2)$$

## ❖ Structural Factor S(Q) – Hard Sphere Model

$$u(r) \begin{cases} 0, & r \geq 2R_0 \\ \infty, & 0, & r < 2R_0 \end{cases}$$

Interparticle potential

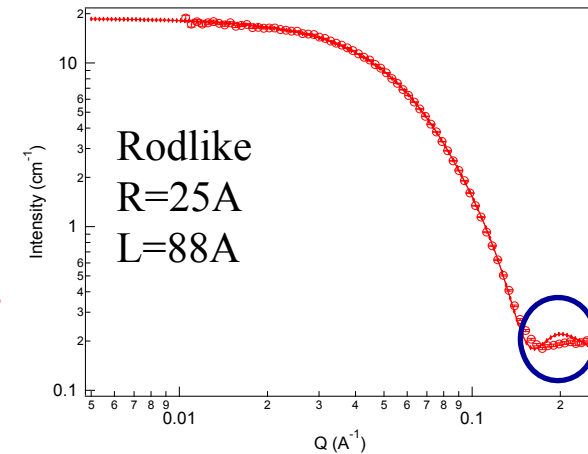
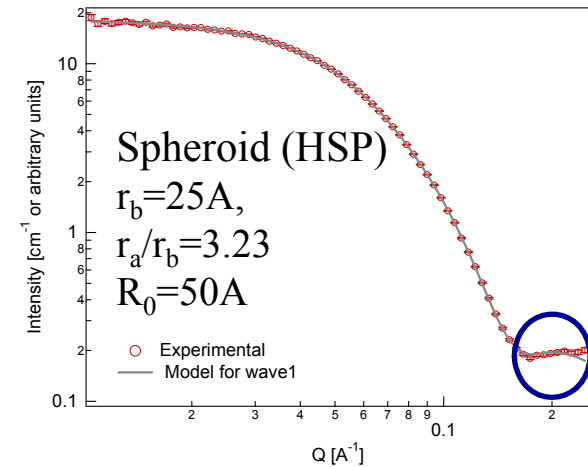
In solution the single particle form factor must be averaged over all angles to give the form factor:



$$\frac{d\Sigma}{d\Omega} = n_m (\rho_m - \rho_s)^2 \int_0^1 V_m^2(r_b) f(r_b) dr_b \int [F(Q, x)]^2 S(Q) dx + bkgd$$

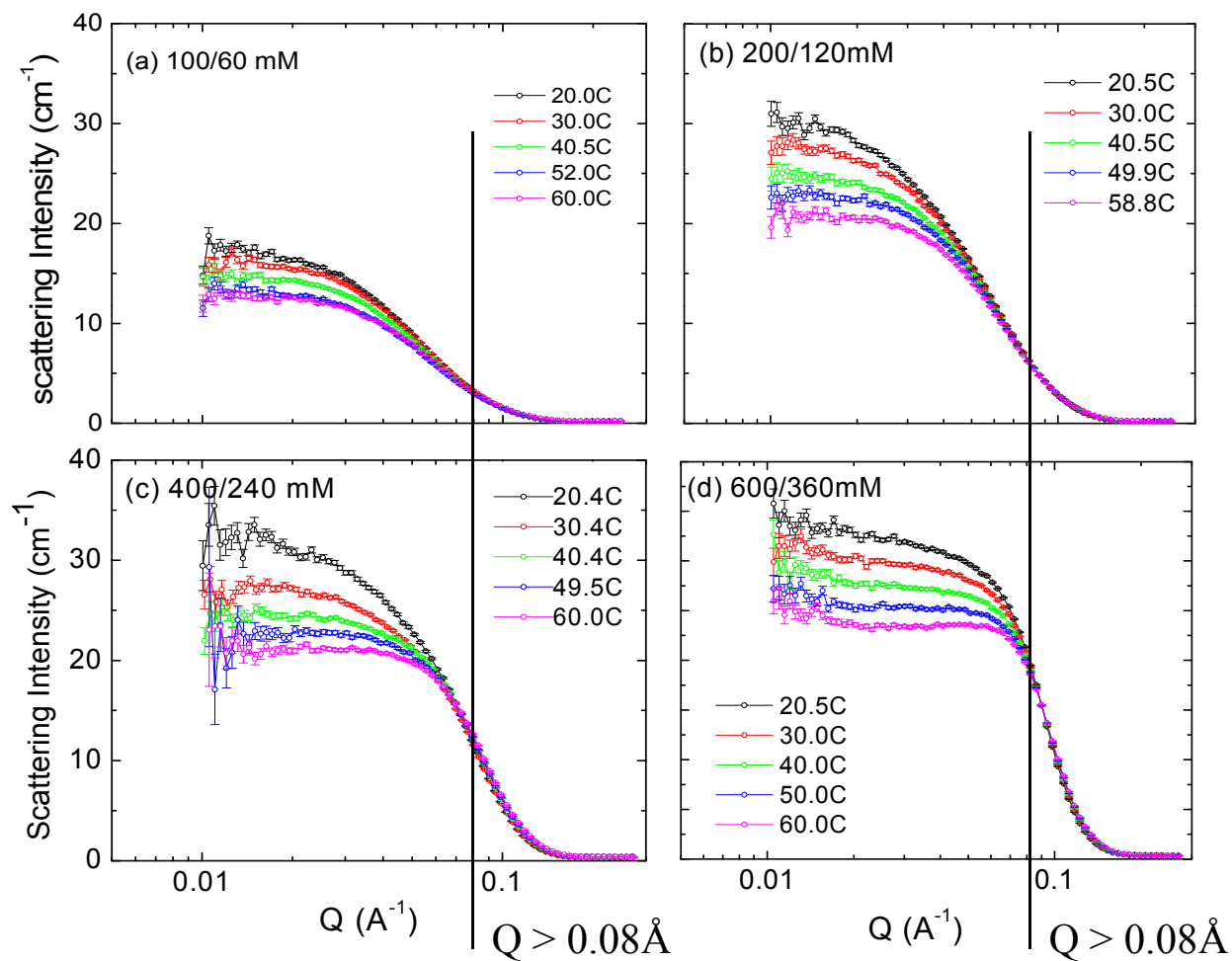
1. Irena Package from the USAXS at APS, ANL: <http://usaxs.xor.aps.anl.gov/staff/ilavsky/irena.html>
2. SANS Igor Pro from SANS at NCNR, NIST: [http://www.ncnr.nist.gov/programs/sans/data/red\\_anal.html](http://www.ncnr.nist.gov/programs/sans/data/red_anal.html)

100/60mM CTAB/NaSal, 20°C





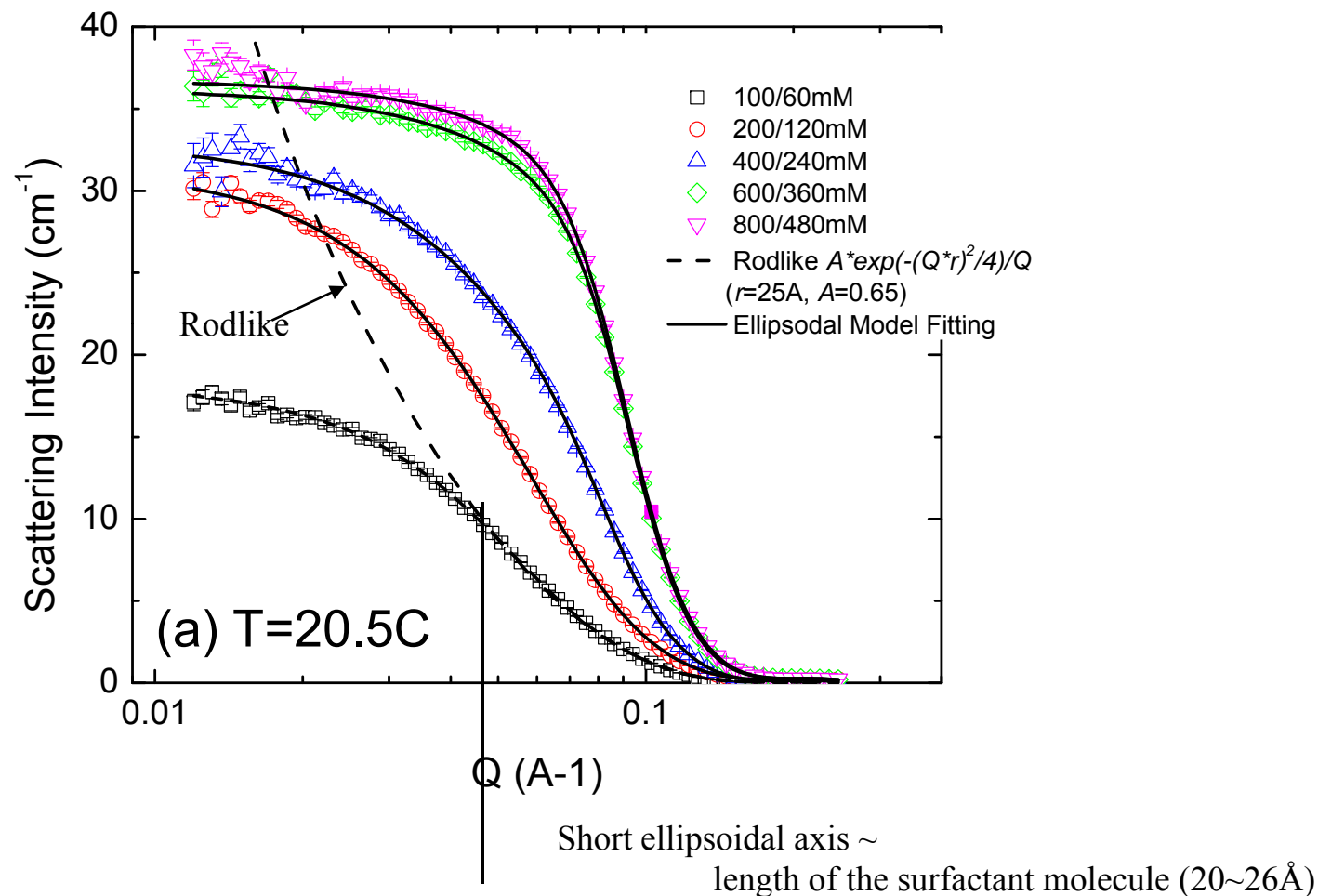
## Temperature dependence of scattering intensity



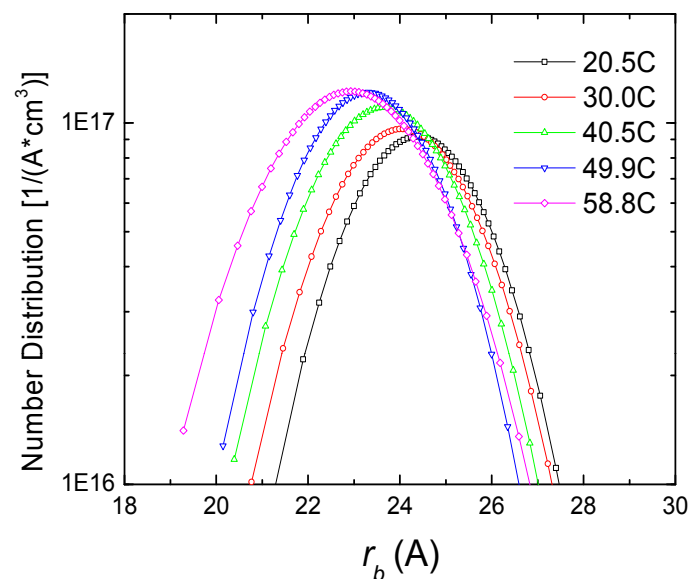
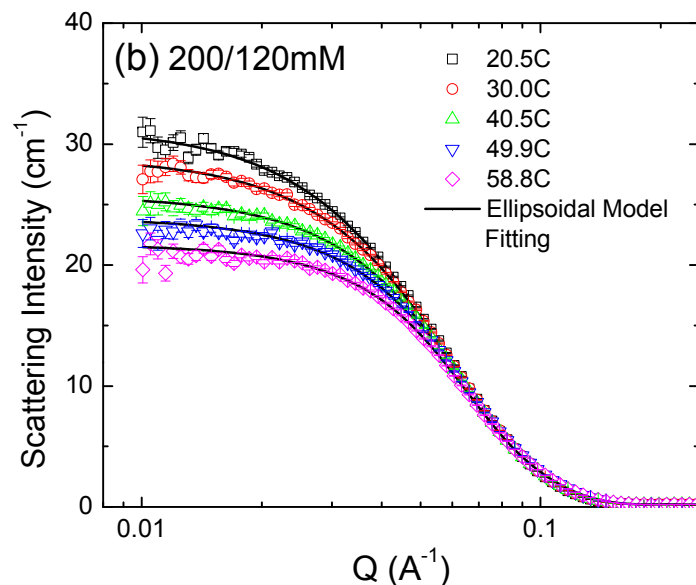
$Q > 0.08 \text{ \AA}^{-1}$   
Short axis remain constant

$Q < 0.08 \text{ \AA}^{-1}$   
Long axis change with temperature  
↓  
shorter with temp.

## Temperature dependence of scattering intensity



## Model fitting

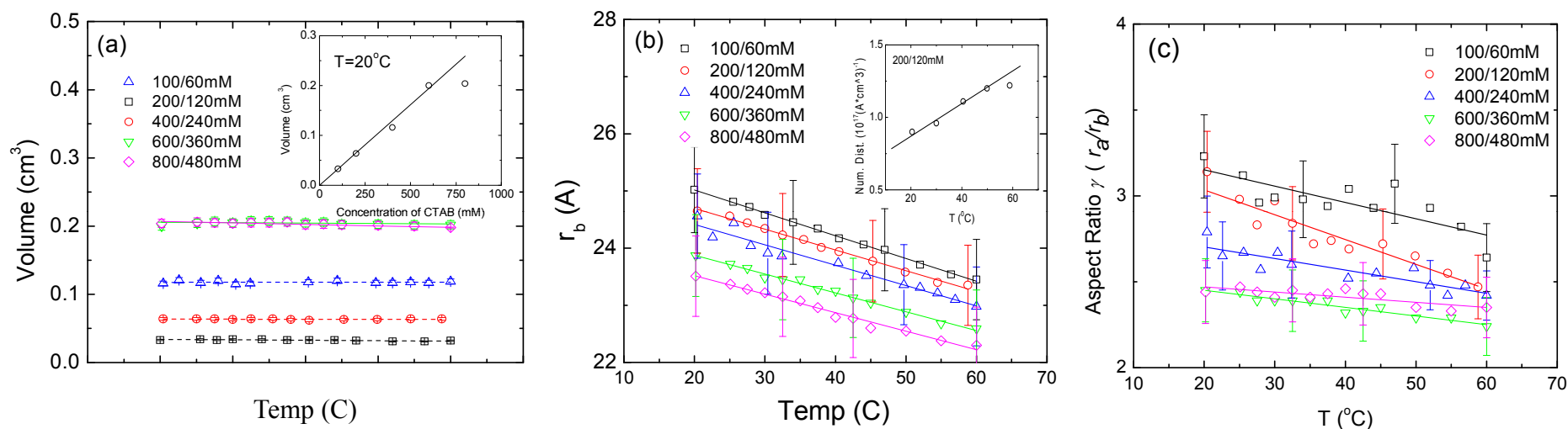


Model: Ellipsoid form, a hard sphere structure factor and Gaussian size distribution

Fitting parameters (7): total scattering volume of micelles, the semiminor axis  $r_b$ , width of Gaussian function ( $\delta$ ), aspect ratio ( $\gamma=r_a/r_b$ ), the radius ( $R_0$ ) and volume fraction ( $\eta=4\pi R_0^3 n_m/3$ ) of hard sphere, and background (*bkgd*).

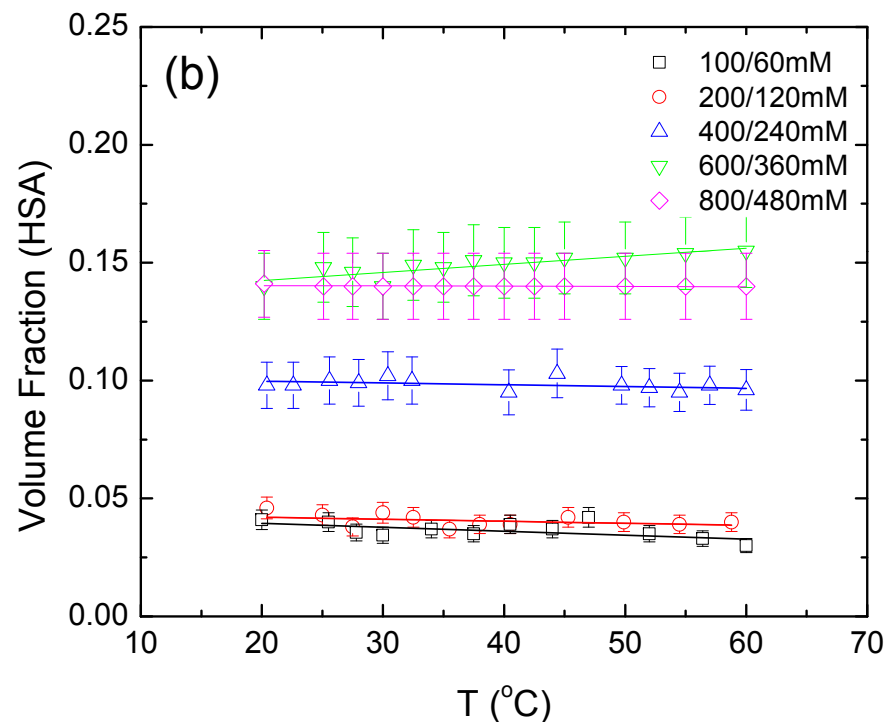
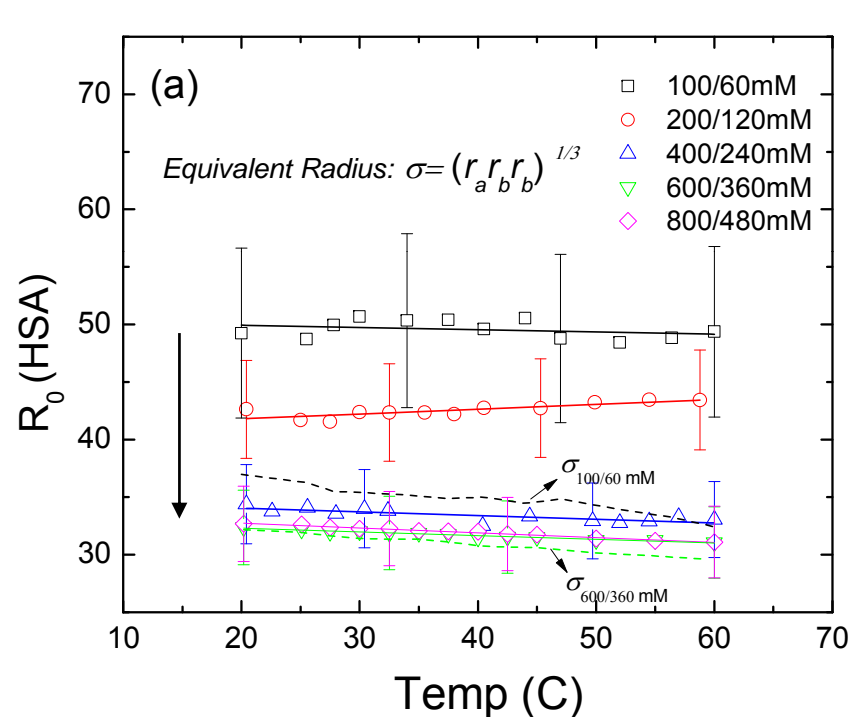
Width ( $\delta$ ) of Gaussian function  $\sim 0.001 \text{ \AA}$ , the semiminor length of the ellipsoidal particle might be simply equal to the length of the surfactant molecule and these ellipsoidal particles could be monodispersed

# Temperature dependence of fitting parameters of Micelles



- Linear decrease in both the semiminor axis  $r_b$  and aspect ratio ( $r_a/r_b$ )
- : Micelles begin to condense with increase in temperature
- : 100/60 mM shows the largest particle size
- :  $r_a$  (growth direction) shortens faster than  $r_b$
- : Volume remains constant-micelles break- and extra broken begin to recombine
- : number density increases with heating

# Temperature dependence of fitting parameters of Micelles



$R_0 \rightarrow 50$  to  $33 \text{ \AA}$  (100/60 to 400/240 mM)

HAS works well for ellipsoidal or more spherical micelles

Volume fraction:  $4\pi R_0^3 n_m / 3$

Temperature effect on size of micelles and number density

## Summary

- ❖ Highly concentration CTAB/NaSal formed ellipsoidal micelle. Ellipsoidal micelles have been investigated by small angle neutron scattering.
- ❖ SANS results suggests that this micelles solution fall in the ellipsoidal regime and micelles shape are independent on the concentration and temperature.
- ❖ Micelles size decreases with concentration and temperature whereas total volume of micelles remain constant, indicating that long micelles start to break on heating and broken surfactant molecules coalesce again to form more micelles.
- ❖ No structural transitions (linear change) in the studied temperature range for highly concentration CTAB/NaSal.